

# Deconfinement phase transition with heavy quarks

Pok Man Lo

*GSI*

*NeD & TURIC*

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*pml@gsi.de*

In collaboration with...

Bengt Friman (*GSI*)

Chihiro Sasaki (*FIAS*)

Krzysztof Redlich (*U. of Wroclaw*)

Olaf Kaczmarek (*U. of Bielefeld*)

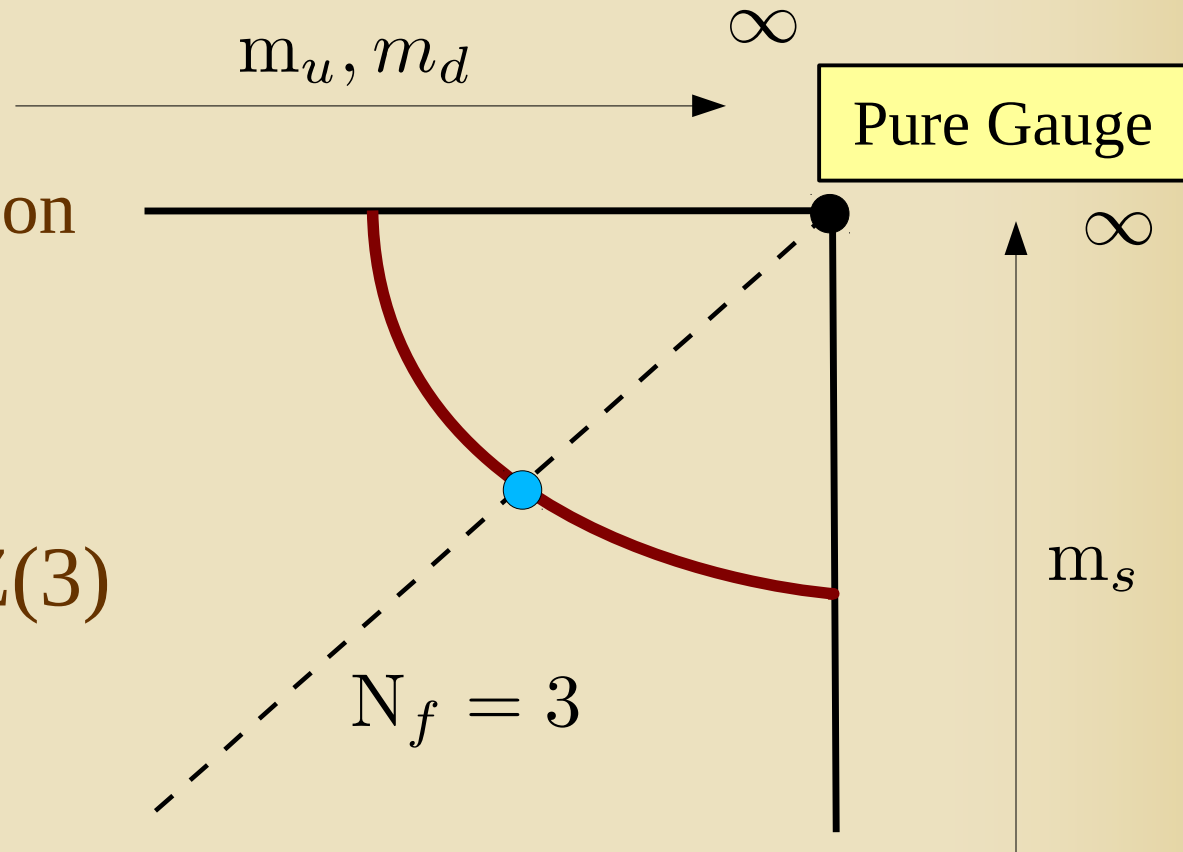
# Content

Deconfinement phase transition with heavy quarks

- Effective theory for PL coupled with heavy quarks
- Critical quark mass and phase boundary
- Quark mass dependence of transition temperature

# Deconfinement phase transition

- Pure SU(3)
  - 1<sup>st</sup> order phase transition
  - Stable against small explicit breaking
- Heavy quark breaks Z(3)
  - Strength  $\uparrow$  as  $m \downarrow$



1<sup>st</sup> order  $\rightarrow$  2<sup>nd</sup> order (deconfining CEP)  $\rightarrow$  crossover

# Polyakov loop

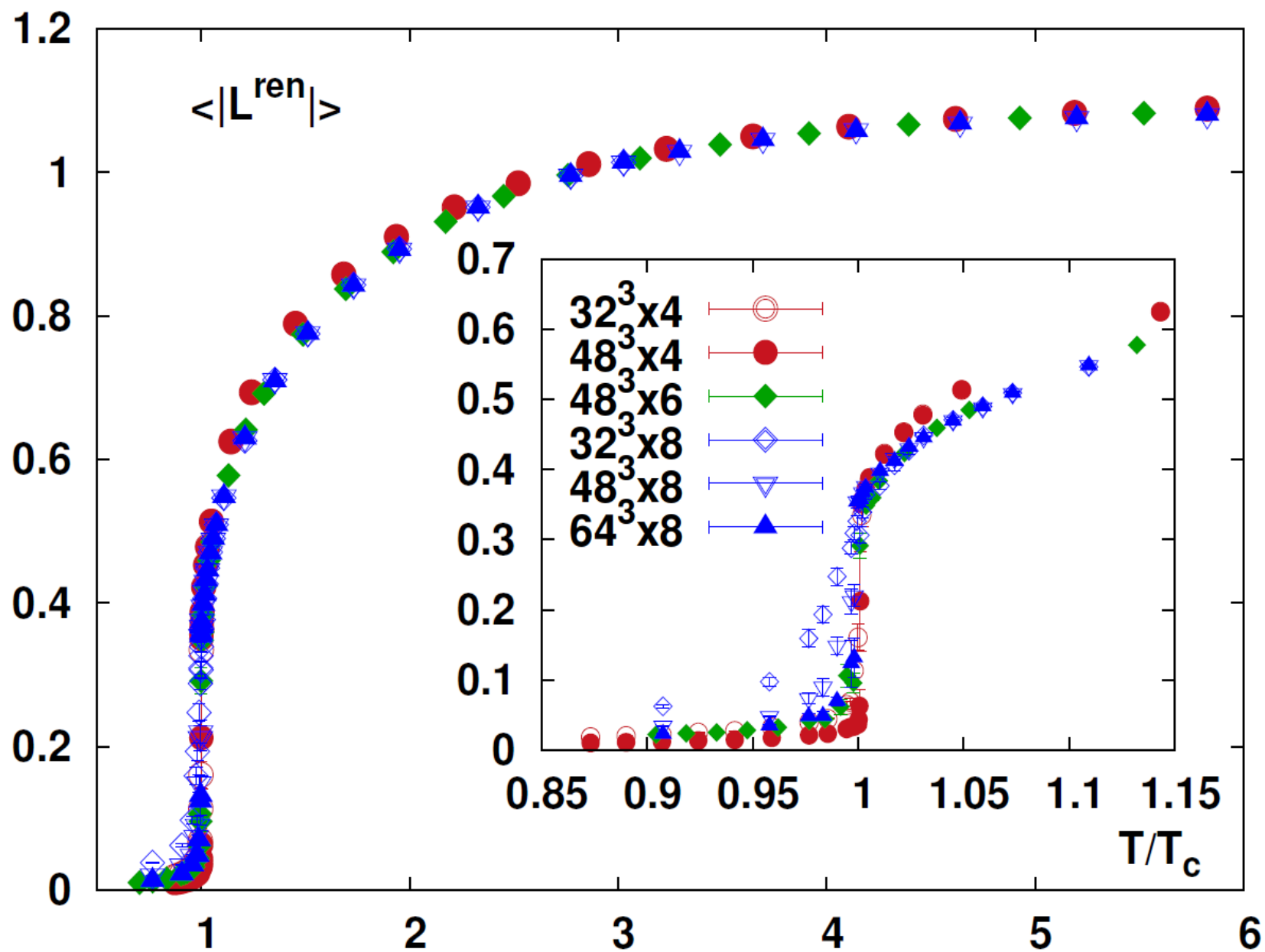
- Order parameter **characterizes** the state of the system

$$\langle L \rangle$$

Operator does **not** respect  
the symmetry

$$L \rightarrow L e^{i2n\pi/3}$$

confined phase:  $\langle L \rangle = 0$   
deconfined phase:  $\langle L \rangle \neq 0$



# Polyakov loop susceptibilities

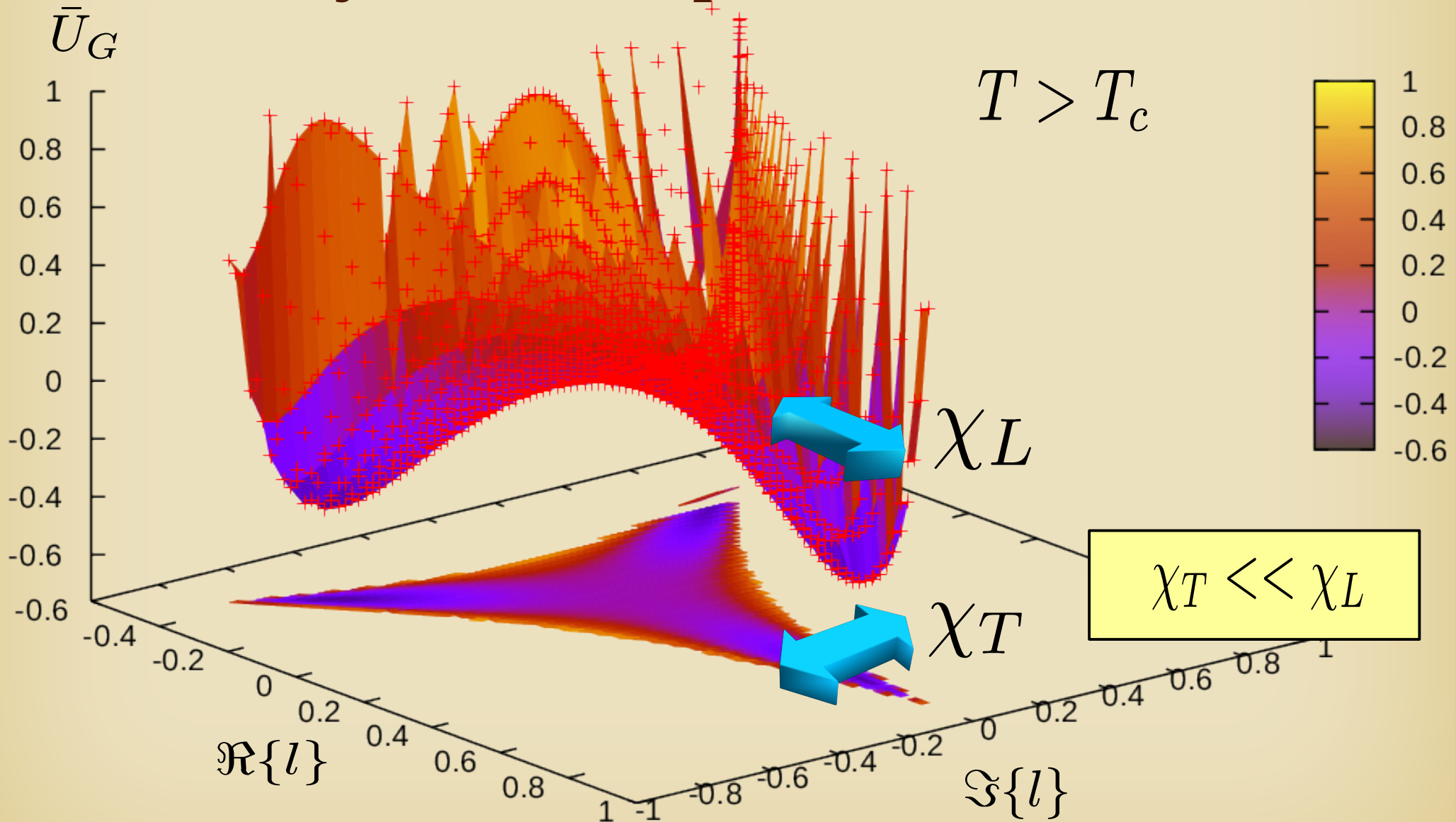
- $L$  is complex-valued for SU(3)

real sector:

$$L = L_L + iL_T \longrightarrow \begin{aligned} \chi_L &= V(\langle L_L L_L \rangle - \langle L_L \rangle^2) \\ \chi_T &= V(\langle L_T L_T \rangle - \langle L_T \rangle^2) \end{aligned}$$

- Sensitive to the **transition** of phases  
features **peak** and **width** near the transition
- Effective potential: inverse of curvature

