

Heavy quark transport properties from LHC to CBM energies

Hamza Berrehrah

Collaborators : E. Bratkovskaya, W. Cassing, P.B. Gossiaux & J. Aichelin

NeD-TURIC, June 10, 2014



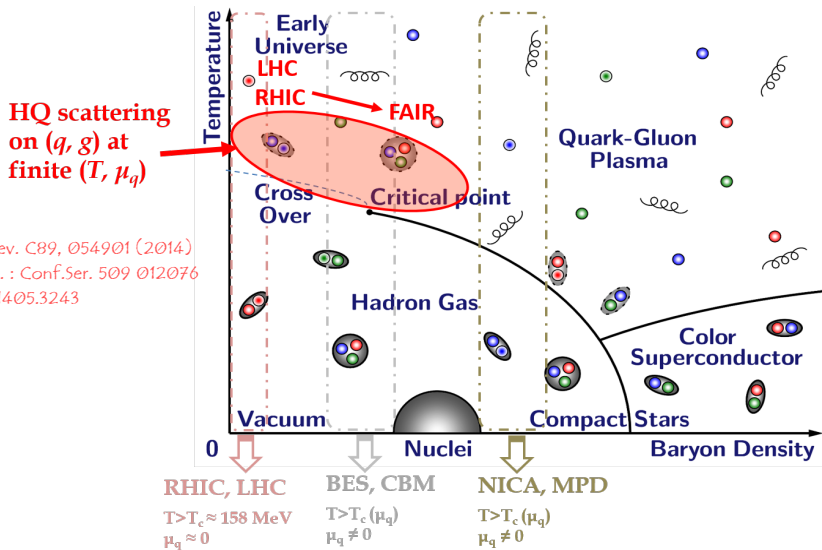
FIAS Frankfurt Institute
for Advanced Studies



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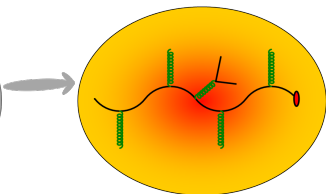
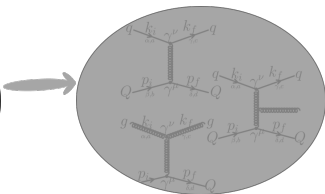
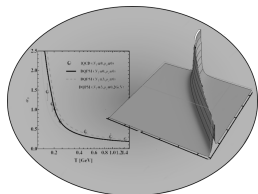
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GIESSEN



Global Project : HQ dynamics and transport properties at finite (T, μ) 

Phys.Rev. C89, 054901 (2014)
J. Phys. : Conf.Ser. 509 012076
arXiv :1405.3243

HQ scattering and quenching in a finite temperature and chemical potential QCD medium



1 DQPM at finite (T, μ)

- Fundamental ingredients : α_s, IR
- q, g, Q masses, widths, spectral functions

[Eur. Phys. J. Spec. Top. 168, 3 (2009)
PRL 94 (2005) 172301]

2 HQ scattering at finite (T, μ)

- Elastic cross section : qQ, gQ
- Inelastic cross section : qQg, gQg, \dots

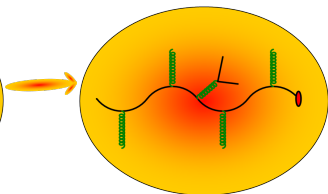
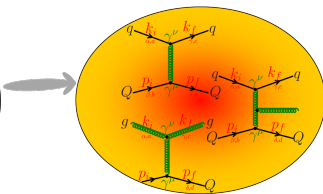
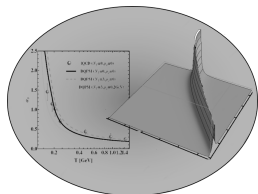
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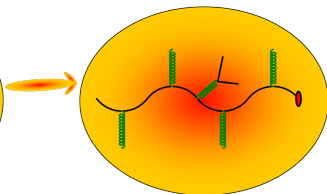
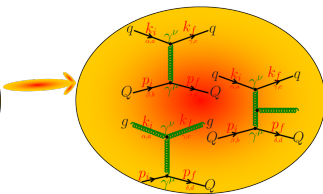
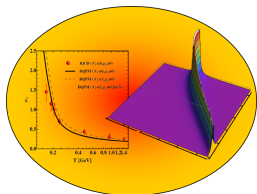
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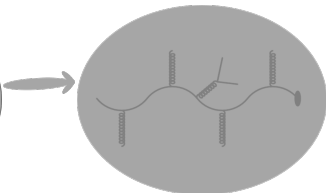
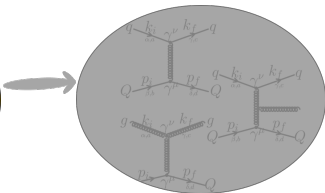
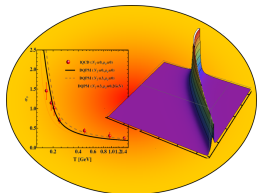
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Dynamical quasi-particle model (DQPM) at finite T

1 DQPM entropy density

$$s_i^{DQP} = - \int \frac{d\omega}{2\pi} \frac{d^3 p}{(2\pi)^3} \frac{\partial n_i}{\partial T} (\Im \ln(-\Delta^{-1}) + \Im \Pi \times \Re \Delta)$$

2 DQPM Masses and Widths

$$m_g^2 = \frac{g^2}{6} \left(N_c + \frac{1}{2} N_f \right) T^2, \quad m_q^2 = g^2 \frac{N_c^2 - 1}{8N_c} T^2$$

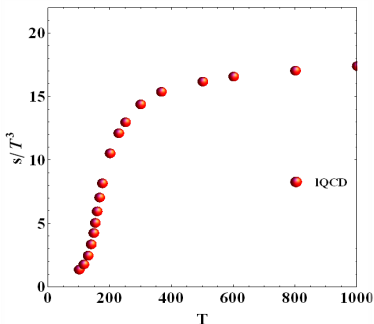
$$\gamma_g = \frac{1}{3} N_c \frac{g^2 T}{8\pi} \ln \left(\frac{2c}{g^2} + 1 \right), \quad \gamma_q = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{8\pi} \ln \left(\frac{2c}{g^2} + 1 \right)$$

3 DQPM Coupling Constant

$$g^2(T) = \frac{48\pi^2}{(11N_c - 2N_f) \ln(\lambda^2(T/T_c - T_s/T_c)^2)}$$

4 DQPM Parameters T_s, λ, c

Peshier, Cassing, PRL 94 (2005) 172301
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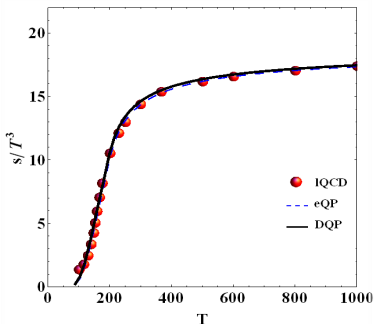
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$$T_c = 0.158 \text{ GeV}, \quad T_s = 0.56 T_c$$

$$\lambda = 2.42, \quad c = 14.4$$

Dynamical quasi-particle model (DQPM) at finite T

1 DQPM α_s , m and γ

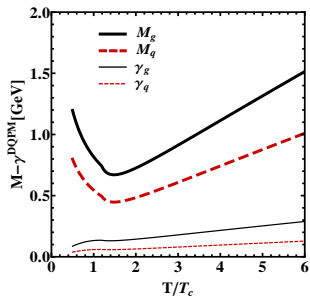
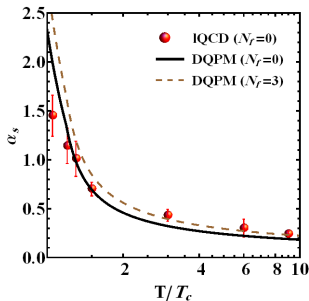
DQPM gives a good description of IQCD results

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Peshier, PRD 70 (2004) 034016