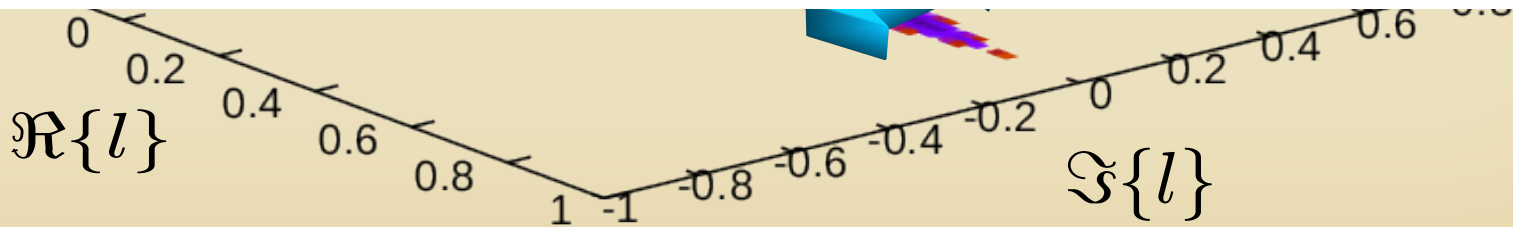
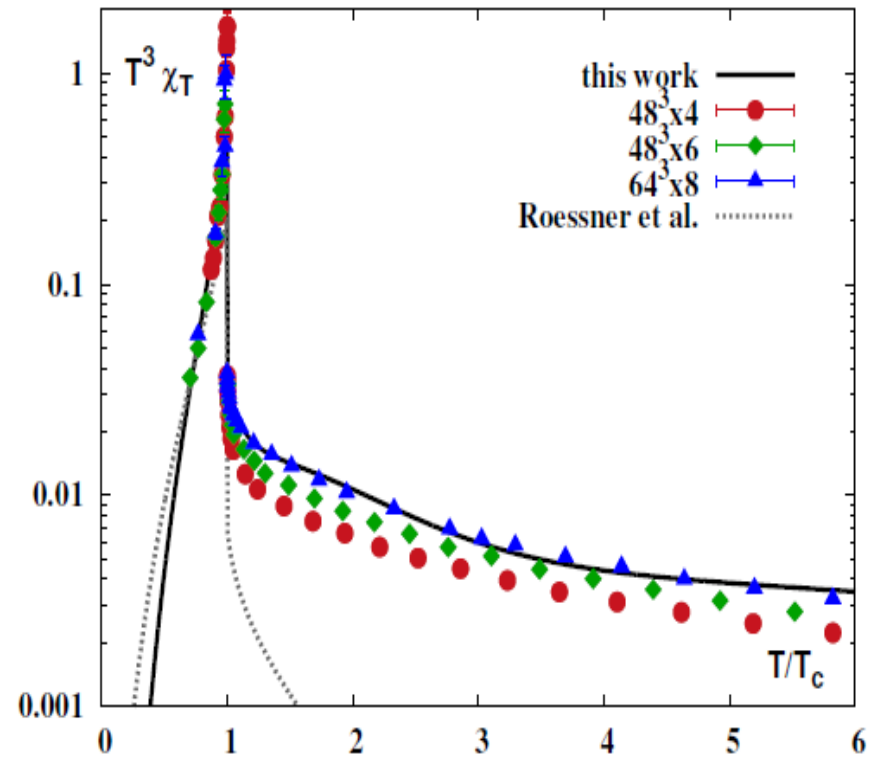
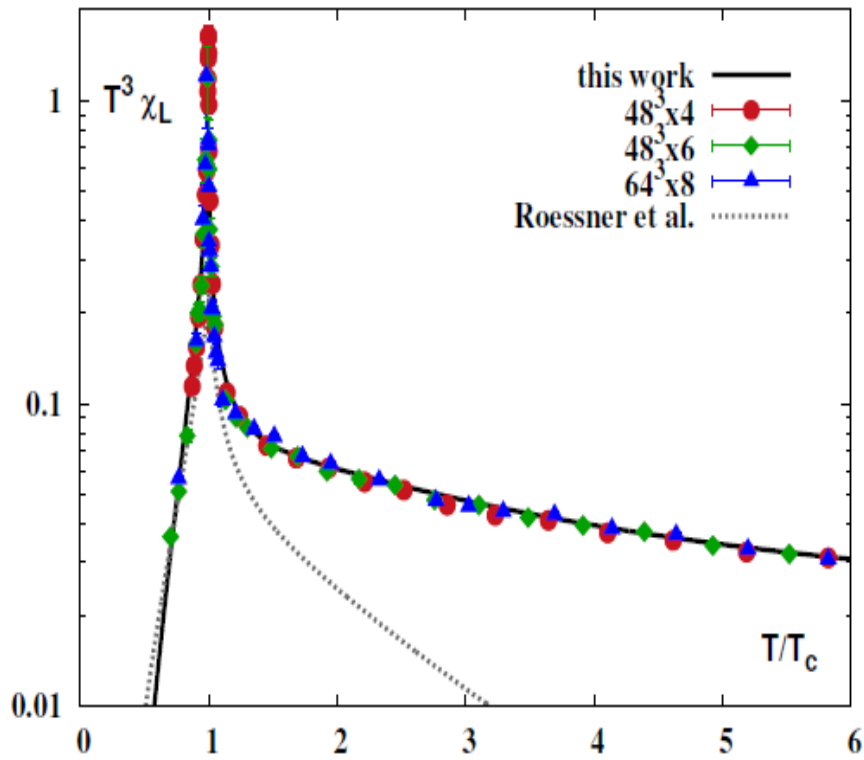
# Polyakov Loop Eff. Potential





# Polyakov Loop Eff. Potential

$\bar{U}_C$



# Construction of PL effective model

Z(3) symmetry, Haar measure...



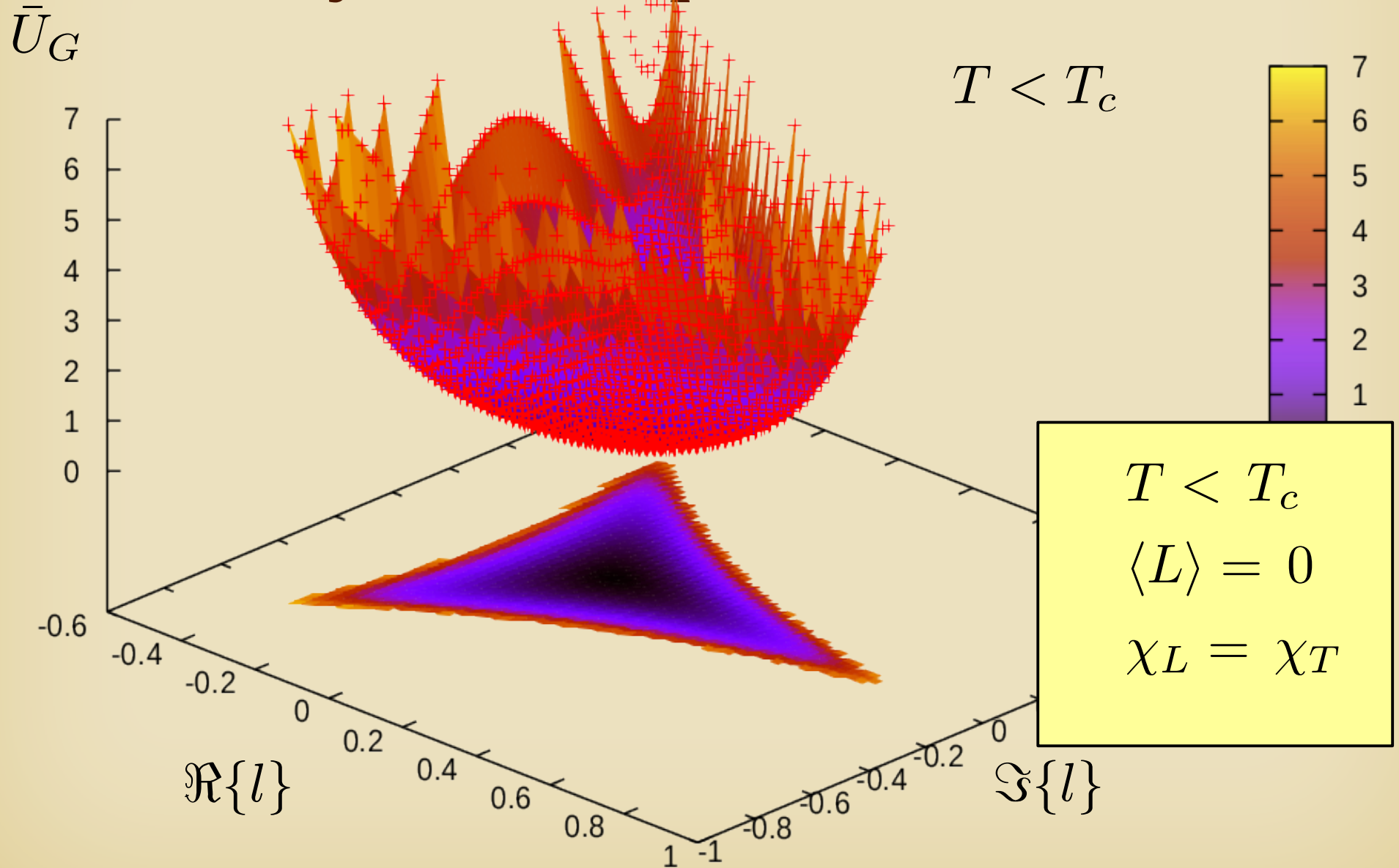
$$U_{eff}[L, \bar{L}] = -\frac{A[T]}{2} \bar{L}L + B[T] \ln M_{Haar} + \frac{1}{2} C[T] (L^3 + \bar{L}^3) + D[T] (\bar{L}L)^2$$