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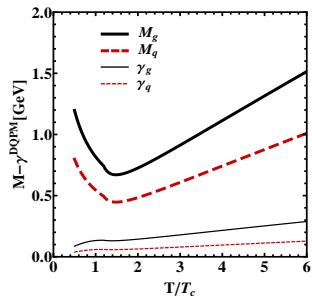
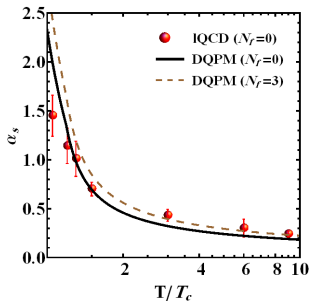
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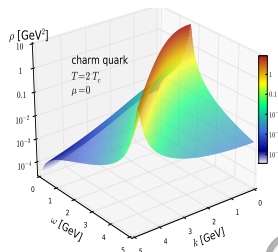
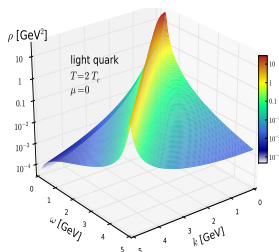
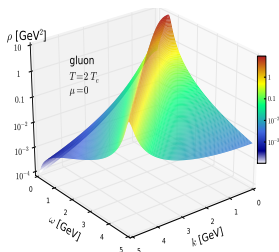
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2 DQPM $\rho(\omega, p, T)$



Dynamical quasi-particle model (DQPM) at finite (T, μ)

1 Scaling hypothesis

$$M_g^2(T) = \frac{g^2(T/T_c)}{6} \left((N_c + \frac{1}{2} N_f) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

$$M_q^2(T) = \frac{N_c^2 - 1}{8N_c} g^2(T/T_c) \left(T^2 + \frac{\mu_q^2}{\pi^2} \right)$$

$$\Downarrow$$

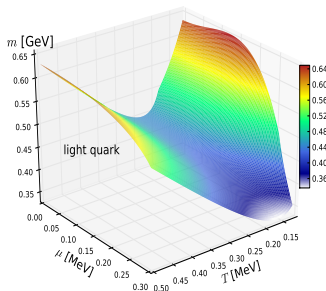
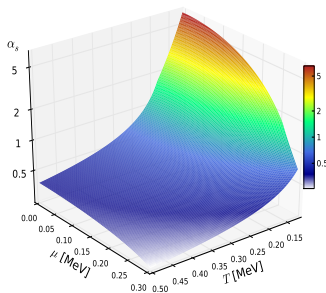
$$T^*2 = T^2 + \frac{\mu^2}{\pi^2}$$

$$g(T/T_c(\mu=0)) \rightarrow g(T^*/T_c(\mu))$$

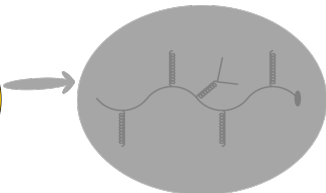
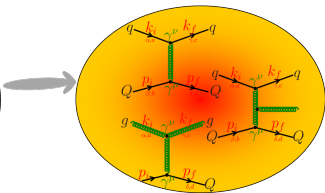
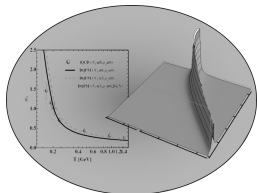
$$T_c(\mu) = T_c(\mu=0) \times \sqrt{1 - 8.79\mu^2}$$

2 α_s , masses at finite (T, μ)

- $\mu_q \nearrow \rightarrow$ decrease of α_s , $m_{q,g,Q}$
- $\mu_q \nearrow \rightarrow$ shift of the BW spectral function to small m , but same amplitude



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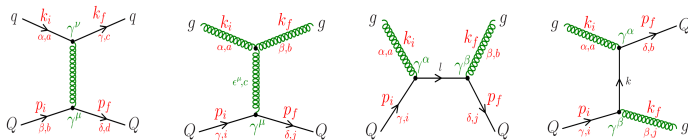
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[arXiv :1405.3243]

HQ elastic scattering at finite (T, μ_q) :

On- vs Off-shell non-pQCD based approaches



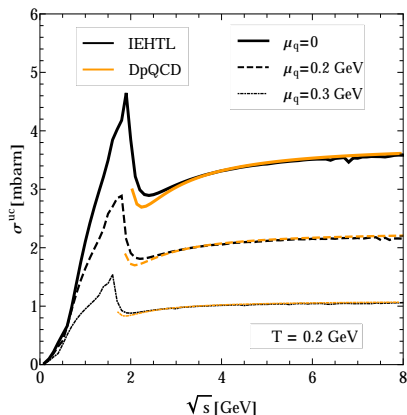
• DpQCD (Dressed pQCD) : On-shell non-pQCD

- $\alpha_s^{DQPM}(T, IR, m)$: from DQPM (DQPM pole mass for g, q, Q)
- $G^{\mu\nu}(q, m_g) = -i \frac{g_{\mu\nu} - q_\mu q_\nu / m_g^2}{q_0^2 - \mathbf{q}^2 - m_g^2}$

• IEHTL (Infrared Enhanced HTL) : Off-shell non-pQCD

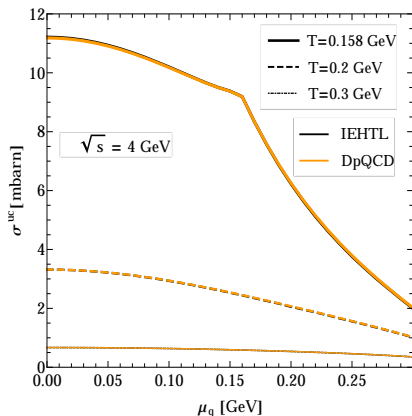
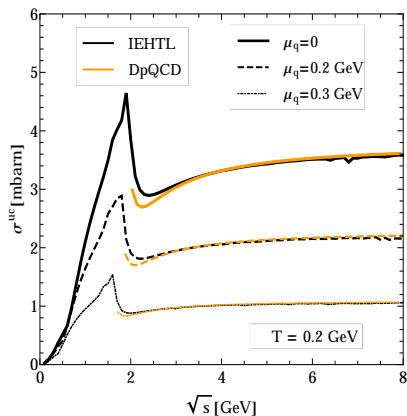
- $\alpha^{DQPM}(T, IR, m, \rho^{BW})$ from DQPM (finite mass and width)
- Off-shell kinematical limits
- $G^{\mu\nu}(q, m_g) = -i \frac{g_{\mu\nu} - q_\mu q_\nu / m_g^2}{q_0^2 - \mathbf{q}^2 - m_g^2 + i2\gamma_g q_0}$
- $\sigma^{IEHTL}(s, T) = \int \Pi dm^{(l)} \sigma^{q,g-Q}(s, m^{(1)}, m^{(2)}, m^{(3)}, m^{(4)}) \rho_{(1)}(m^{(1)}) \rho_{(2)}(m^{(2)}) \rho_{(3)}(m^{(3)}) \rho_{(4)}(m^{(4)})$

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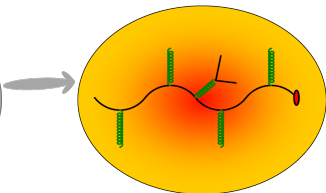
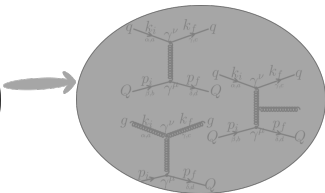
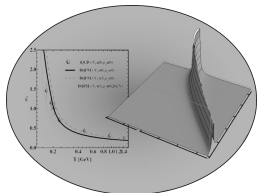
- Effect of $\rho^{BW}(m)$ is negligible (small parton width), **except reducing the kinematic threshold**

HQ elastic scattering at finite (T, μ_q)



- Effect of $\rho^{BW}(m)$ is negligible (small parton width), **except reducing the kinematic threshold**
- $(T, \mu_q) \nearrow \rightarrow m_g(T, \mu_q) \searrow$, but $\alpha_s \searrow$: decrease of σ^{qQ} , with large effect for (small T , large μ_q)
- Large enhancement of σ^{qQ} for T close to $T_c(\mu_q) \rightarrow$ infrared enhanced of $\alpha_s(T)$

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HQ Transport properties at finite (T, μ_q)

$$\frac{d \langle \mathcal{X} \rangle}{dt} = \frac{1}{(2\pi)^5 2E_p} \int \frac{d^3 q}{2E_q} f(\vec{q}) \int \frac{d^3 q'}{2E_{q'}} \int \frac{d^3 p'}{2E_{p'}} \delta^{(4)}(P_{in} - P_{fin}) \mathcal{X} \sum |\mathcal{M}_{2,2}|$$

- $\mathcal{X} = 1 \mapsto$ Interaction rate : $\mathcal{R}(p_Q, T, \mu_q) = \frac{dN_{coll}}{dt}$
- $\mathcal{X} = (E - E') \mapsto$ Energy Loss : $\frac{dE}{dt}(p_Q, T, \mu_q)$
- $\mathcal{X} = (\vec{p} - \vec{p}') \mapsto$ Drag coefficient : $\mathcal{A}(p_Q, T, \mu_q)$
- $\mathcal{X} = (p^i - p'^i)(p^j - p'^j) \mapsto$ Diffusion coefficient : $B^{ij}(p_Q, T)$

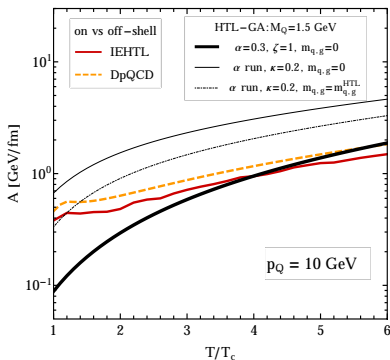
1 On-Shell case

$$Tr_{(i)}^{on} = \int \frac{d^3 p_i}{(2\pi)^3 2E_i}, \quad \sum |\mathcal{M}_{2,2}| \equiv \sum |\mathcal{M}_{2,2}^{HTL-GA}|, \quad \sum |\mathcal{M}_{2,2}^{DpQCD}|$$

2 Off-Shell case

$$Tr_{(i)}^{on} \rightarrow Tr_{(i)}^{off} = \int \frac{d^4 p_i}{(2\pi)^4} \rho_i(p_i) \Theta(\omega_i), \quad \frac{1}{2E_p} \rightarrow \int \frac{d\omega}{2\pi} \rho_p(\omega) \theta(\omega), \quad \sum |\mathcal{M}_{2,2}| \equiv \sum |\mathcal{M}_{2,2}^{IEHTL}|$$

HQ energy and longitudinal momentum losses at finite T



Perturbative approaches

HTL-GA

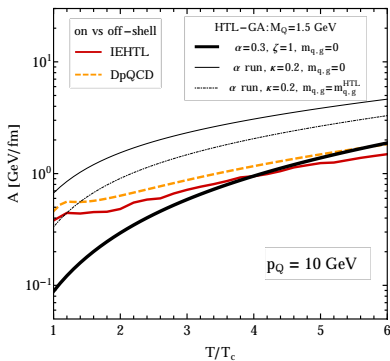
- $\alpha_s(Q^2)$, massless q, g /massive $m_{q,g} = m_{q,g}^{\text{HTL}}$
- $G^{\mu\nu}(q, m_g) = -i \frac{g_{\mu\nu}}{q^2 - \kappa \tilde{m}_D^2}$, $\kappa \approx 0.2$

Naive-pQCD

- $\alpha_s = 0.3$, $G^{\mu\nu}(q, m_g) = -i \frac{g_{\mu\nu}}{q^2 - m_D^2}$, $m_D = gT$

Gossiaux et al, Prog.Theor.Phys.Suppl. 193 (2012) 110-116
 Phys.Rev. C78 (2008) 014904, C79 (2009) 044906,

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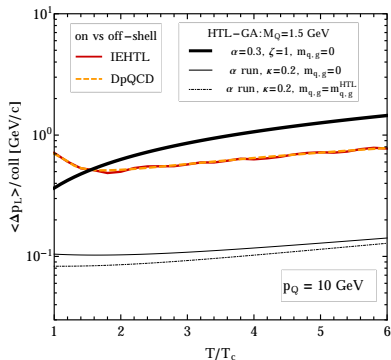
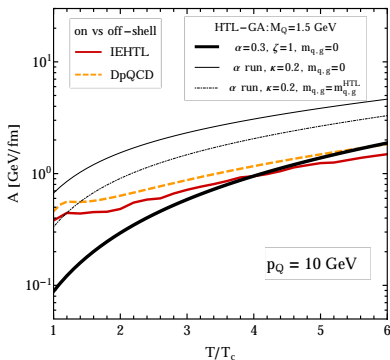
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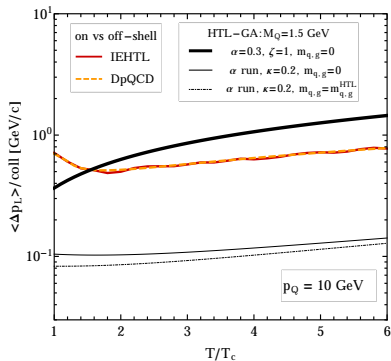
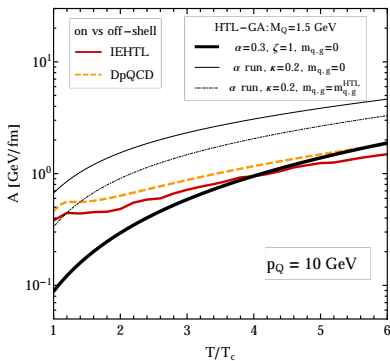
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- pQCD \rightarrow non-pQCD based models : reduction of A , dE/dx
- Finite $m_{q,g} \rightarrow$ reduction of the drag coefficient, dE/dx in the HTL-GA approach
- pQCD α_s cst \rightarrow α_s running : large effect in A , dE/dx temperature dependence
- Enhancement of DpQCD/IEHTL at low temperatures \rightarrow strong increase of α_s (infrared enhancement)

HQ energy and longitudinal momentum losses at finite T



- On- \rightarrow off-shell : noticeable difference in A , dE/dx (propagators + asymmetry of $\rho^{BW}(m)$)
- pQCD \rightarrow non-pQCD based models : reduction of A , dE/dx but enhancement of $\langle \Delta p_L \rangle$
- Finite $m_{q,g}$ \rightarrow reduction of the drag coefficient, dE/dx and $\langle \Delta p_L \rangle$ in the HTL-GA approach
- pQCD α_s cst \rightarrow α_s running : large effect in A , dE/dx and $\langle \Delta p_L \rangle$ temperature dependence
- Enhancement of DpQCD/IEHTL at low temperatures \rightarrow strong increase of α_s (infrared enhancement)
- A , dE/dx and $\langle \Delta p_L \rangle$ depend on : i) our description of $\sigma^{g,g-Q}$, ii) nature of the QGP

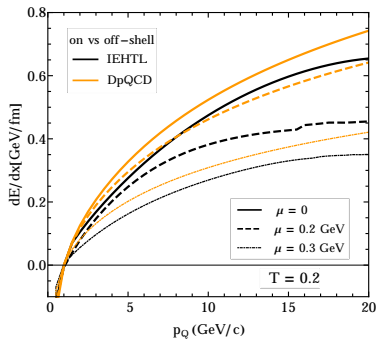
HQ energy and longitudinal momentum losses at finite T



- On- \rightarrow off-shell : noticeable difference in $A, dE/dx$ (propagators + asymmetry of $\rho^{BW}(m)$)
- pQCD \rightarrow non-pQCD based models : reduction of $A, dE/dx$ but enhancement of $\langle \Delta p_L \rangle$
- Finite $m_{q,g} \rightarrow$ reduction of the drag coefficient, dE/dx and $\langle \Delta p_L \rangle$ in the HTL-GA approach
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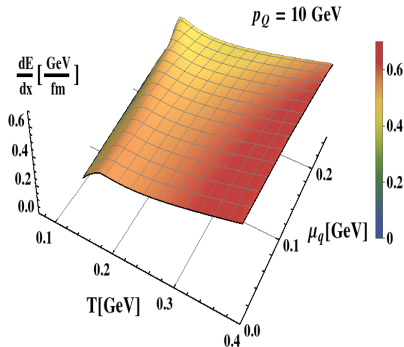
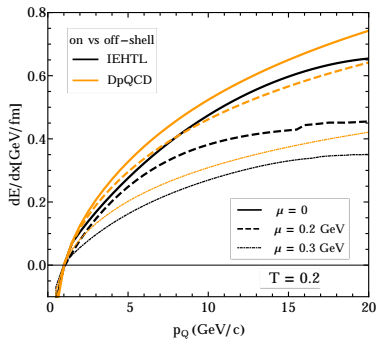
$A, dE/dx, \langle \Delta p_L \rangle, \dots$ vary substantially due to different assumptions/ingredients \rightarrow Systematic study of the models on the level of: i) microscopic/mesoscopic ingredients, ii) macroscopic observables v_2, R_{AA}

HQ energy and longitudinal momentum losses at finite (T, μ_q)