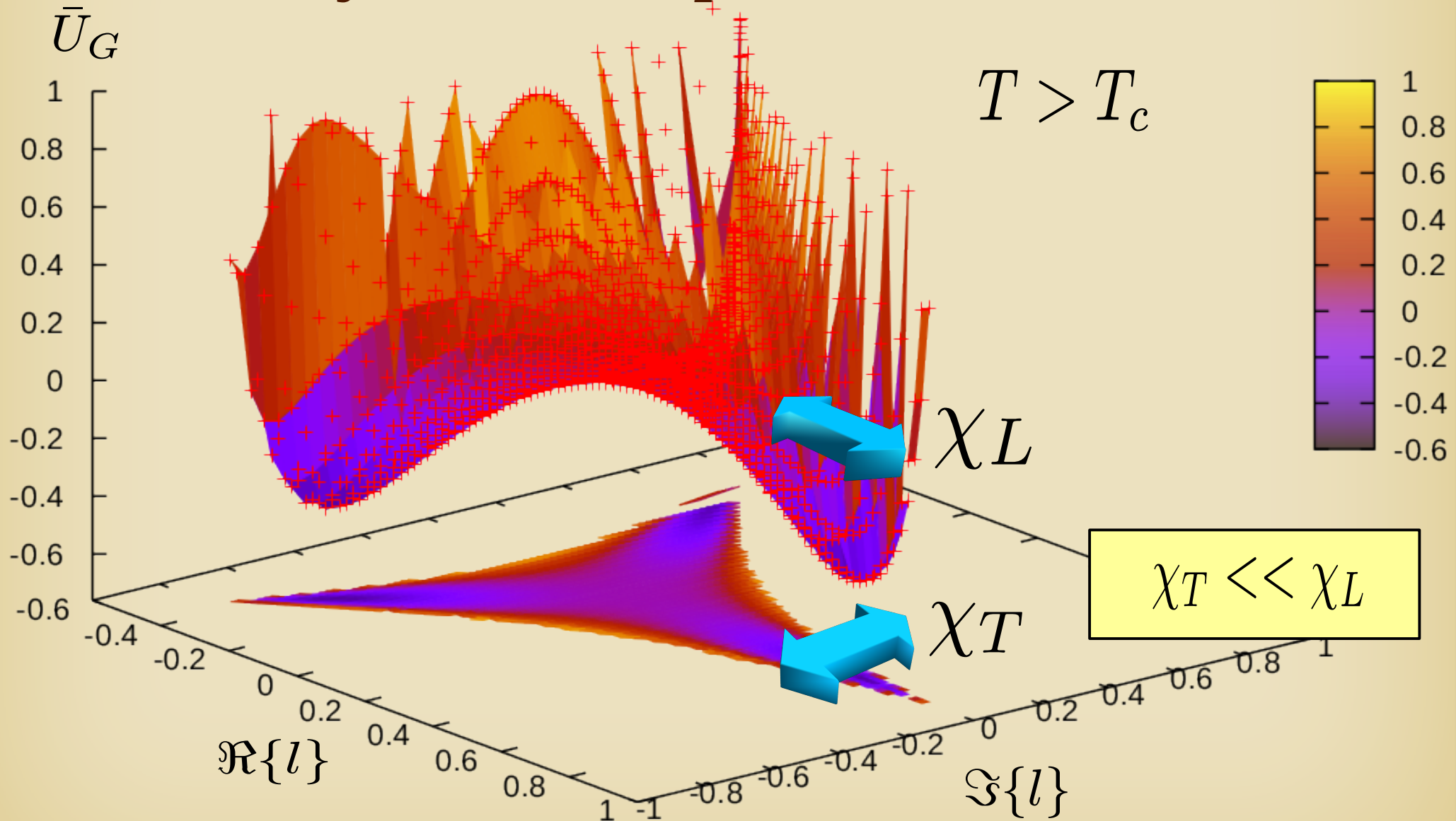
lattice inputs

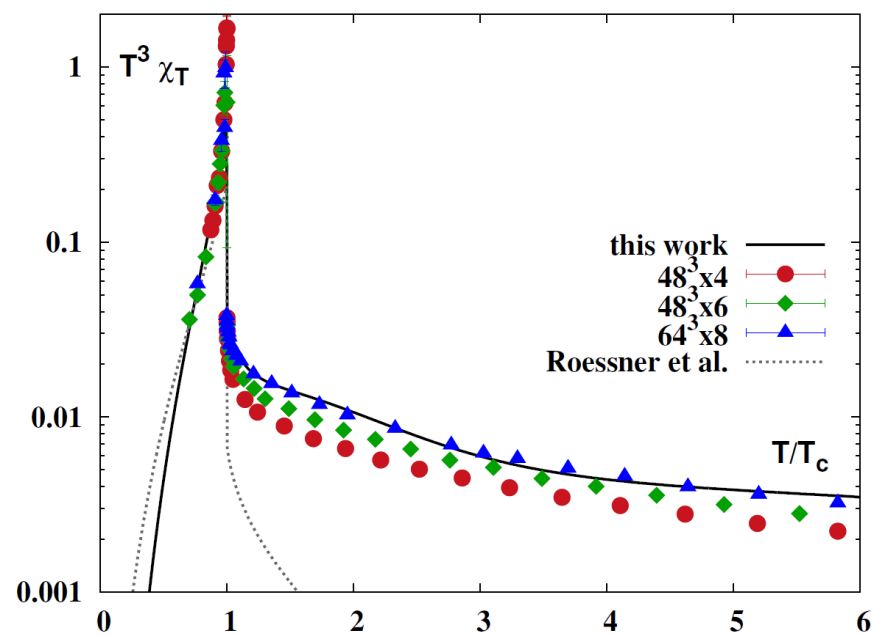
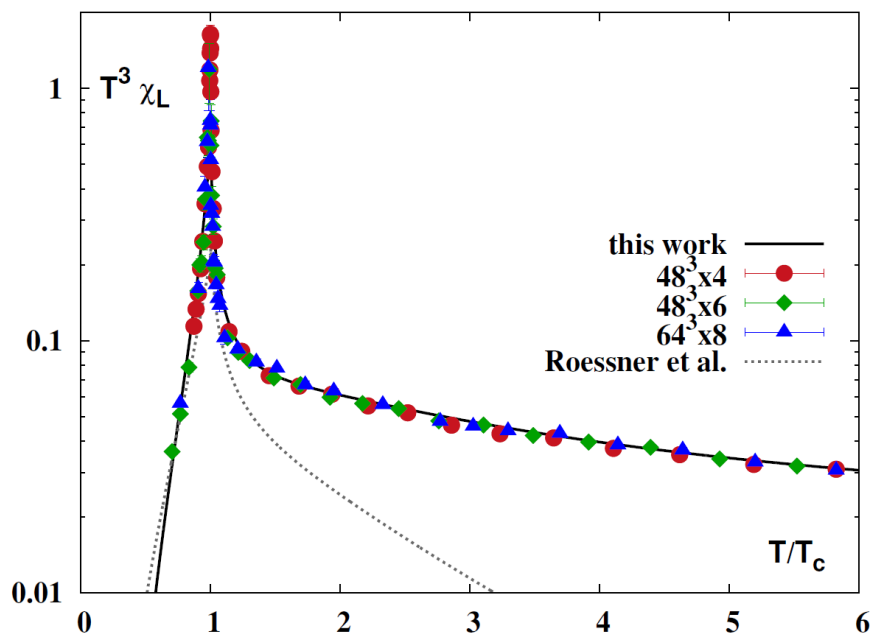
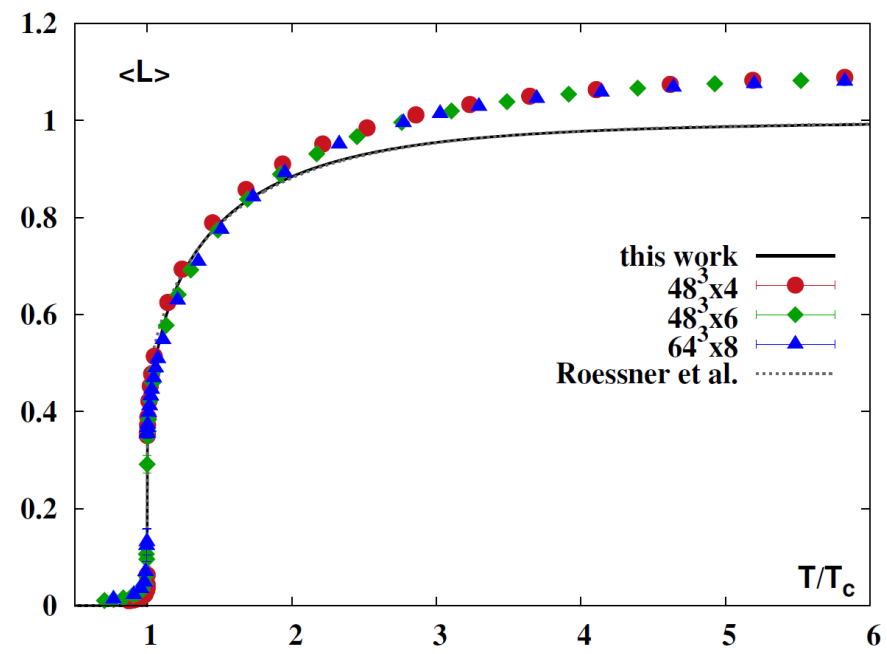
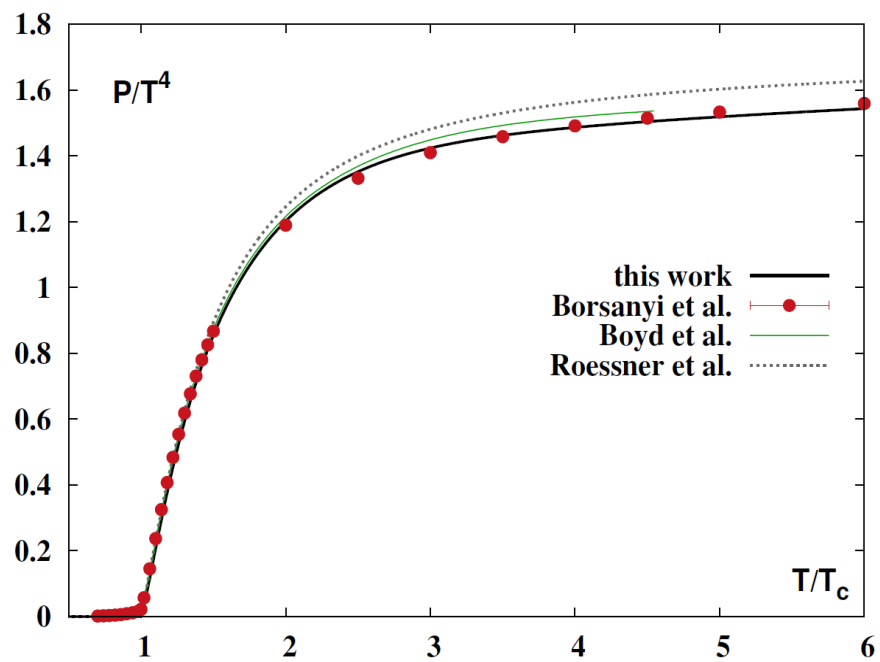
$$P[T], \langle L \rangle, \chi_L, \chi_T$$

# Polyakov loop Eff. Potential



# Polyakov Loop Eff. Potential





# PL-heavy quark coupling

- Fermionic determinant

$$Z = \int DLD\bar{L} \det[\hat{Q}_F] e^{-\beta V U_G[L, \bar{L}]}.$$

- Background field approach

$$\hat{Q}_F = (-\partial_\tau + \mu + igA_4)\gamma^0 + i\vec{\gamma} \cdot \nabla - M_Q$$

$$\hat{L} = e^{i\beta g A_4^a T^a}$$

$$L = \frac{1}{N_c} \text{Tr}_c \hat{L}$$

# PL-heavy quark coupling

- Fermionic determinant (1 loop)

$$\ln \det[\hat{Q}_F] = V 2N_f \int \frac{d^3 k}{(2\pi)^3} [3\beta E[k] + \ln g^+ + \ln g^-]$$

$$g^\pm = 1 + 3 \left( \frac{L}{\bar{L}} \right) e^{-\beta E^\pm} + 3 \left( \frac{\bar{L}}{L} \right) e^{-2\beta E^\pm} + e^{-3\beta E^\pm}$$

$$E^\pm = E[k] \mp \mu$$

$$E[k] = (k^2 + M_Q^2)^{1/2}$$

# PL-heavy quark coupling

- Effective potential

$$\ln \det[\hat{Q}_F] = -VT^3 \bar{U}_Q[L, \bar{L}; M_Q]$$

- Heavy quark limit ( $M_Q/T \gg 1$ )

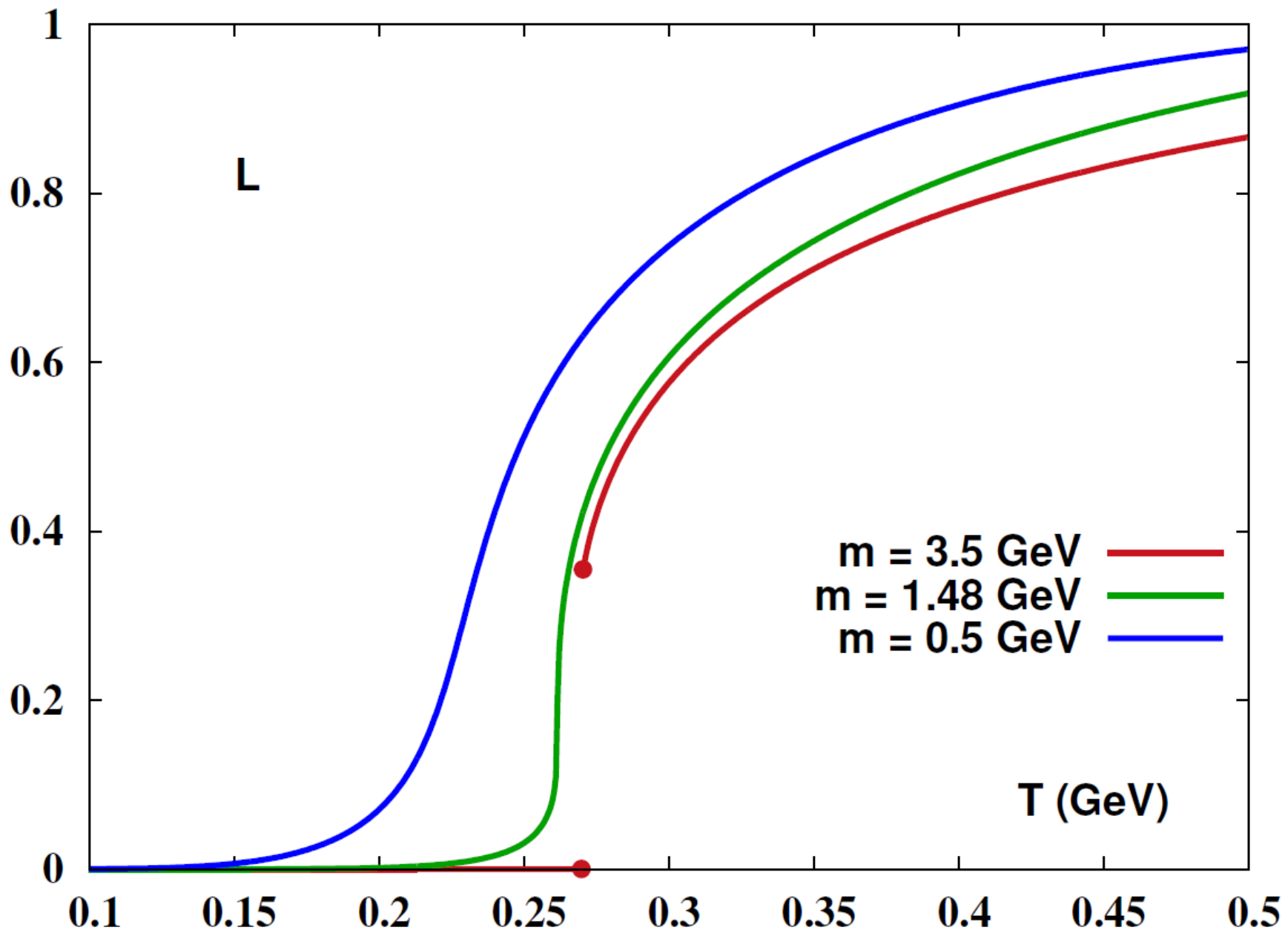
$$\bar{U}_Q[L, \bar{L}; M_Q] \approx -h_{\text{eff}}[M_Q/T] L_L + \dots$$

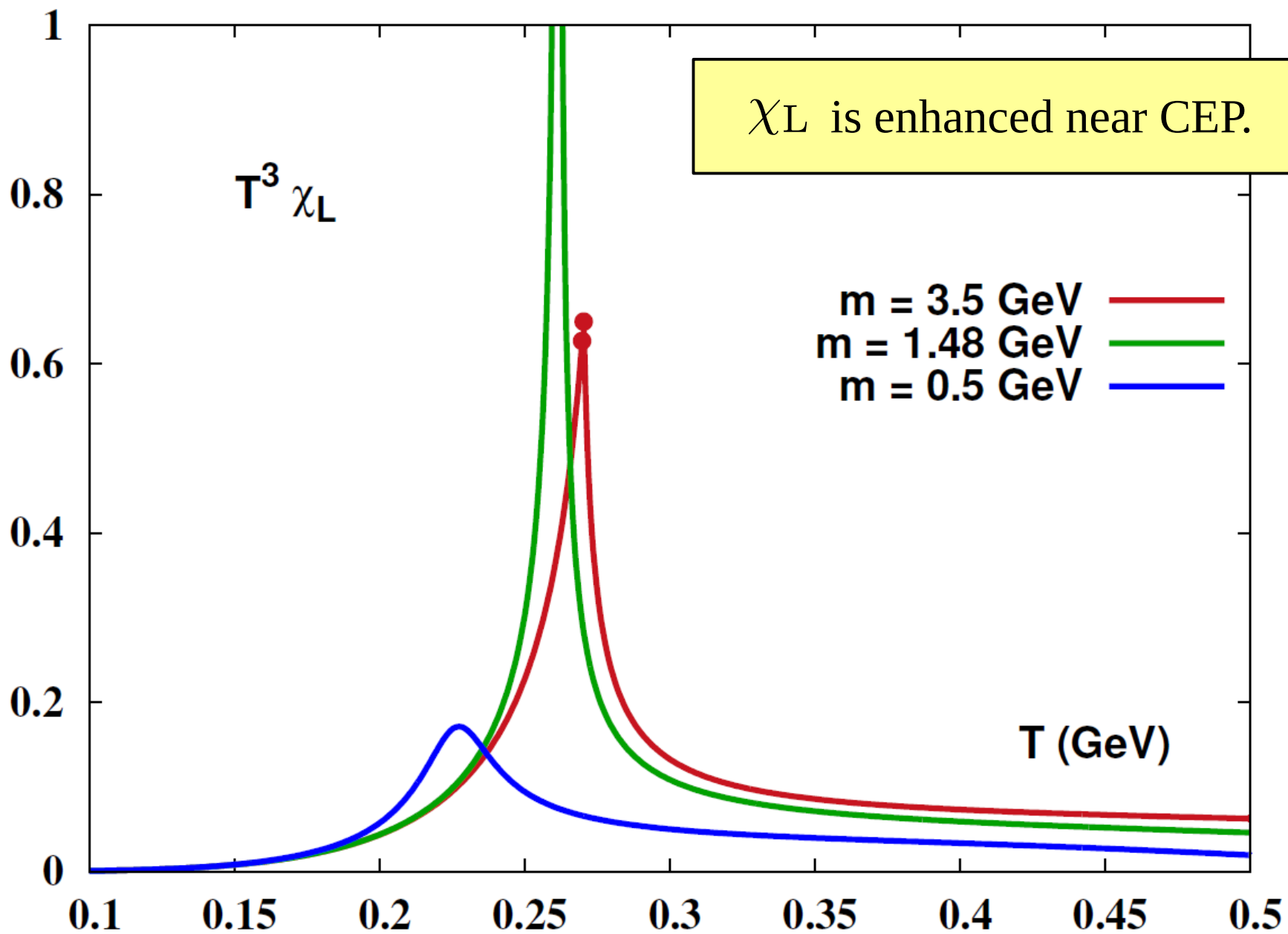
$$\bar{U}_G \longrightarrow \bar{U}_G - h_{\text{eff}} L_L$$

$$h_{\text{eff}}[M_Q/T; N_f] = \frac{6N_f}{\pi^2 T^3} \int dk k^2 e^{-\beta \sqrt{k^2 + M_Q^2}}$$

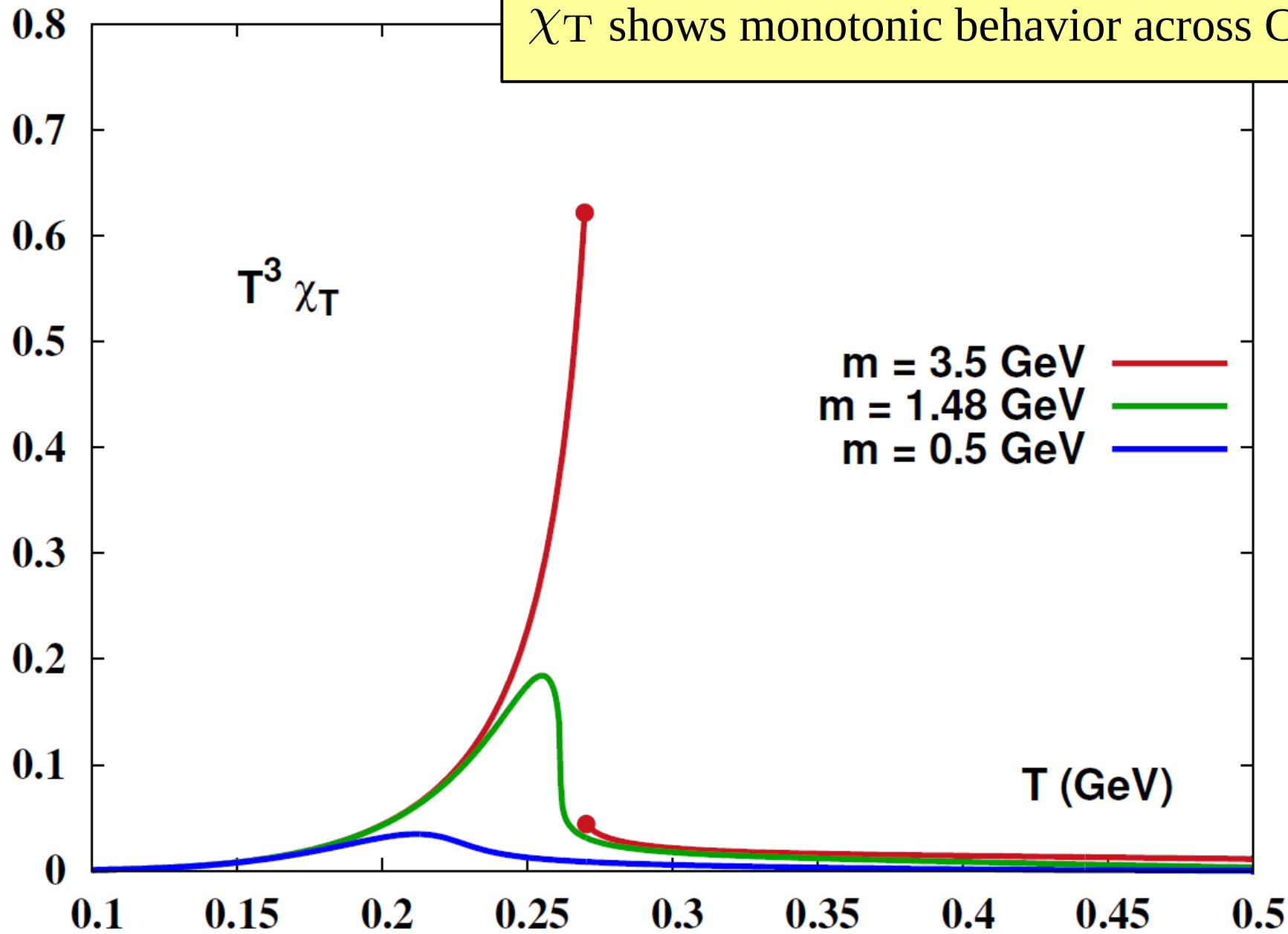
$$h_{\text{eff}} \rightarrow 0 \quad \text{as} \quad M_Q/T \rightarrow \infty$$





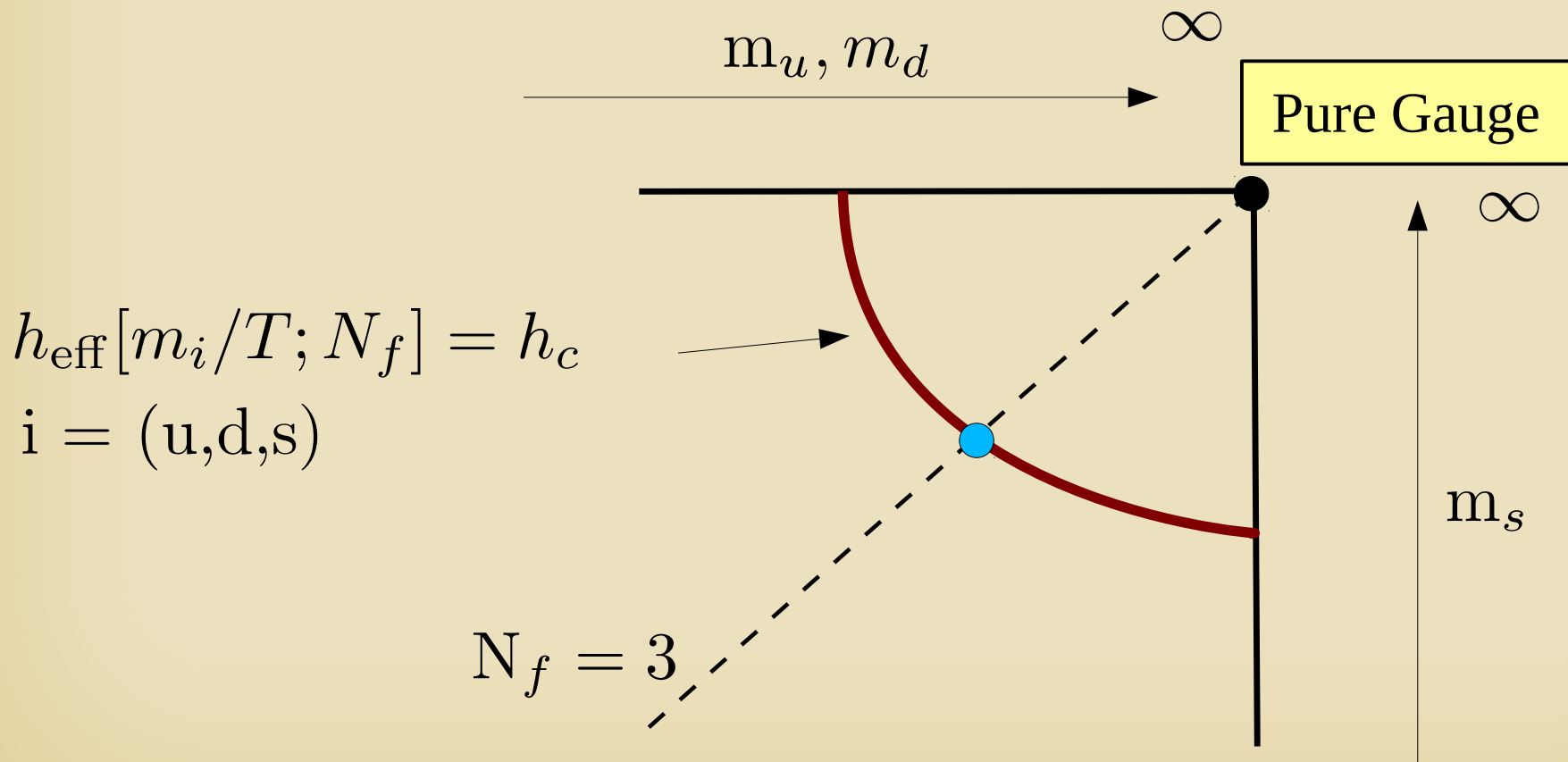


$\chi_T$  shows monotonic behavior across CEP.



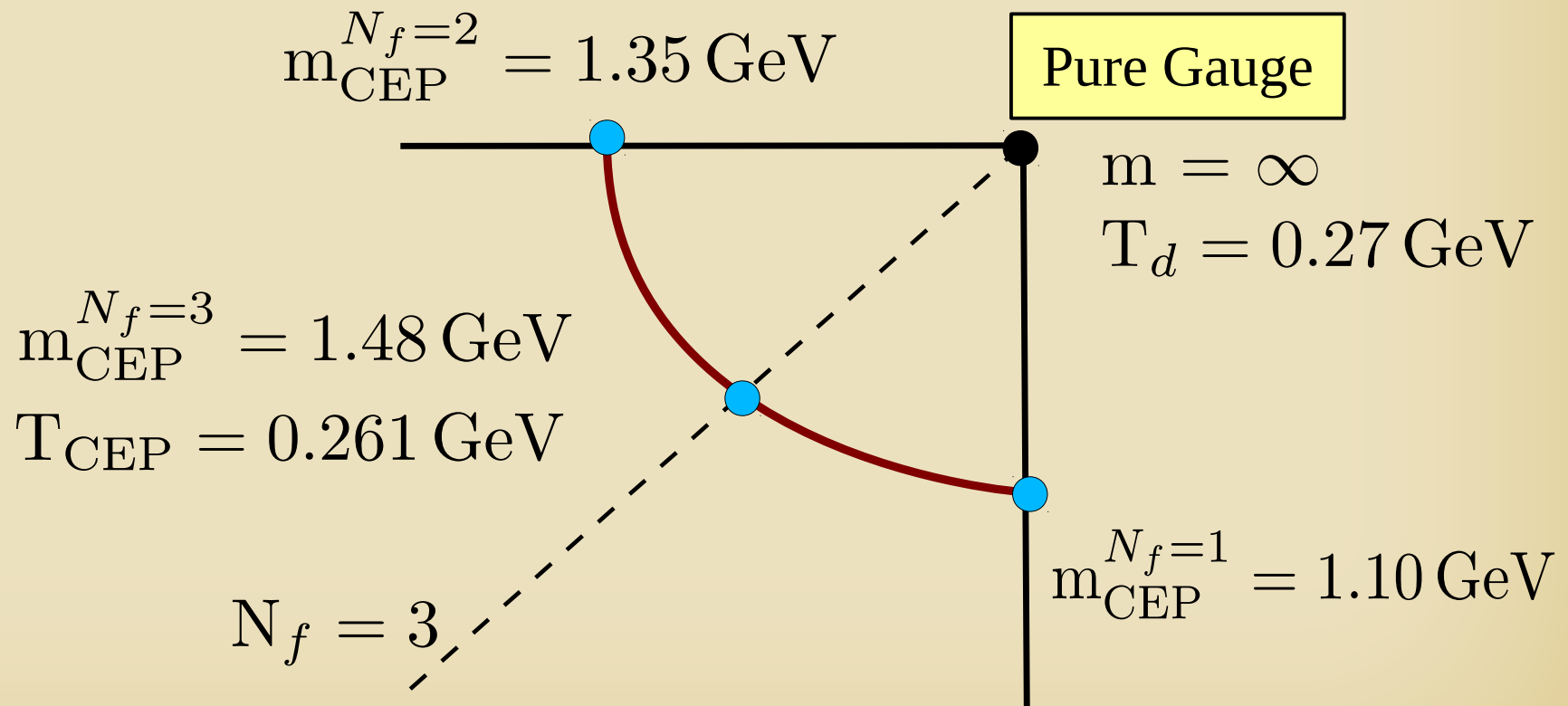
# Critical quark mass

- Phase boundary of deconfinement phase transition



# Critical quark mass

- Critical end point results from effective potential



# Critical quark mass

- $N_f$  dependence of critical quark mass

$$h_{\text{eff}}[M_Q/T; N_f] = \frac{6N_f}{\pi^2 T^3} \int dk k^2 e^{-\beta \sqrt{k^2 + M_Q^2}}$$

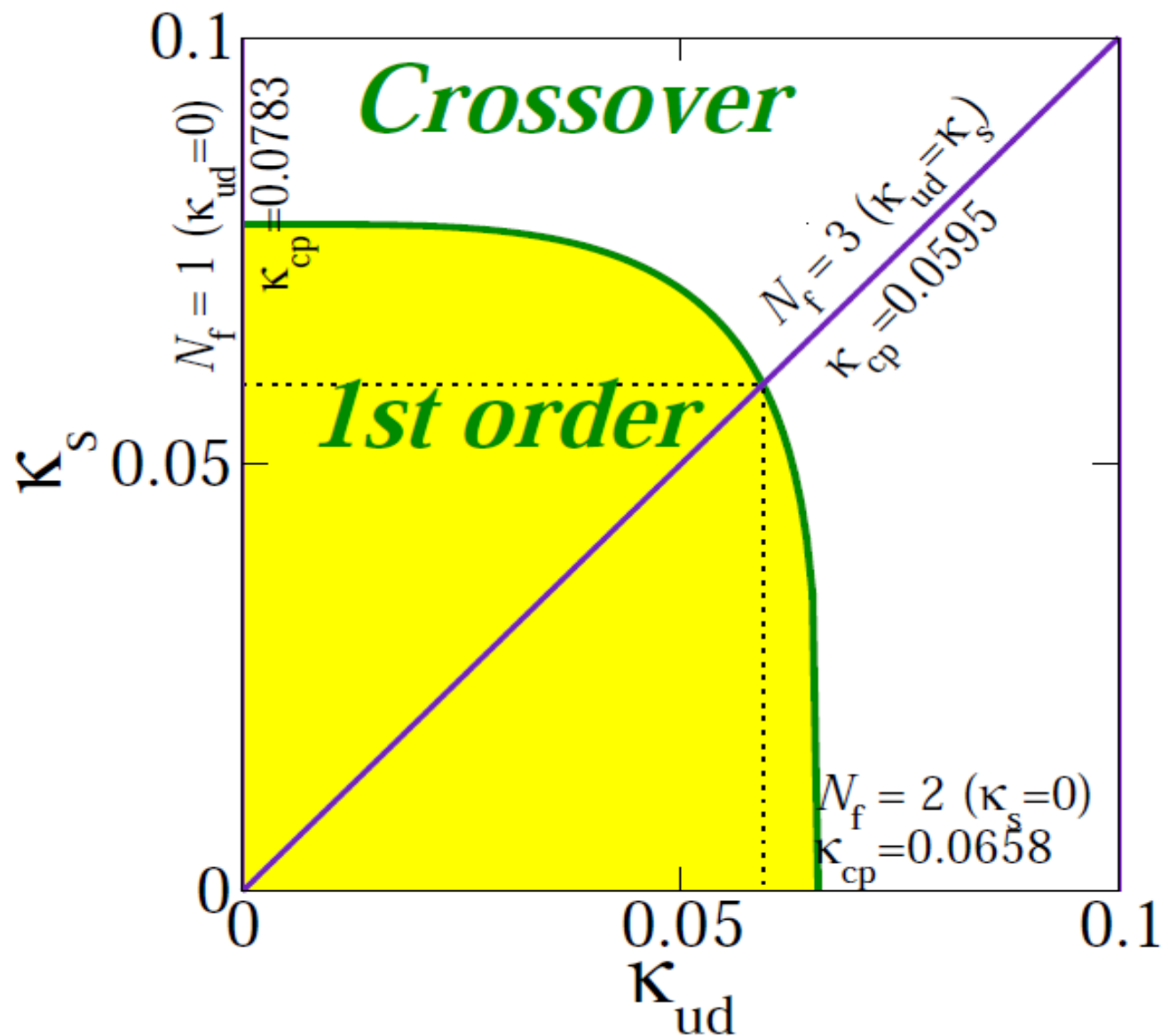
$$h_{\text{eff}}[M_Q/T; N_f] = h_c \longleftrightarrow \text{Deconfining CEP}$$