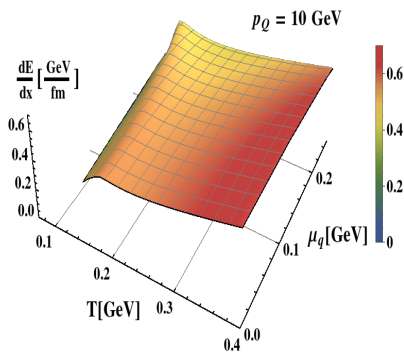
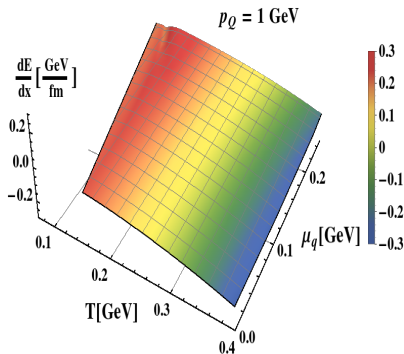
- On- \rightarrow off-shell : noticeable difference in dE/dx , A but uniform as $\mu_q \nearrow$
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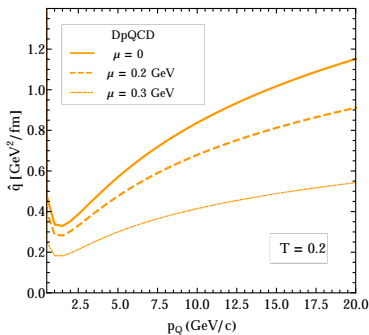
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- $\mu_q = 0 \rightarrow$ finite μ_q : smooth dependence on both variables T and μ
- $\mu_q = 0$: for low p_Q , HQ gains energy to approach thermal equilibrium ($dE/dx < 0$)
- $\mu_q \neq 0$: for low p_Q , HQ losses energy even at small T

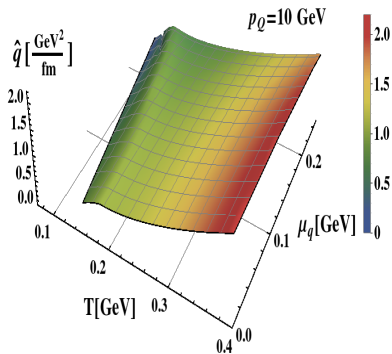
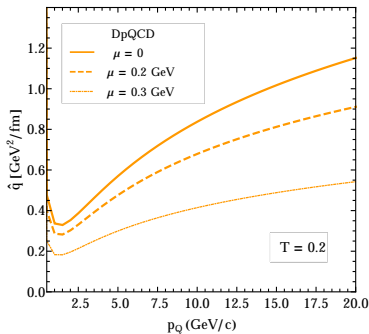
HQ might loss considerable energy not only in a HOT but also in a DENSE medium

HQ transverse momentum loss at finite (T, μ_q)



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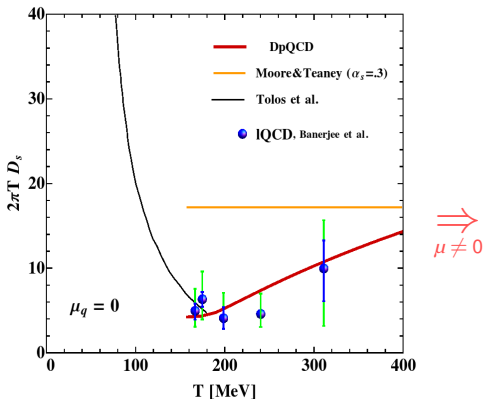
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- $\mu_q = 0 \rightarrow$ finite μ_q : decrease of \hat{q} , $\forall T, \forall p_Q$

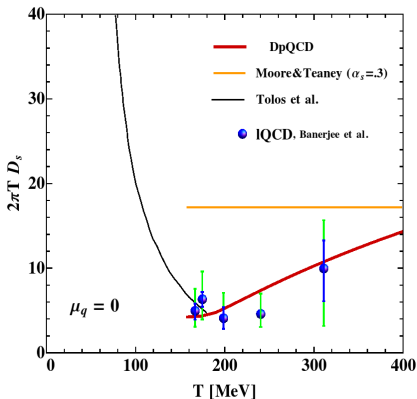
HQ transverse momentum loss is more remarkable in a HOT medium. The DENSE medium has little influence on $\frac{\Delta \langle p_T^2 \rangle}{\Delta x}$.

HQ spatial diffusion coefficient in HOT and DENSE medium

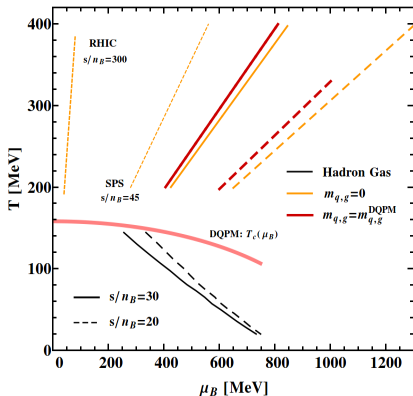


- $D_s = T/(M_Q \eta_D) = 2T^2/\kappa$; $\kappa = d \langle (\vec{p} - \vec{p}')^2 \rangle / 3d\tau$. Nice agreement around the cross over T_c at $\mu = 0$
- Minimum at T_c for FAIR energies??

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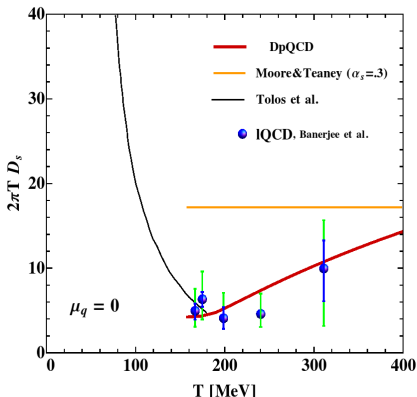


\Rightarrow
 $\mu \neq 0$

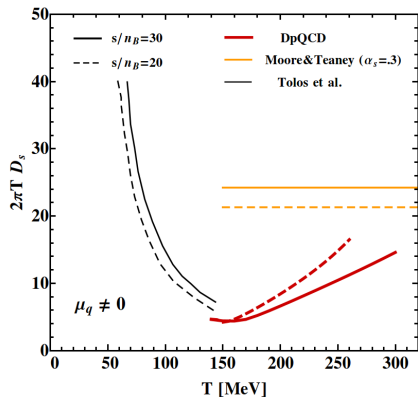


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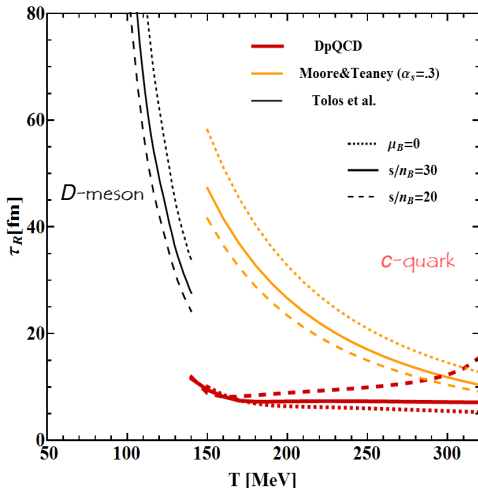


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- Minimum at T_c for FAIR energies??
- Adiabatic FAIR trajectories (with $S/N_B = 20 - 30$) following . . .
- Continuous transition \rightarrow No 1st order transition \rightarrow Consistent with our model assumptions
- HQ physics : Both partonic and hadronic worlds contribute? \rightarrow quantitative studies

HQ relaxation time in HOT and DENSE medium



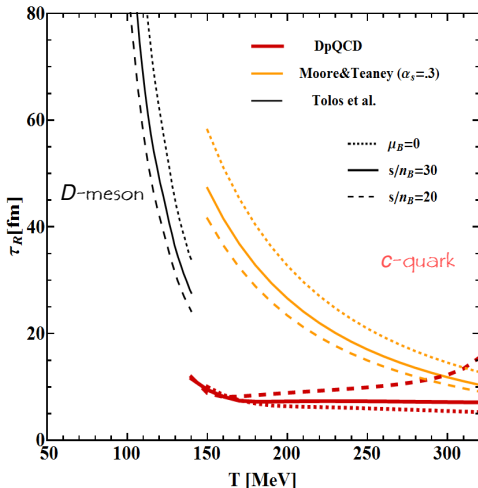
- Almost good matching between c-quark and D-meson relaxation times
- Perturbative models \rightarrow large c-quark relaxation time around T_c
- Non-perturbative treatment of c-quark interactions with $q, g \rightarrow$ necessary around T_c
- $\mu_q = 0 \rightarrow \mu_q$ finite : small enhancement of τ_R , due to a decrease of the $q, g-Q$ interaction strength

Moore and Teaney, PRC 71, 064904 (2005)

Tolos et al, PRD 88, 074019 (2013)

D-meson, see talks : J. Torres-Rincon & V. Ozvenchuk

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Strong indication that close to the phase transition the effective degrees-of-freedom are dynamically dressed massive quasi-particles and not massless quarks and gluons.