$$h_{\text{eff}} \uparrow N_f \uparrow$$

$$h_{\text{eff}} \downarrow M_Q \uparrow$$

$$m_{\text{CEP}}^{N_f=3} > m_{\text{CEP}}^{N_f=2} > m_{\text{CEP}}^{N_f=1}$$

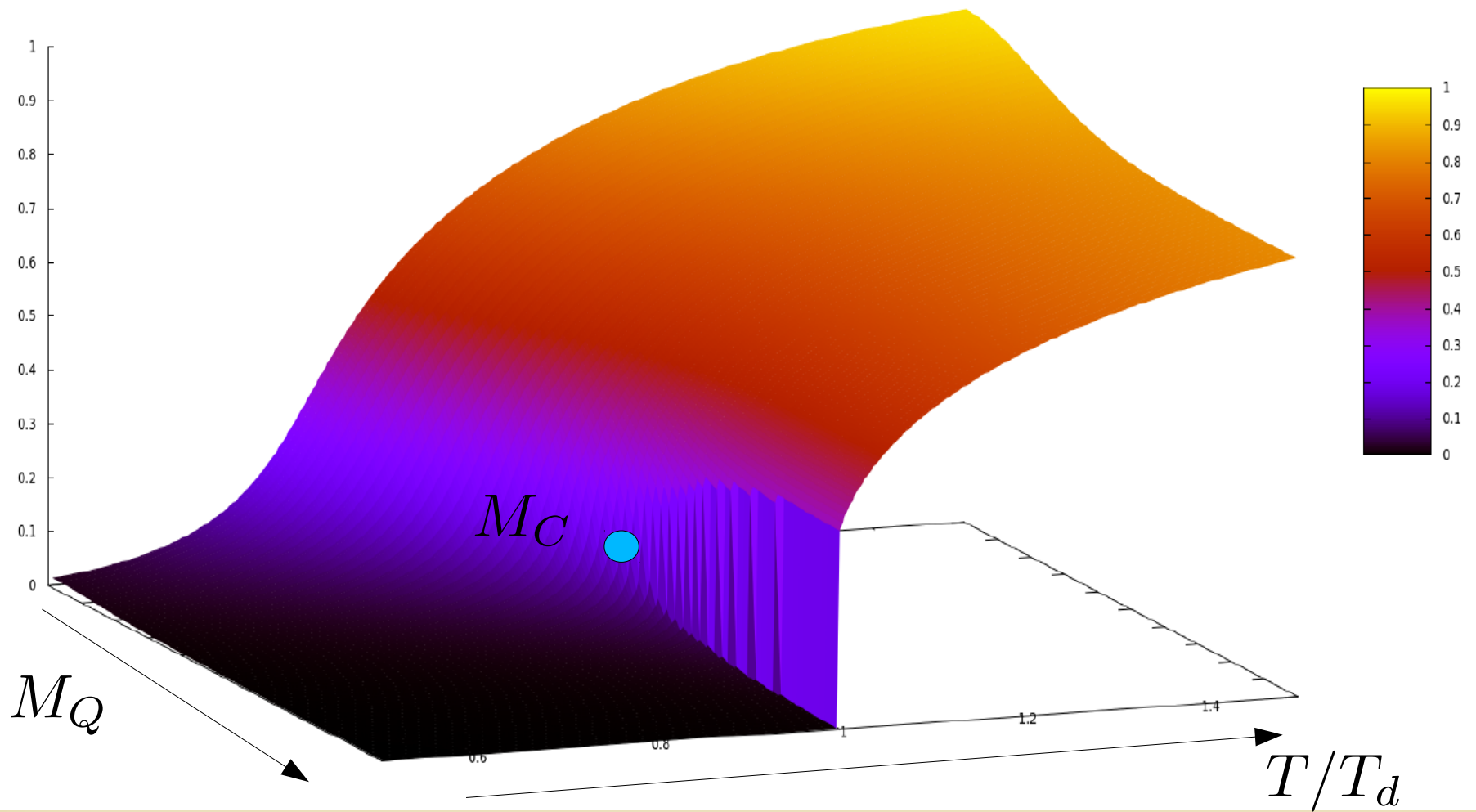
$\kappa \downarrow M_Q \uparrow$



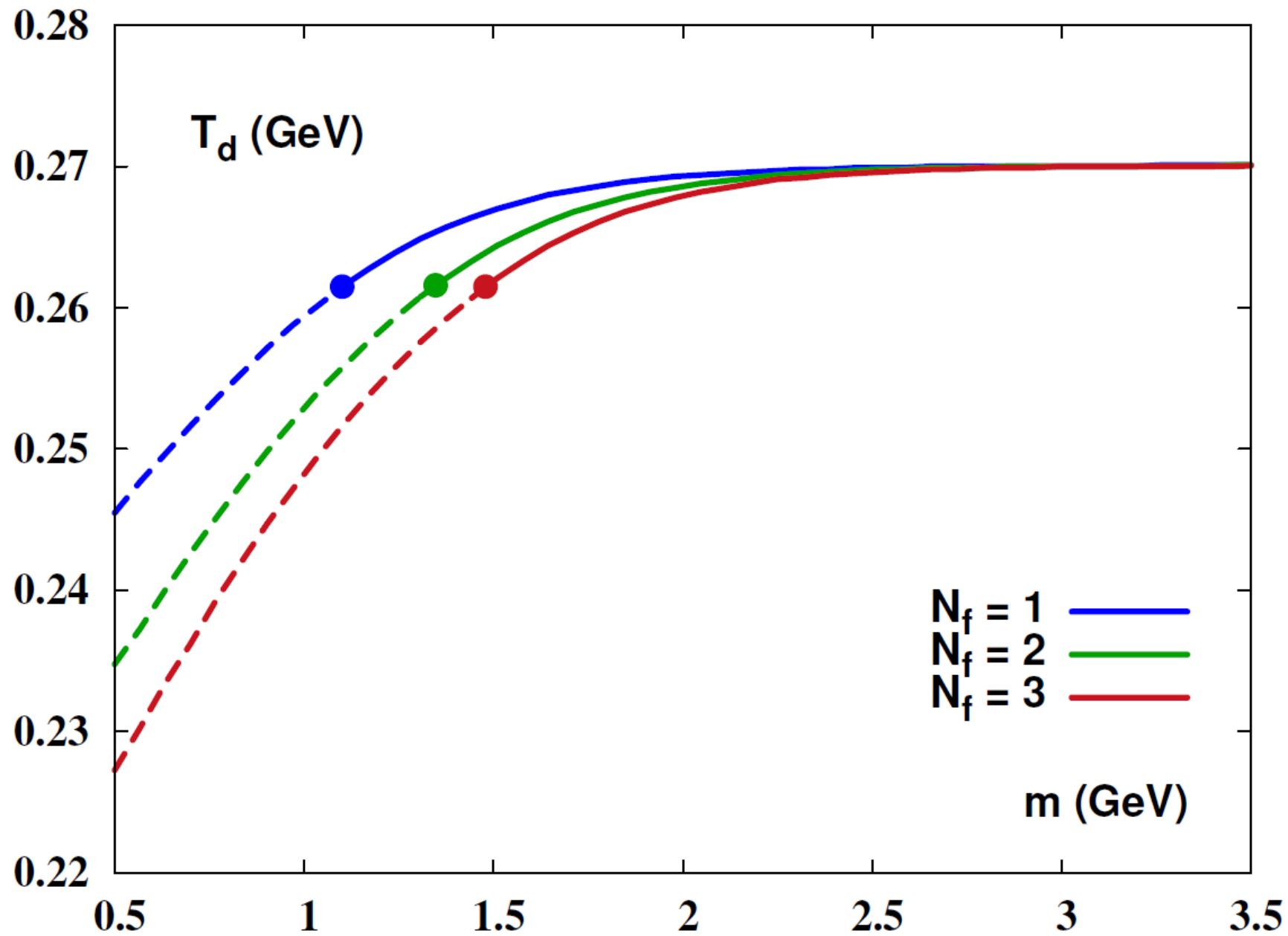
$$\kappa_c^{N_f=3} < \kappa_c^{N_f=2} < \kappa_c^{N_f=1}$$

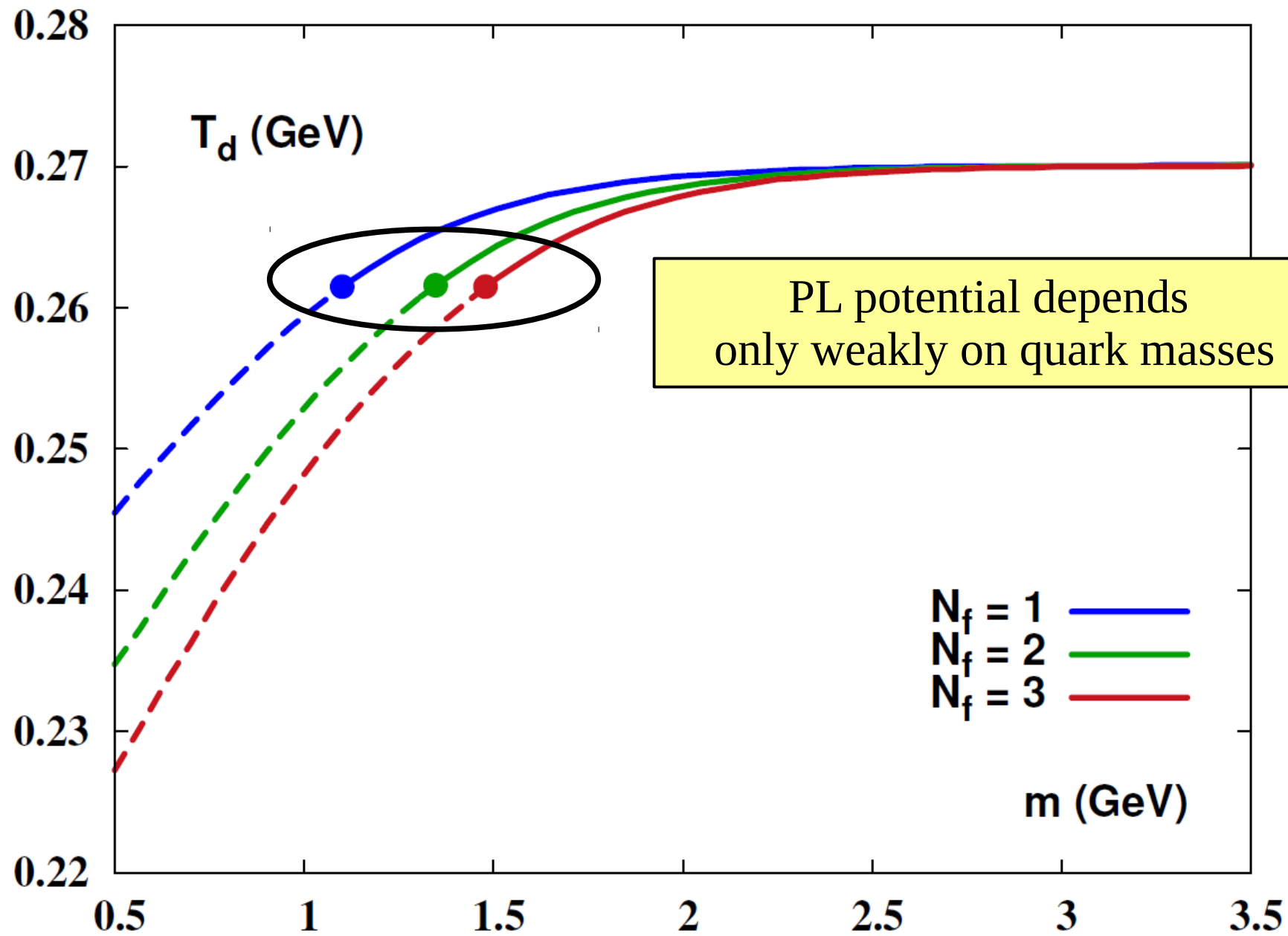
WHOT-QCD Collaboration (Saito, H. et al.)

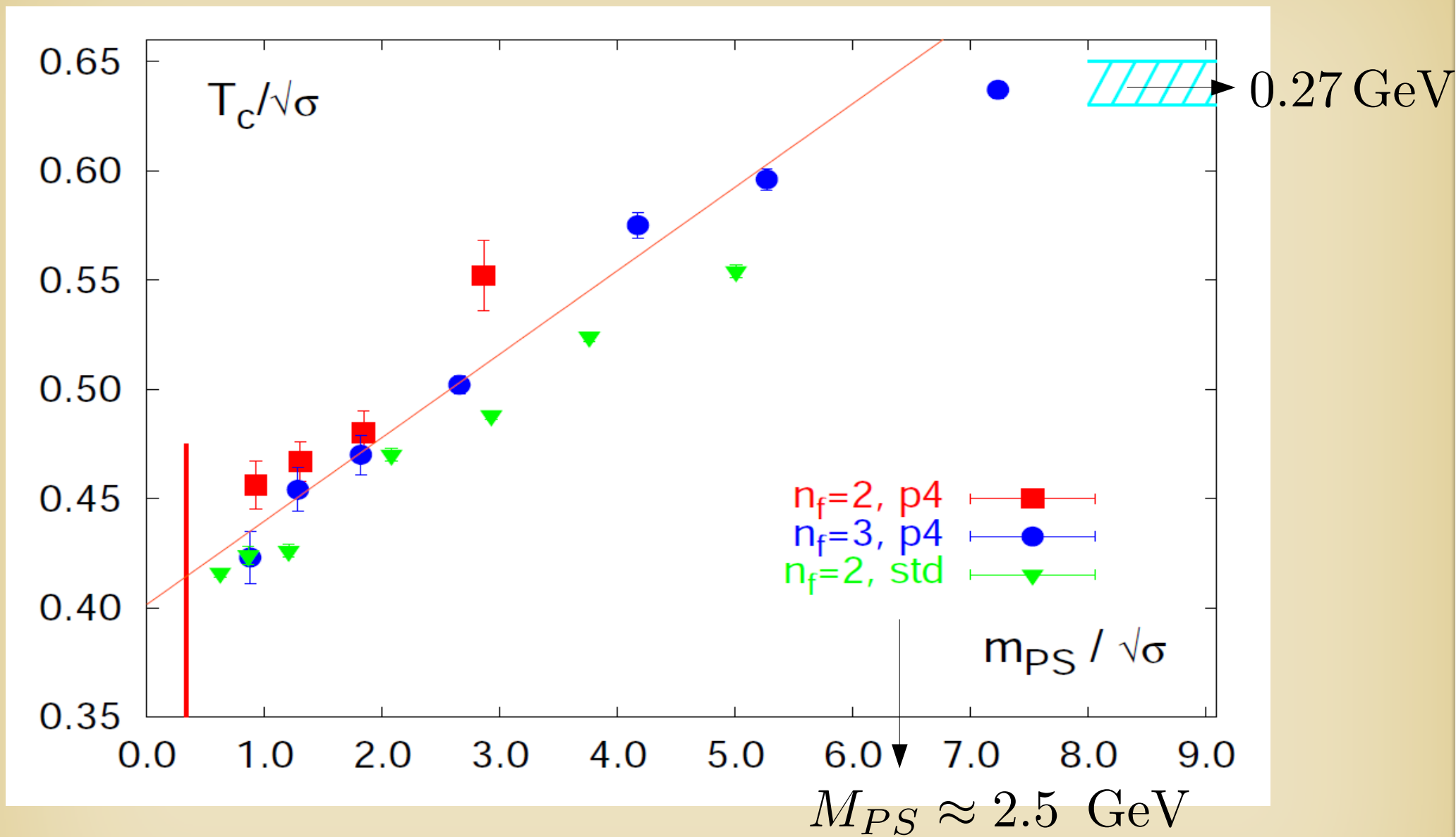
$$\langle L \rangle [T, M_Q]$$











# Heavy quark scale

- Typical heavy quarkonium mass scale:

$$m_c = 1.3 \text{ GeV}$$

$$m_b = 4.2 \text{ GeV}$$

$$m_{J/\psi} = 3.097 \text{ GeV}$$

$$m_\Upsilon = 9.460 \text{ GeV}$$

$$m_{\eta_c} = 2.98 \text{ GeV}$$

$$m_{\eta_b} = 9.391 \text{ GeV}$$

$$m_{PS}/m_V = 0.96$$

$$m_{PS}/m_V = 0.99$$

# Model dependence of CEP

- Current model:

$$m_{\text{CEP}}^{N_f=3} \approx 1.48 \text{ GeV}$$

$$T_{\text{CEP}} \approx 0.26 \text{ GeV}$$

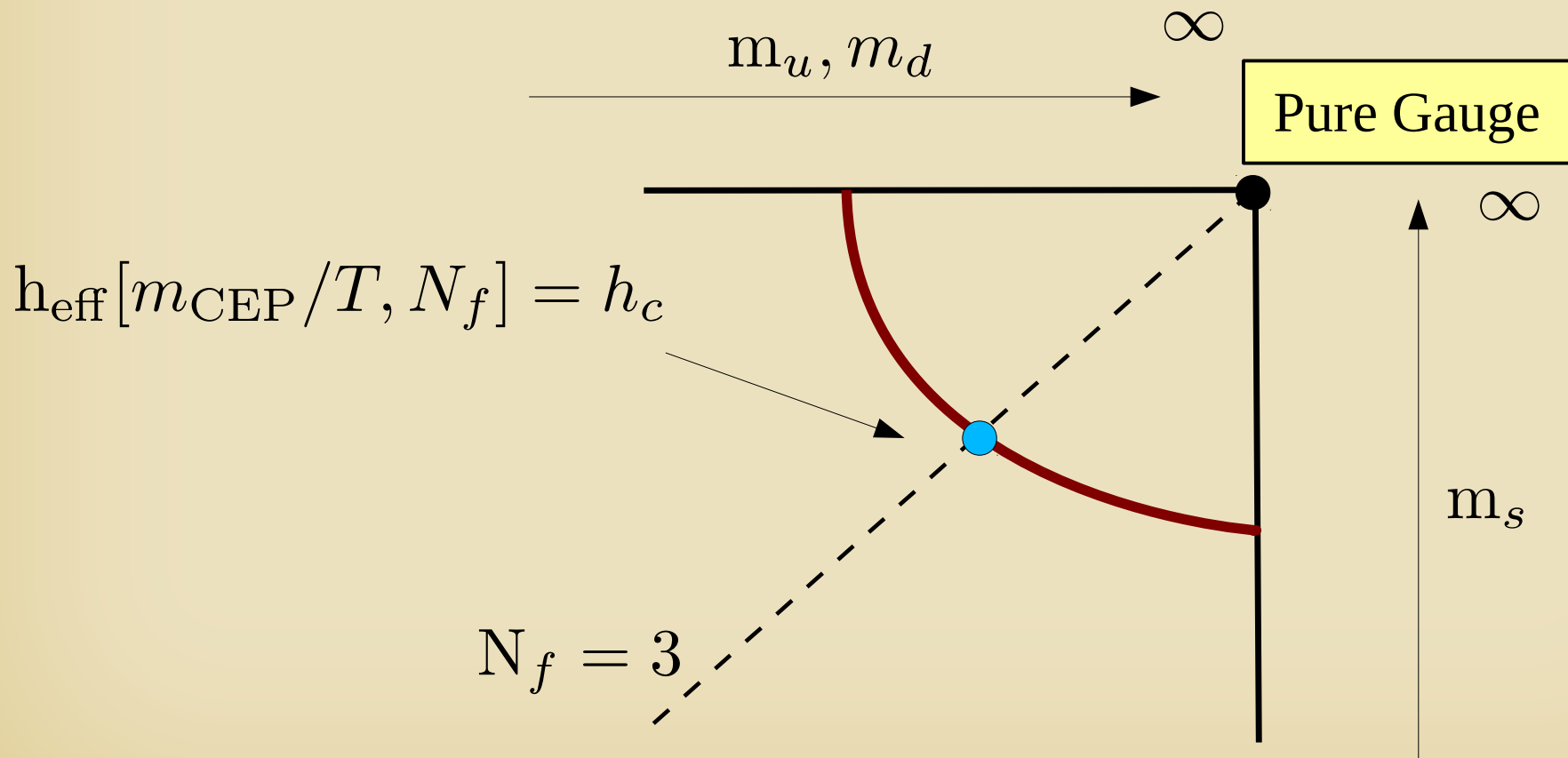
- Matrix model:

$$m_{\text{CEP}}^{N_f=3} \approx 2.5 \text{ GeV}$$

$$T_{\text{CEP}} \approx 0.27 \text{ GeV}$$

# Critical quark mass at finite density

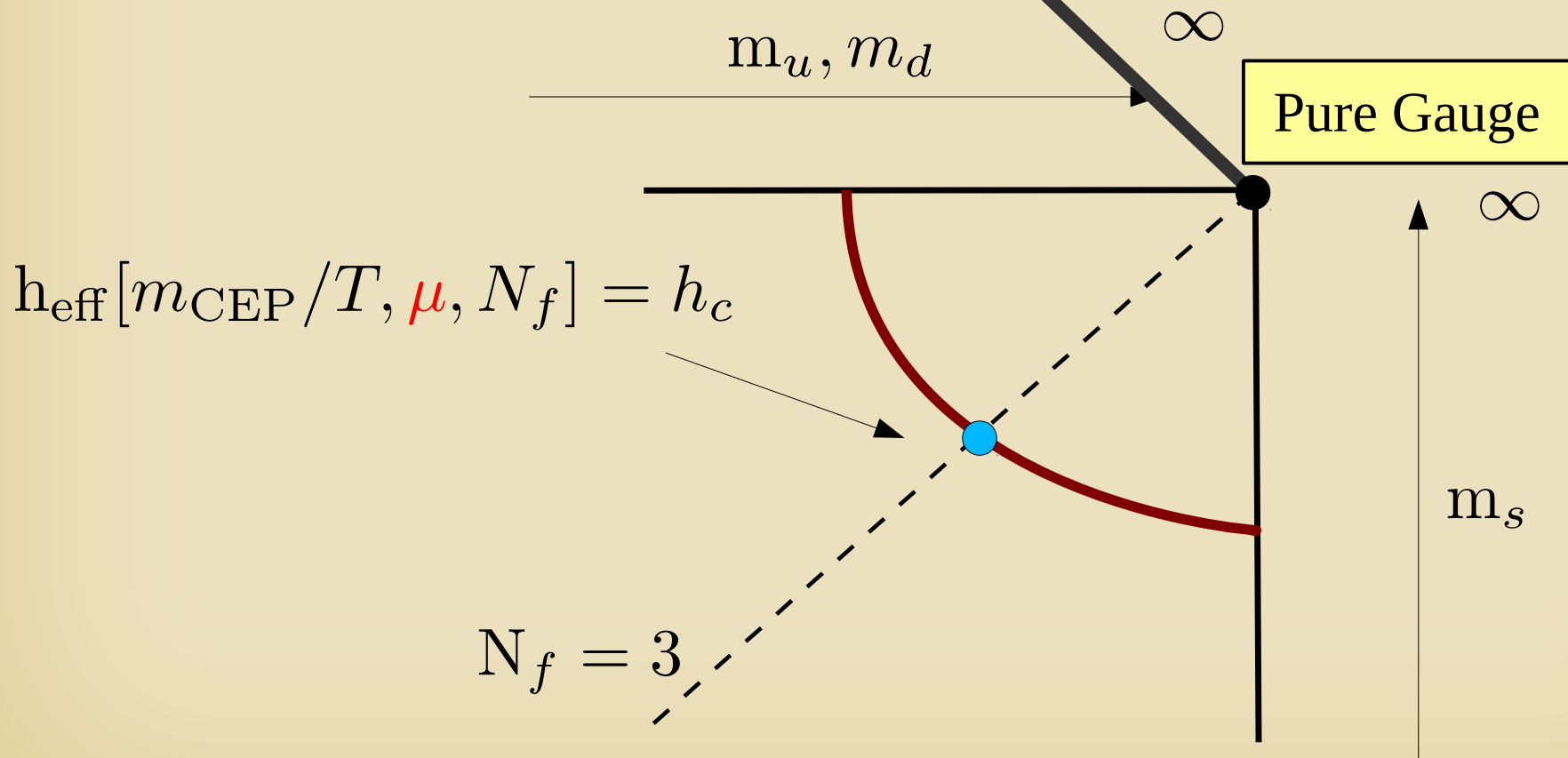
- Phase boundary of deconfinement phase transition

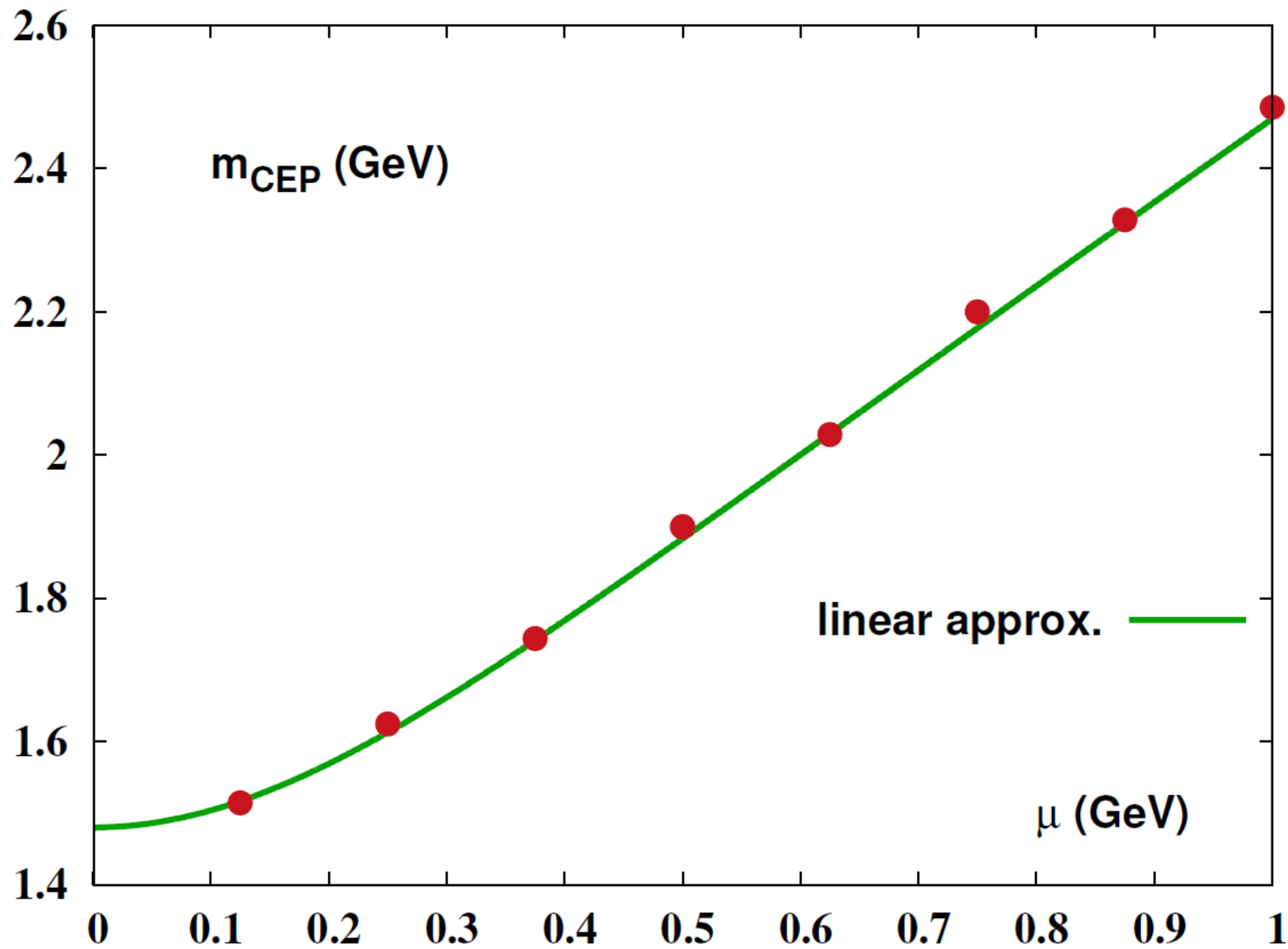


$\mu$ 

# Critical quark mass at finite density

- Phase boundary of deconfinement phase transition







# Summary of part 1

- $\chi_L$  is strongly enhanced in the critical region  
    —→ probe the location of CEP
- $\chi_T$  is insensitive to criticality  
    —→ shows only monotonic behaviors
- Deconfining CEP:  $m_{\text{CEP}}^{N_f=3} \approx 1.48 \text{ GeV}$ 
  - lattice estimate:  $\approx 1 - 1.5 \text{ GeV}$
  - $T_{\text{CEP}} \approx 0.26 \text{ GeV}$

# Summary of part 1

- $m_{\text{CEP}}$  increases with  $\mu$ 
  - ▶ first order region shrinks!
- Results of the CEP are model dependent
  - ▶ mandatory to take fluctuations of order parameter into account in constructing the effective potential