Moore and Teaney, PRC 71, 064904 (2005)

Tolos et al, PRD 88, 074019 (2013)

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1 Goals :

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ii) noticeable effect on the mesoscopic level
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3 Perspectives : HQ dynamics in the QGP at finite (T, μ)

- Extend our model to include 1st order transition
- Implement the HQ partonic processes into the PHSD transport approach to study HQ dynamics at CBM, SPS, RHIC and LHC

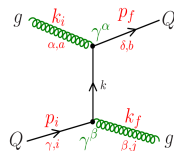
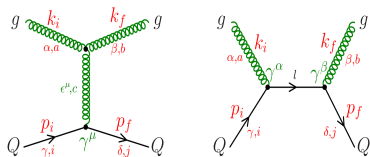
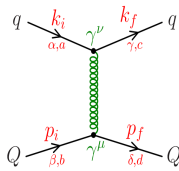


Back up

Cross Sections at finite temperature

1 Problems

- Coupling constant α_s (qqg , ggg and $gggg$ vertices)
- Regularization cut-off $\frac{1}{t - \mu}$
- Quark and gluon propagators at finite temperature and chemical potential
- q, Q, g masses at finite temperature and chemical potential
- Gauge invariance of the amplitudes



Dynamical quasi-particle model (DQPM) at finite T

1 DQPM entropy density

$$s_i^{DQP} = - \int \frac{d\omega}{2\pi} \frac{d^3 p}{(2\pi)^3} \frac{\partial n_i}{\partial T} \left(\Im \ln(-\Delta^{-1}) + \Im \Pi \times \Re \Delta \right)$$

$$s^{DQP} = s^{(0),DQP} + \Delta s^{DQP},$$

$$s^{(0),DQP} = \frac{1}{T} \int \frac{d^3 p}{(2\pi)^3} \left(-T \ln(1 - e^{-\omega/T}) + \omega n_B(\omega) \right)$$

$$\Delta s^{DQP} = \int \frac{d\omega}{2\pi} \frac{d^3 p}{(2\pi)^3} \frac{dn_B}{dT} \left(\arctan \lambda - \frac{\lambda}{1 + \lambda^2} \right),$$

with: $\lambda = \Im \Delta / \Re \Delta$

$$\Delta(\rho_0, \mathbf{p}) = \int_{-\infty}^{+\infty} \frac{d\omega}{2\pi} \frac{A(\omega, \mathbf{p})}{\rho_0 - \omega}$$

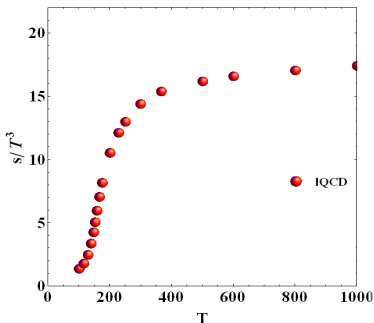
\Downarrow

$$A(\omega, \mathbf{p}) = \frac{\gamma}{E} \left(\frac{1}{(\omega - E)^2 + \gamma^2} - \frac{1}{(\omega + E)^2 + \gamma^2} \right)$$

Peshier, Cassing, PRL 94 (2005) 172301

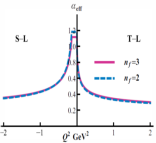
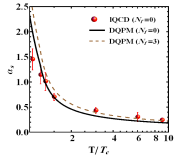
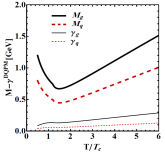
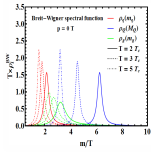
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

IQCD: WB JHEP. 09 (2010) 073; 11 (2010) 077



$T_c = 0.158 \text{ GeV}$, $T_s = 0.56 T_c$
 $\lambda = 2.42$, $c = 14.4$

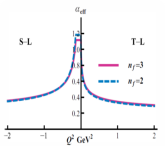
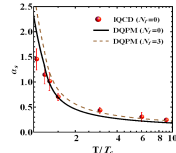
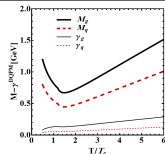
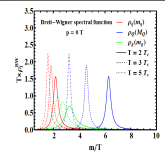
On- vs Off-shell; pQCD vs non-pQCD based approaches

	Naive pQCD	HTL-GA	DpQCD	IEHTL
α_s	Constant $\alpha_s = 0.3$			
Propagators	$\frac{1}{t - \xi \tilde{m}_D^2}$ $\xi = 1$	$\frac{1}{t - \kappa \tilde{m}_D^2}, \kappa = 0.2$ $\tilde{m}_D^2(T) = \frac{N_c}{3} \left(1 + \frac{N_f}{6}\right)$ $\times 4\pi\alpha_s(-\tilde{m}_D(T^2))T^2$	$G_F^{\mu\nu}(q, m_g) =$ $-i \frac{g_{\mu\nu} - q_\mu q_\nu / m_g^2}{q^2 - m_g^2}$ $S_F(p, M_Q) = \frac{\not{p} + M_Q}{p^2 - M_Q^2}$	$G_F^{\mu\nu}(q, m_g) =$ $-i \frac{g_{\mu\nu} - q_\mu q_\nu / m_g^2}{q_0^2 - \mathbf{q}^2 - m_g^2 + i2\gamma_g q_0}$ $\Rightarrow \frac{\not{p} + M_Q}{p_0^2 - \mathbf{p}^2 - M_Q^2 + i2\gamma_Q p_0}$
Masses	$M_c = 1.5 \text{ GeV}, m_q = m_g = 0$			

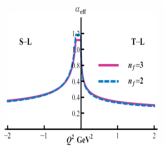
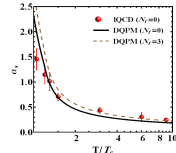
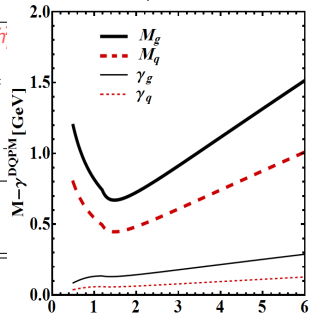
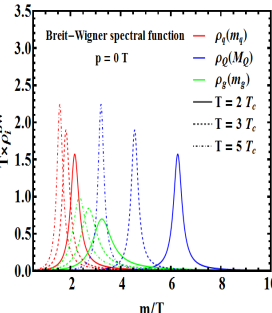
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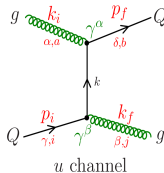
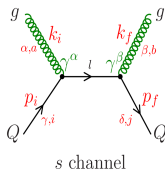
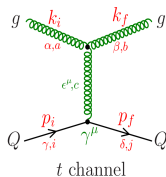
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Heavy Quark Elastic Scattering

gQ Elastic Scattering

Additional Problems : 3
gluon vertex, gauge
invariance



pQCD (massless g, q)

Transverse gauge :

$$\sum_{\text{spins}} \epsilon_i^\mu \epsilon_i^{*\mu'} =$$

$$-g^{\mu\mu'} + \frac{2}{s} (p_i^\mu k_i^{\mu'} + p_i^{\mu'} k_i^\mu)$$

HTL (Hard Thermal Loop)

Transverse gauge

$$G_F^{\mu\nu}(q, m_g) = -i \frac{g_{\mu\nu}}{q^2 - \kappa m_D^2}$$

DpQCD (Dressed pQCD)

$$\text{Lorentz Covariance : } \sum_{\text{pol}, i} \epsilon_{i,\alpha} \epsilon_{i,\lambda} = g_{\alpha\lambda} - \frac{k_{i,\alpha} k_{i,\lambda}}{(m_g^i)^2},$$

$$G_F^{\mu\nu}(q, m_g) = -i \frac{g_{\mu\nu} - q_\mu q_\nu / m_g^2}{q^2 - m_g^2}, \quad S_F(p, M_Q) = \frac{\not{p} + M_Q}{p^2 - M_Q^2}$$