# Studying QCD medium with Polyakov loop correlators

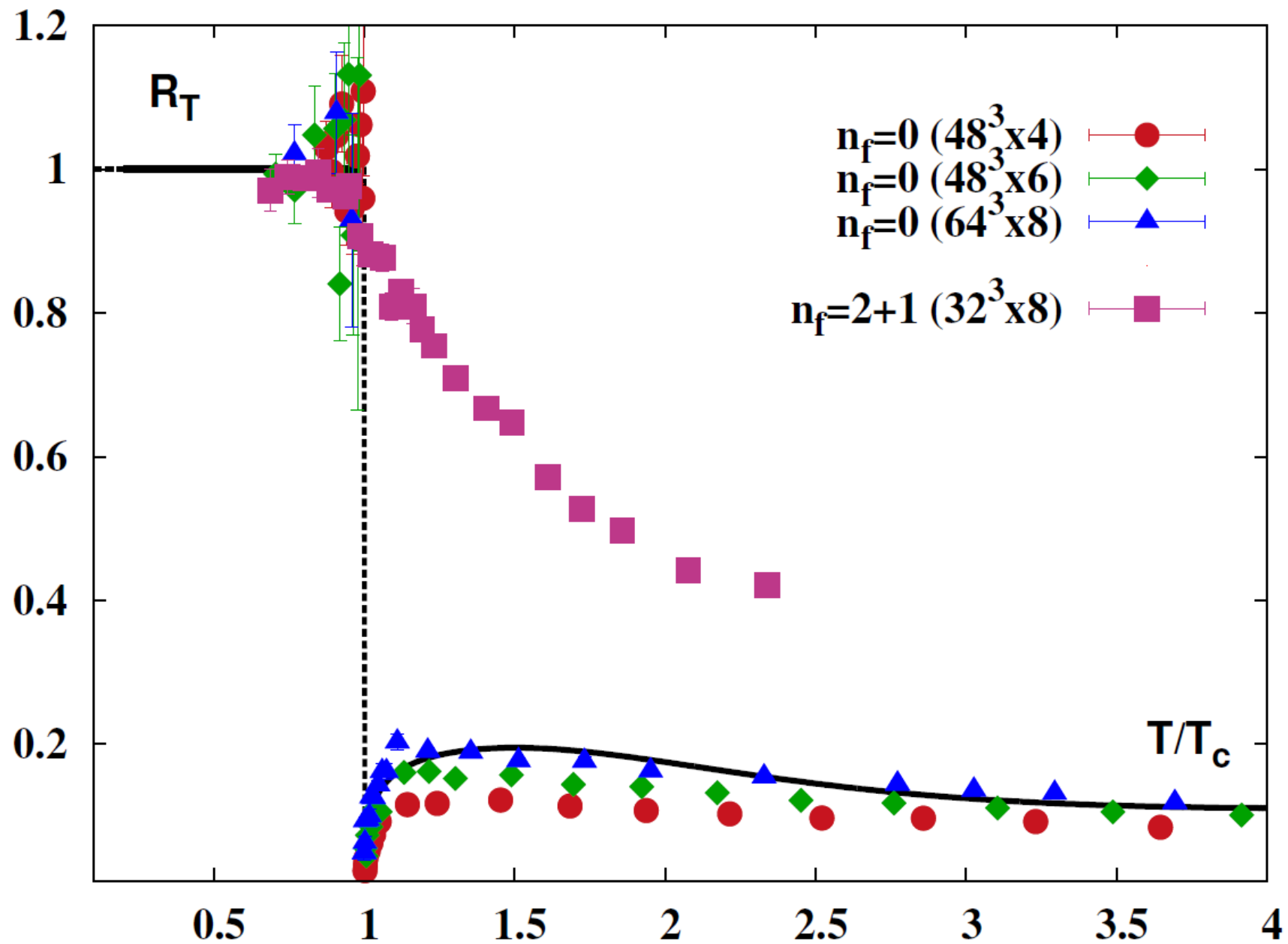
# Polyakov line correlators

- The Polyakov loop susceptibilities can be understood as **integrated correlation functions**

$$L_{\vec{x}} = \left\langle \frac{1}{N_c} \text{Tr} \mathcal{P} e^{ig \int_0^\beta d\tau A^4[\tau, \vec{x}]} \right\rangle$$

$$\chi_L = \int d^3x \langle L_L(x) L_L(0) \rangle_c$$

$$\chi_T = \int d^3x \langle L_T(x) L_T(0) \rangle_c$$



# Polyakov line correlators

- Below  $T_c$ , from  $Z(3)$  symmetry

$$\longrightarrow \chi_T / \chi_L = 1$$

$$\langle LL \rangle = 0 = \langle L_L L_L \rangle - \langle L_T L_T \rangle$$

- Above  $T_c$ ,  $Z(3)$  is spontaneously broken

$$\longrightarrow \chi_T \neq \chi_L$$

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- Above  $T_c$ ,  $Z(3)$  is spontaneously broken

$$\longrightarrow \chi_T \neq \chi_L$$

$$\chi_T \ll \chi_L$$

Magnitudes of  $\chi$ 's reflect screening properties of QCD medium!

# Screening masses of the Polyakov line correlators

- The screening masses for these gauge invariant correlators have been extracted

$$m_{L,T} = \lim_{r \rightarrow \infty} -\frac{d}{dr} \ln C_{L,T}(r)$$



# Screening masses of the Polyakov line correlators

- The screening masses for these gauge invariant correlators are extracted

$$m_{L,T} = \lim_{r \rightarrow \infty} -\frac{d}{dr} \ln C_{L,T}(r)$$

??

Perturbatively:  
starts with 2 and 3 gluons exchange  
(S. Nadkarni, Phys. Rev. D 33, 3738 (1986))

Effective field theory:  
glueball exchange

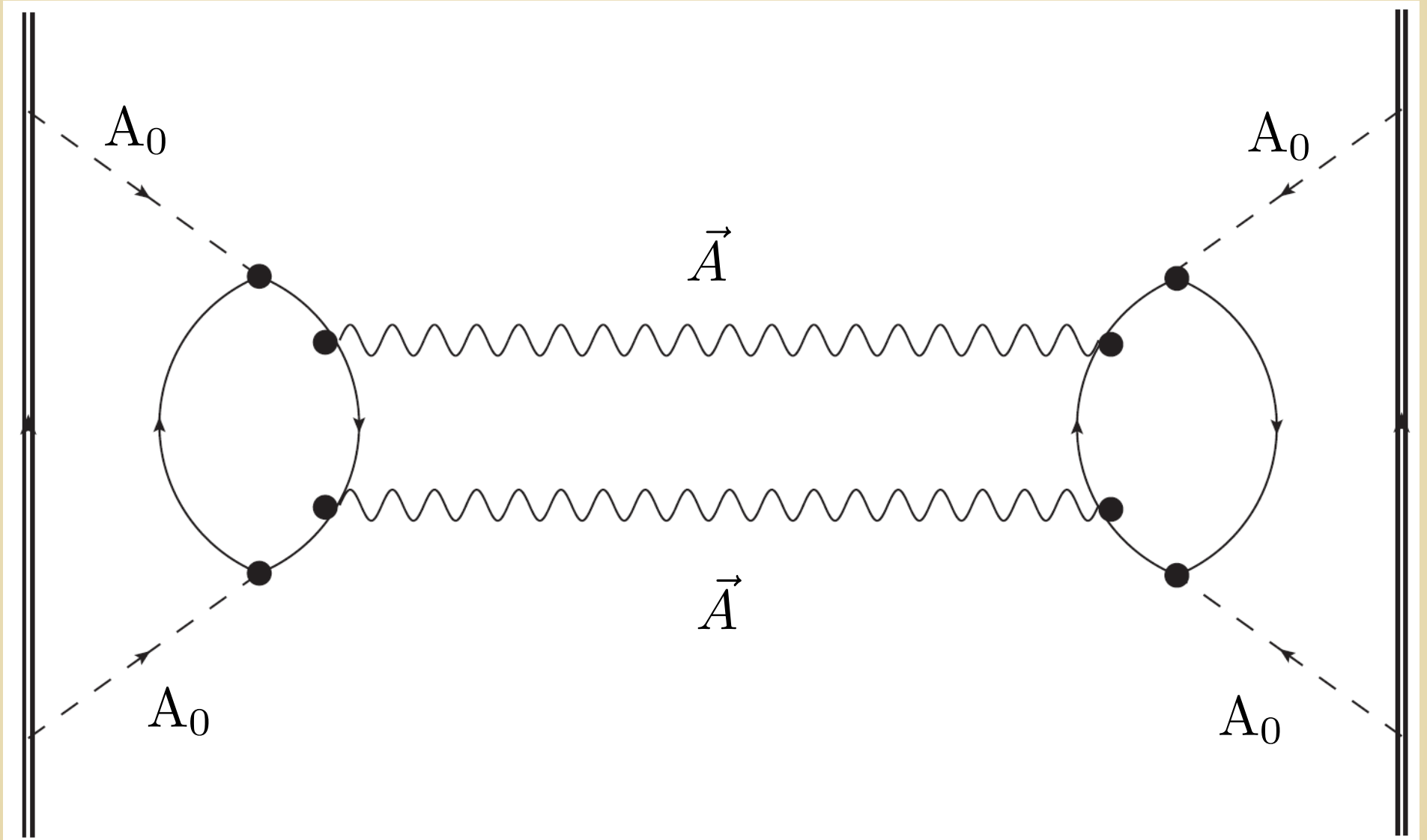
(E. Braaten and A. Nieto, Phys. Rev. Lett. 74, 3530 (1995))

$$\langle L_L(x) L_L(0) \rangle_c$$

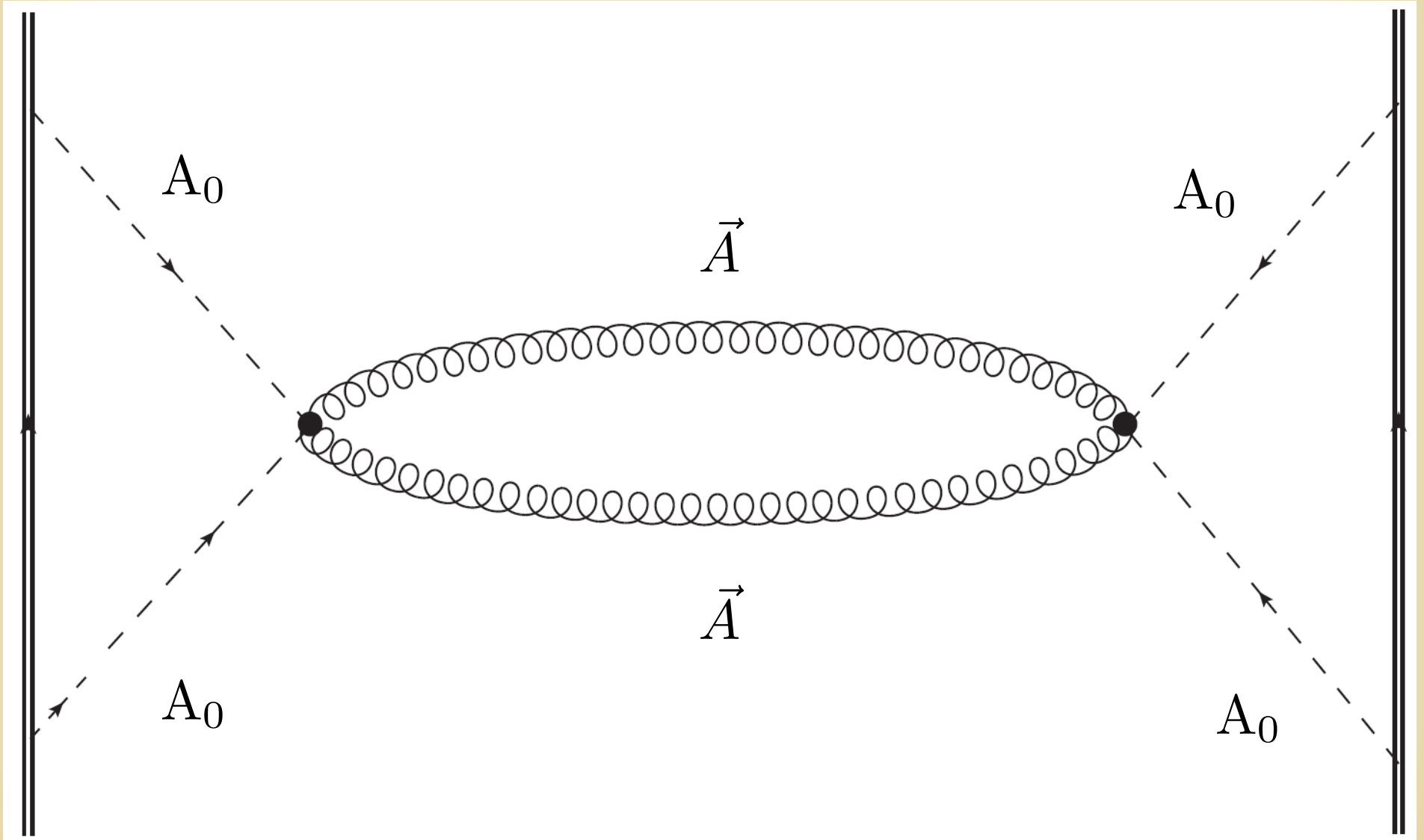
$$\langle L_T(x) L_T(0) \rangle_c$$

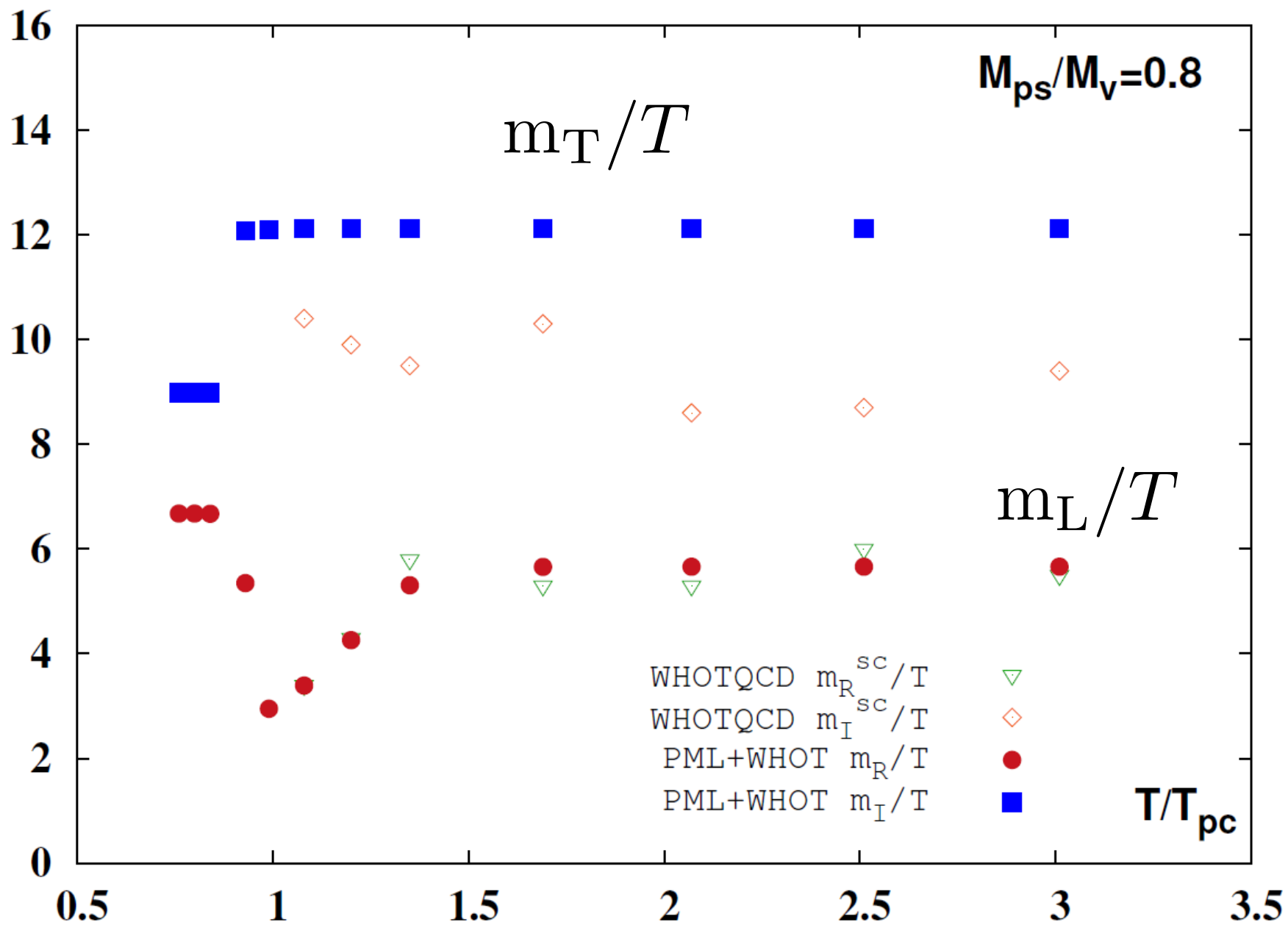
$$L_{\vec{x}} = \left\langle \frac{1}{N_c} \text{Tr} \mathcal{P} e^{ig \int_0^\beta d\tau A^4[\tau, \vec{x}]} \right\rangle$$

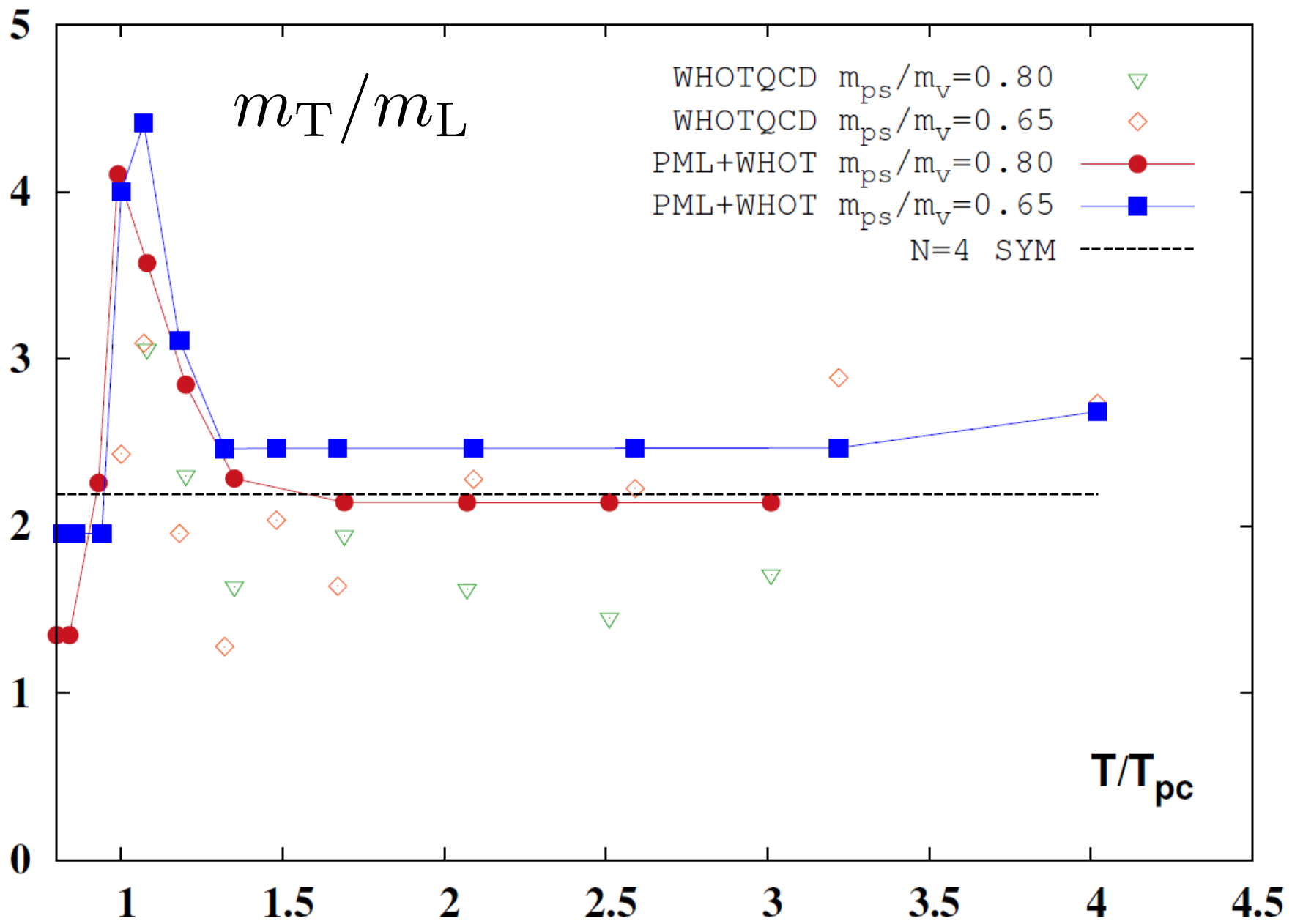
$\langle L_L(x)L_L(0) \rangle_c$  contains the exchange of magnetic photons!

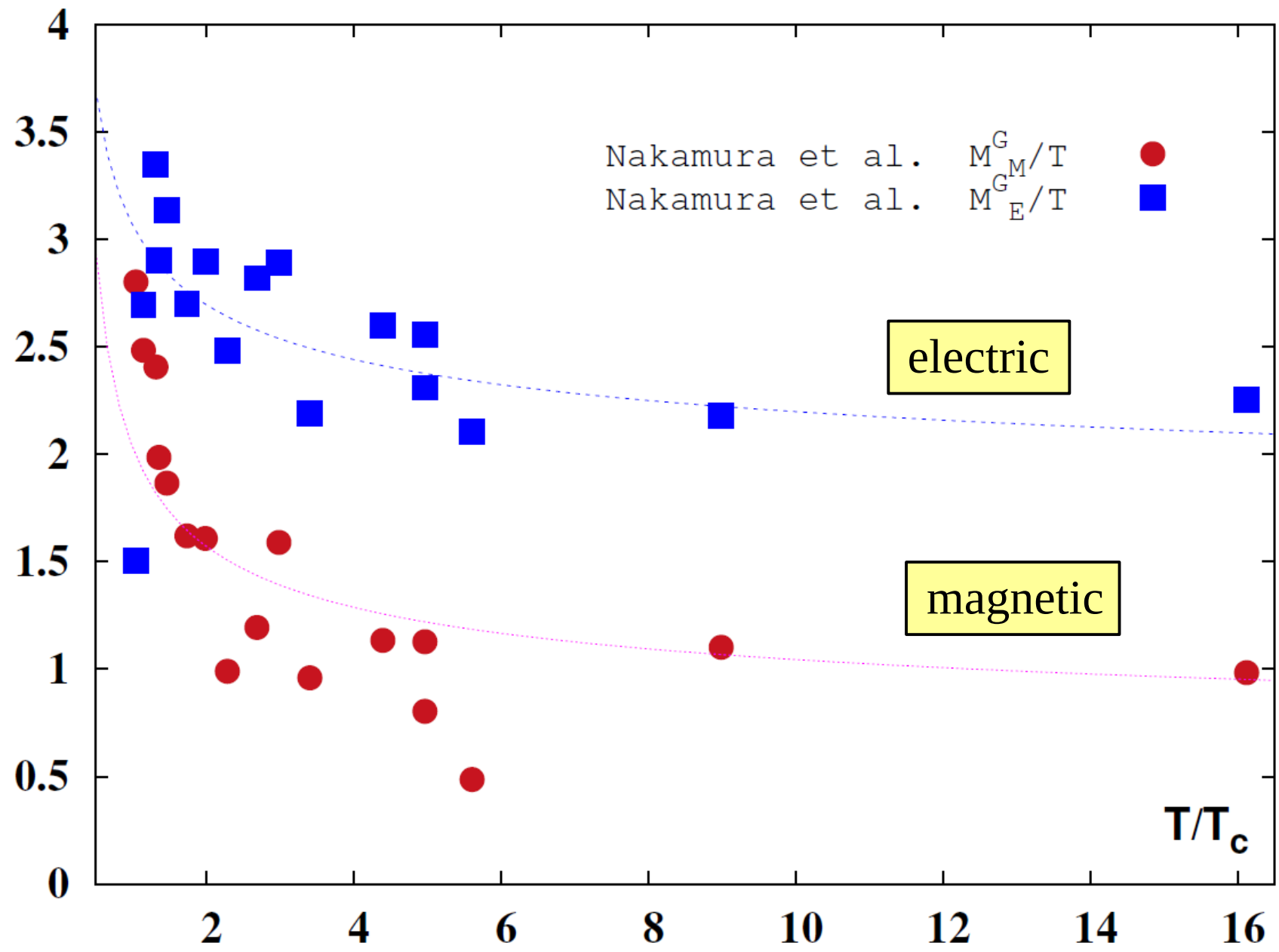


$\langle L_L(x) L_L(0) \rangle_c$  contains the exchange of magnetic gluons and glueballs!









# R-parity

$$A_0 \rightarrow -A_0$$

- Longitudinal PL: even, magnetic?
- Transverse PL: odd, electric?

$$m_{L,T} = \lim_{r \rightarrow \infty} -\frac{d}{dr} \ln C_{L,T}(r)$$

$$\chi_L = \int d^3x \langle L_L(x) L_L(0) \rangle_c$$

$$\chi_T = \int d^3x \langle L_T(x) L_T(0) \rangle_c$$

P. B. Arnold and L. G. Yaffe, Phys. Rev. D 52, 7208 (1995)

Y. Maezawa et al. [WHOT-QCD Collaboration], Phys. Rev. D 81, 091501 (2010)

# R-parity

$$A_0 \rightarrow -A_0$$

- Longitudinal PL: even, magnetic?
- Transverse PL: odd, electric?  $\longrightarrow$

electric screening >  
magnetic screening

$$m_{L,T} = \lim_{r \rightarrow \infty} -\frac{d}{dr} \ln C_{L,T}(r)$$

$$\chi_L = \int d^3x \langle L_L(x) L_L(0) \rangle_c$$

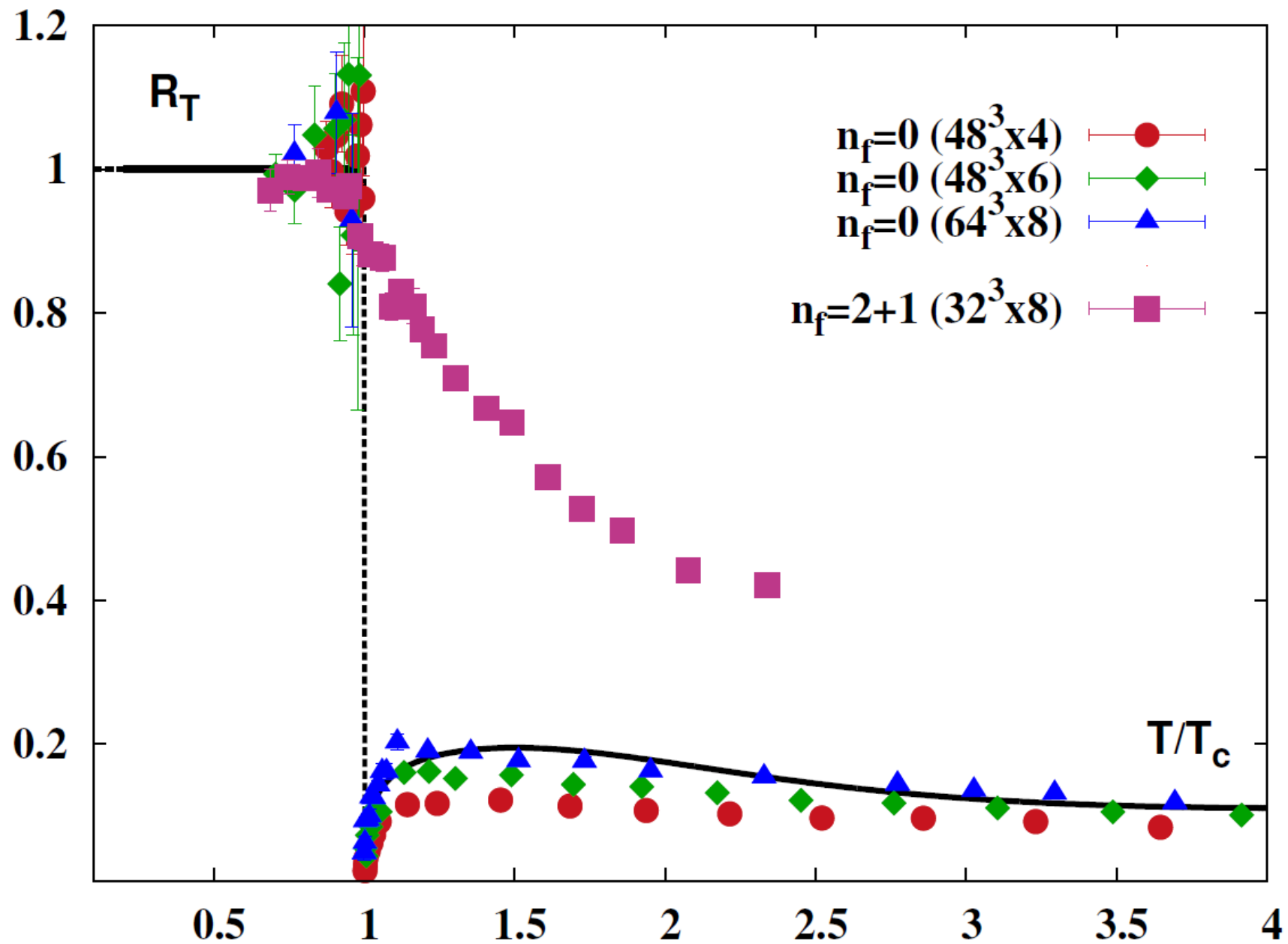
$$\chi_T = \int d^3x \langle L_T(x) L_T(0) \rangle_c$$

above  $T_c$

$$m_T > m_L$$

$$\chi_T \ll \chi_L$$





# Summary of part 2

- $\chi_{L,T}$  can be understood as integrated correlation functions

$$\chi_L = \int d^3x \langle L_L(x) L_L(0) \rangle_c$$

$$\chi_T = \int d^3x \langle L_T(x) L_T(0) \rangle_c$$

- From R-parity

$$\chi_T < \chi_L$$

$$m_T > m_L$$



electric screening > magnetic screening

# Summary of part 2

- $\chi_{L,T}$  link screening properties and deconfinement

Theoretical understanding is still incomplete, perturbative study is still absent.

Thank You!