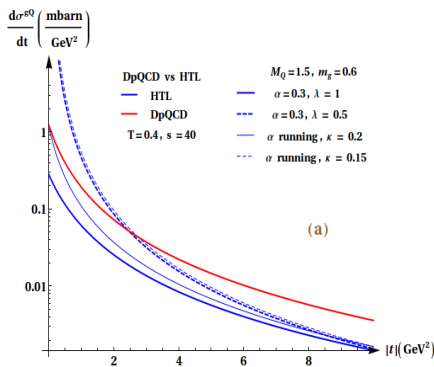
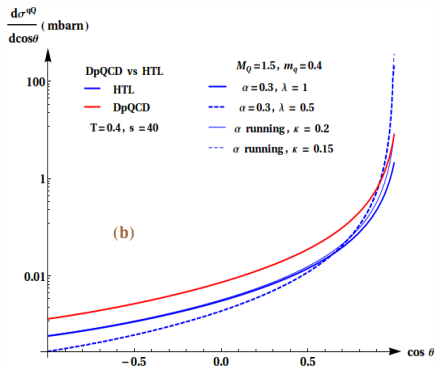
IEHTL (Infrared Enhanced HTL)

$$\text{Lorentz Covariance, } G_F^{\mu\nu}(q, m_g) = -i \frac{g_{\mu\nu} - q_\mu q_\nu / m_g^2}{q_0^2 - \mathbf{q}^2 - m_g^2 + i2\gamma_g q_0}$$

$$S_F(p, M_Q) = \frac{\not{p} + M_Q}{p_0^2 - \mathbf{p}^2 - M_Q^2 + i2\gamma_Q p_0}$$

Heavy Quark Elastic Scattering

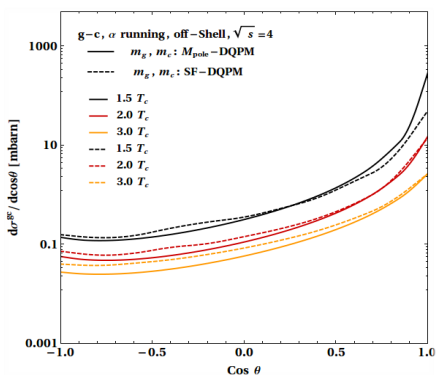
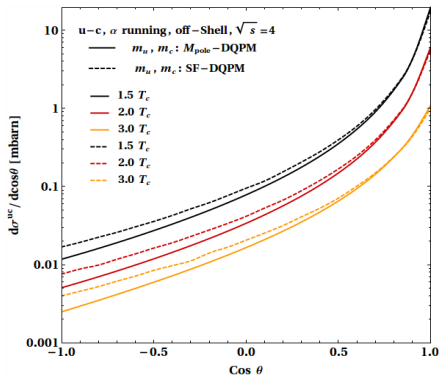
1 σ_{qQ}, σ_{gQ} : HTL vs DpQCD



- HTL/DpQCD : Different behaviours for small/large “ t ”
- σ_{qQ} higher value for running + $\kappa = 0.2$ (differences related to $m_g^{\text{exchanged}}$)
- σ_{qQ}/σ_{gQ} : Same conclusions with larger values for σ_{gQ} • $\sigma(T \nearrow) < \sigma(T \searrow)$

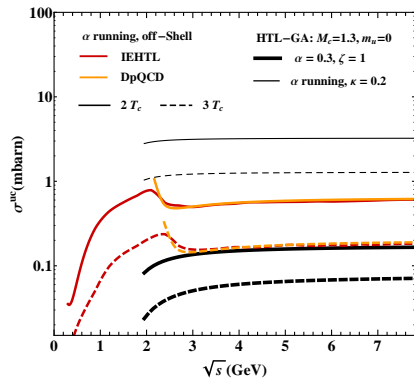
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1 $\sigma_{qQ}, \sigma_{gQ} : \text{DpQCD (On-Shell)} \text{ vs IEHTL (Off-Shell)}$



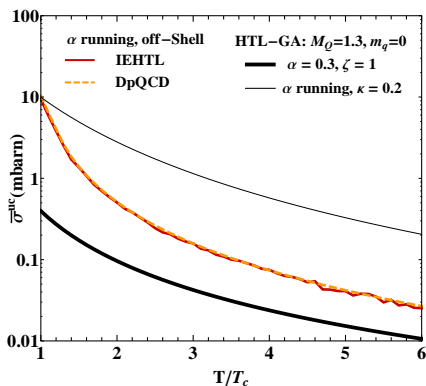
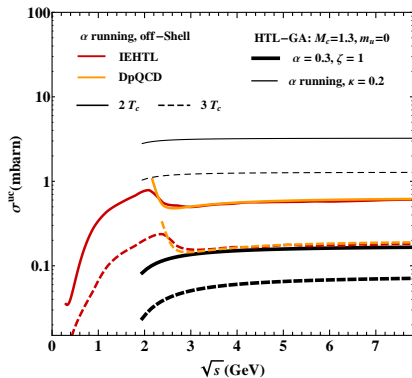
- Deviation of off-shell curves compared to on-shell ones for large angles θ
- Effect of $A(m, T)$ on σ_{qQ} is negligible (small DQPM parton width)
- $\sigma_{qQ}(T \nearrow) < \sigma_{qQ}(T \searrow)$

HQ elastic scattering at finite T : HTL-GA vs DpQCD vs IEHTL



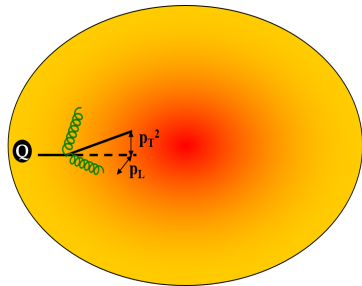
- Different behaviours between HTL-GA and DpQCD/IEHTL for small/large “t”
- σ^{qQ} larger value for HTL-GA with α running + $\kappa = 0.2$ (differences related to $m_g^{\text{exchanged}}$)
- Effect of $\rho^{BW}(m)$ is negligible (small parton width), **except reducing the kinematic threshold**
- Same conclusions as σ^{qQ} can be drawn with larger values for σ^{gQ} (9/4 : color Casimir operators)

HQ elastic scattering at finite T : HTL-GA vs DpQCD vs IEHTL



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- $\bar{\sigma}^{qQ}$: diff power laws in T , i.e. $\bar{\sigma}^{qQ} \sim T^{-\beta}$ (diff β) \rightarrow **sizeable effect on the transport**

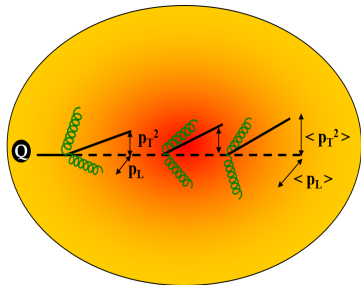
HQ Transport properties



● Single collision

- $\langle p_L \rangle$: average longitudinal transfer momentum
- $\langle p_T^2 \rangle$: average transverse transfer momentum squared

HQ Transport properties



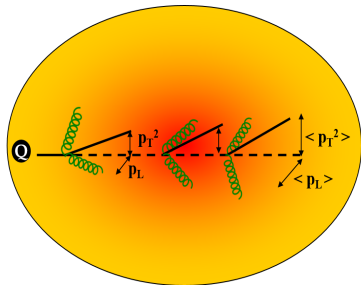
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2 Average over number of collisions

- Drag : $A = \langle p_L \rangle \times \frac{N_{coll}}{fm}$
- \hat{q} : $\hat{q} = \frac{d \langle p_T^2 \rangle}{dx} = \frac{\langle p_T^2 \rangle_{single\ coll}}{\ell} = \frac{2}{v} b_T$
- $B^{ij}(\vec{p}) = b_L(p) \hat{p}^i \hat{p}^j + b_T(p) (\delta^{ij} - \hat{p}^i \hat{p}^j)$,
with : $b_L(p) = \frac{\langle \Delta p_L^2 \rangle}{\Delta t}$; $b_T = \frac{1}{2} \frac{\langle \Delta p_T^2 \rangle}{\Delta t}$
- Collisional energy loss : $\frac{d \langle E \rangle}{dx}$
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HQ Transport properties



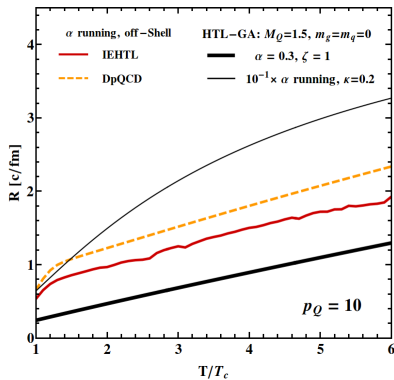
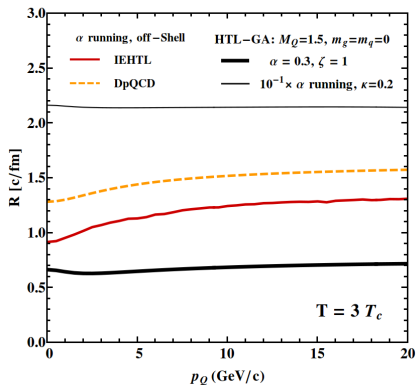
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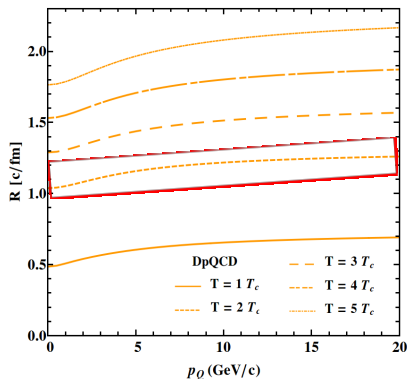
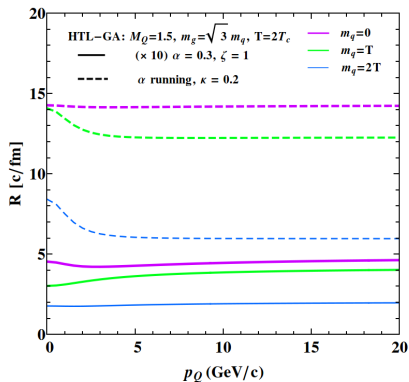
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\mathcal{R} : Interaction rate



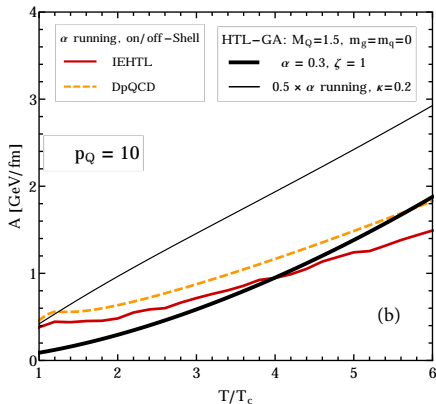
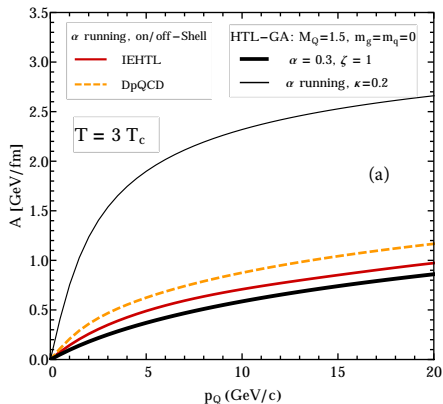
- \mathcal{R} is larger when $\sigma^{q,g-Q}$ is described by HTL-GA with running α_s as compared to the DpQCD/IEHTL models. $\mathcal{R}(\alpha_s \text{ running}) > \mathcal{R}(\alpha_s \text{ cst.})$.
- Effect of $\rho(m, T)$ on \mathcal{R} is noticeable (shift of the off-shell threshold)
- \mathcal{R} depends on : i) our description of $\sigma^{q,g-Q}$, ii) nature of the QGP constituents

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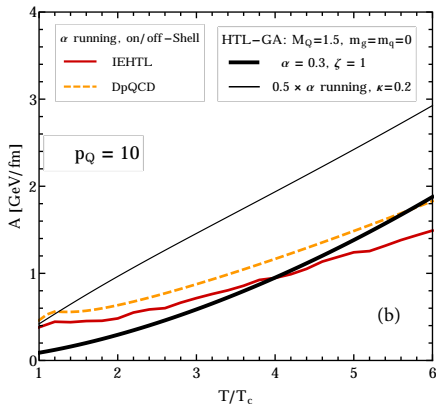
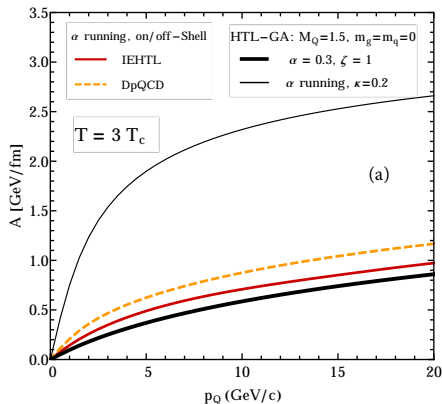
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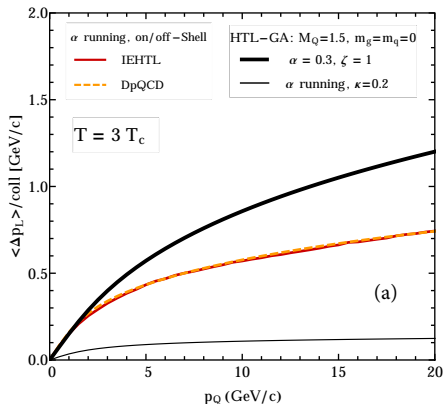
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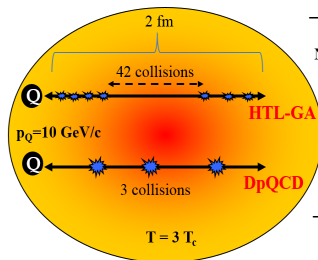
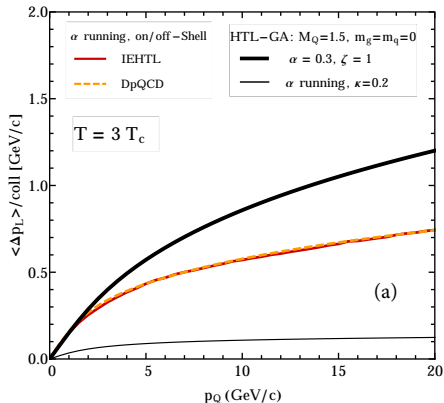
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$\langle \Delta p_L \rangle = \mathcal{A}/\mathcal{R}ate$: average longitudinal momentum loss



- Opposite trends are observed for the momentum transfer per collision $\langle \Delta p_L \rangle$ 😊
- \rightarrow finite parton mass leads to an increase of the momentum transfer per collision

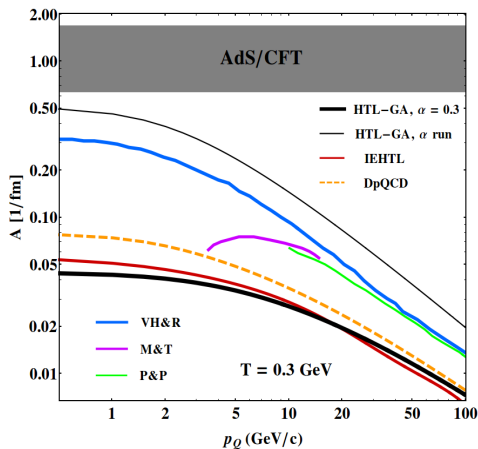
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R N_{coll}/fm	\mathcal{A} GeV/fm	$\langle \Delta p_L \rangle$ GeV
~ 21	~ 2.5	~ 0.12
~ 1.5	~ 0.85	~ 0.57

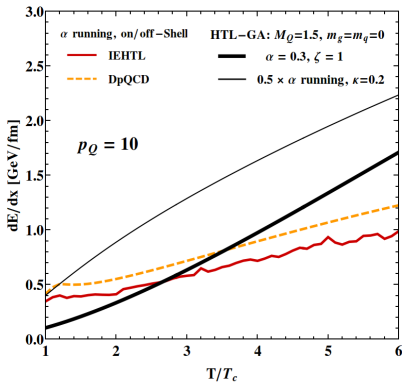
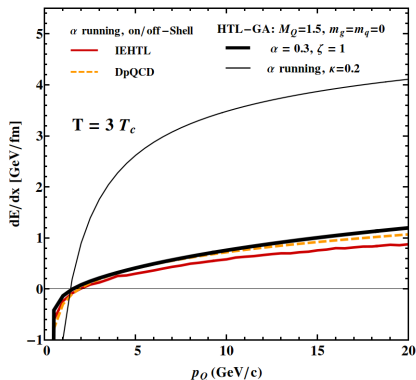
- Opposite trends are observed for the momentum transfer per collision $\langle \Delta p_L \rangle$ 😊
- \rightarrow finite parton mass leads to an increase of the momentum transfer per collision
- Q undergoes more kicks from massless medium partons than the massive ones but nevertheless transfer less energy \rightarrow finite $m_{q,g} + (\alpha_s, IR \text{ regulator})$

Drag coefficient : extended models comparison



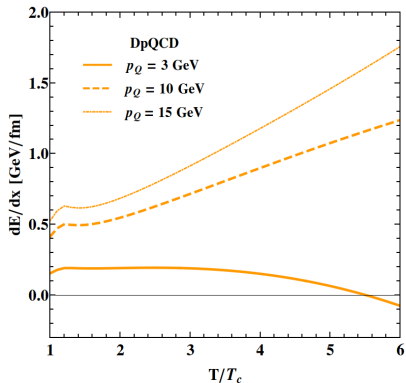
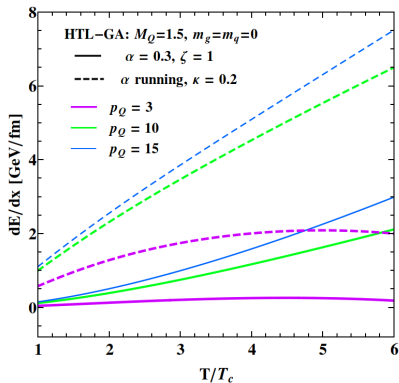
- \mathcal{A} is momentum independent in AdS/CFT approach. All pQCD and non-pQCD based drag coefficients \searrow with $\nearrow p_Q$.
- \mathcal{A} vary substantially due to different assumptions/ ingredients
- \rightarrow Systematic study between the models on the level of
 - microscopic/mesoscopic ingredients,
 - macroscopic observables v_2, R_{AA}

dE/dx : Energy loss



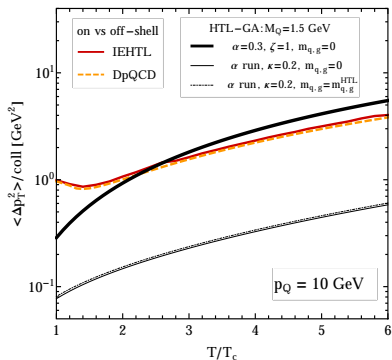
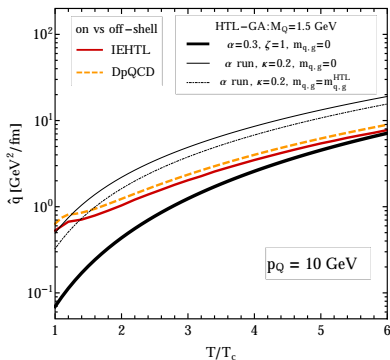
- Conclusions for \mathcal{A} remain valid for $dE/dx \rightarrow$ reduction of dE/dx for finite $m_{q,g}$
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dE/dx : Energy loss



- Conclusions for \mathcal{A} remain valid for $dE/dx \rightarrow$ reduction of dE/dx for finite $m_{q,g}$
- Q undergoes more kicks from massless medium partons than the massive ones but nevertheless transfer less energy
- For large T the low p_Q HQ starts to gain energy to approach thermal equilibrium

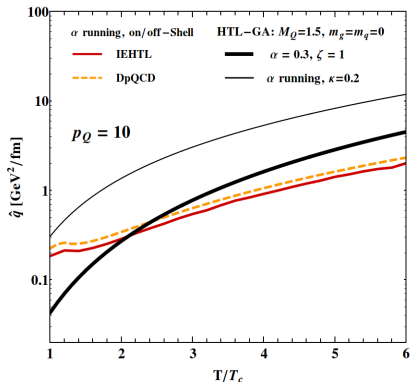
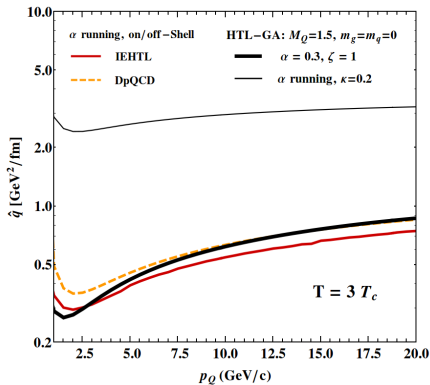
HQ transverse momentum loss at finite T



- $\hat{q} = \frac{\Delta \langle p_T^2 \rangle}{\Delta x} = \frac{4E}{p} B_T, \quad \langle \Delta p_T^2 \rangle \propto \hat{q}/R \propto \langle |t| \rangle, \quad \langle \Delta p_L \rangle \propto A/R \propto \frac{\langle |t| \rangle}{m_q}, \quad \text{with: } \langle |t| \rangle = [(\langle \sigma |t| \rangle) (q = \frac{m_q p}{M_Q})] / \sigma_{as}$
- Finite $m_{q,g} \rightarrow$ increase of the transverse Q momentum loss per collision in the HTL-GA
- More kicks in HTL-GA but less energy/momentum transfer per collision than in DpQCD/IEHTL
- \sim temperature independence of $\langle \Delta p_L \rangle$, but large increase of $\langle \Delta p_T^2 \rangle$ with $T \nearrow$

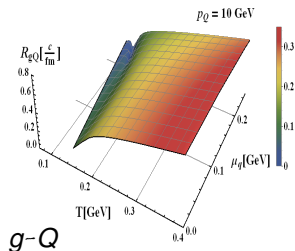
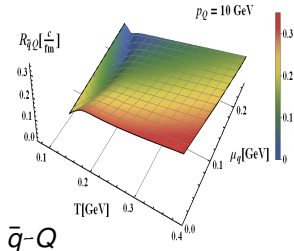
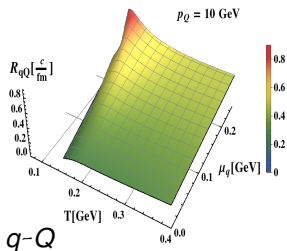
$A, dE/dx, \langle \Delta p_L \rangle, \hat{q}, \dots$ vary substantially due to different assumptions/ingredients \rightarrow Systematic study of the models on the level of: i) microscopic/mesoscopic ingredients, ii) macroscopic observables v_2, R_{AA}

$$\hat{q} = \frac{d\langle p_T^2 \rangle}{dx} : \text{average transverse momentum loss}$$



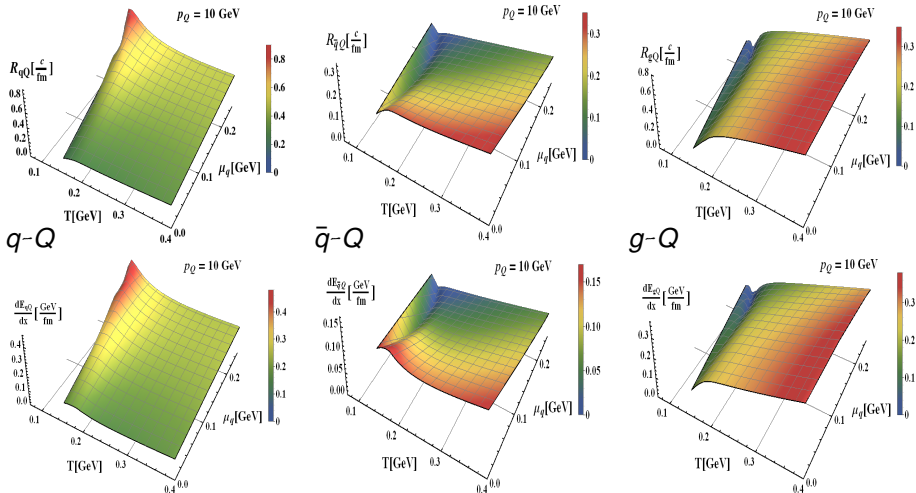
- Q transverse momentum loss : Massless HQ in HTL-GA (α_s running) \gg massive on-shell case (DpQCD) and off-shell (IEHTL) \rightarrow finite $m_{q,g} + (\alpha_s, \text{IR regulator})$
- Collisions with massless q, g have a shorter mean free path than with massive q, g
- $T \nearrow \rightarrow$ huge variation in the transverse Q momentum (HTL-GA, DpQCD/IEHTL)

HQ interaction rates and energy/momentum losses at finite (T, μ_q)



DENSE matter : HQ interacts mores with q than \bar{q}, g , due to the excess of q .

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HQ energy/momentum losses scales with the interaction rates $\rightarrow dE_{qQ}/dx > dE_{\bar{q}Q}/dx$