

# Properties of $K^*$ in a medium

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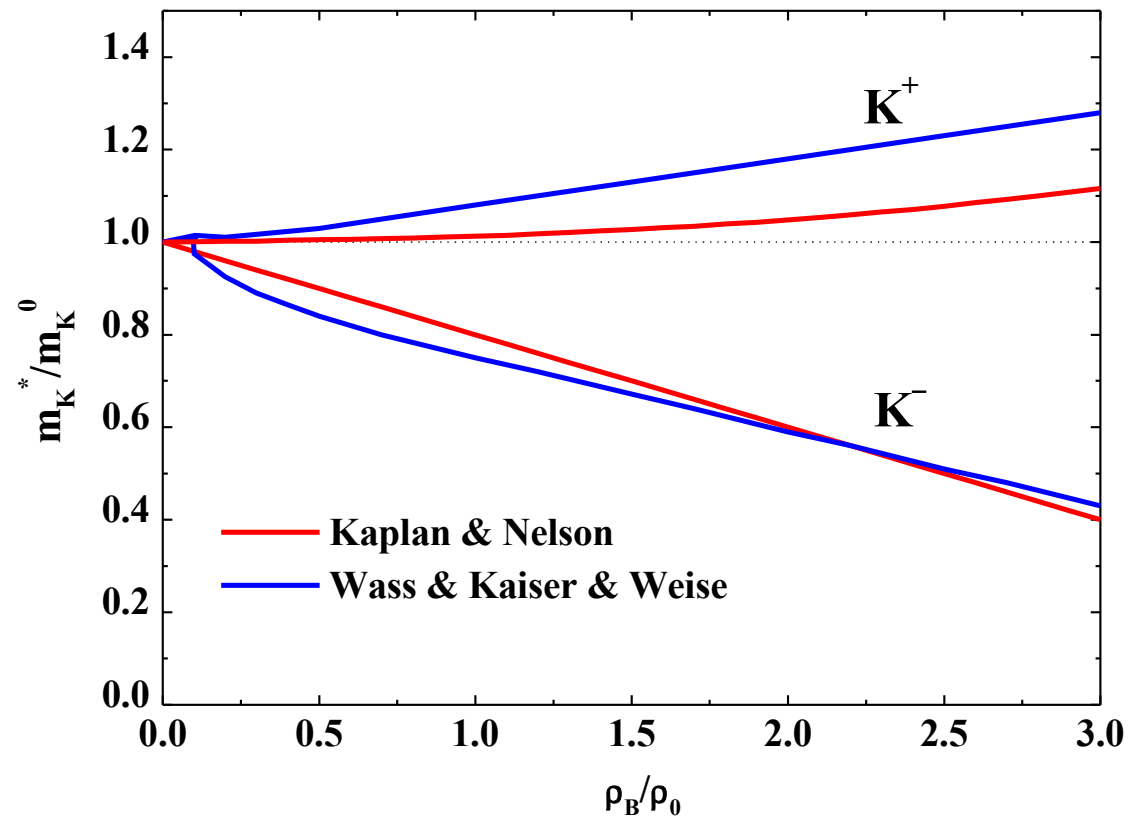
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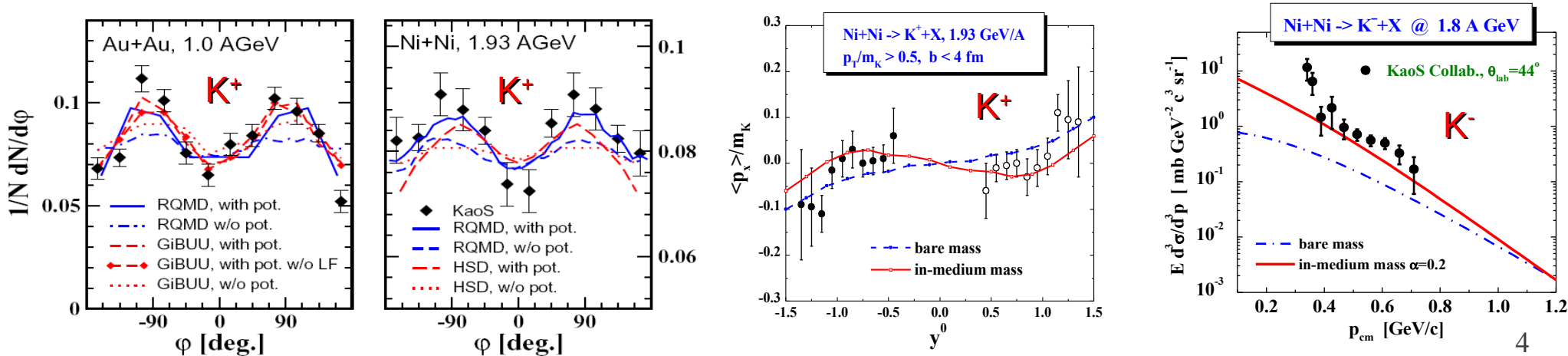
# Introduction and motivation

- **In-medium properties of kaons** (K, anti-K, K\* and anti-K\*)
- First results were obtained using **chiral perturbation theory** (*Kaplan, Nelson, PLB 175 (1986) 57*) and **relativistic mean field models** (*Schaffner, Gal, Mishustin, Stöcker, Greiner, PLB 334 (1994) 268*)
- **Dirac-Brueckner Hartree-Fock** approximation (*Brueckner, PR 97 (1955) 1353; Hjorth-Jensen et al., PR 261 (1995) 125*) applied to **KN system**
- DBHF goes beyond a mean fields and uses realistic KN interactions for the calculations



# Introduction and motivation

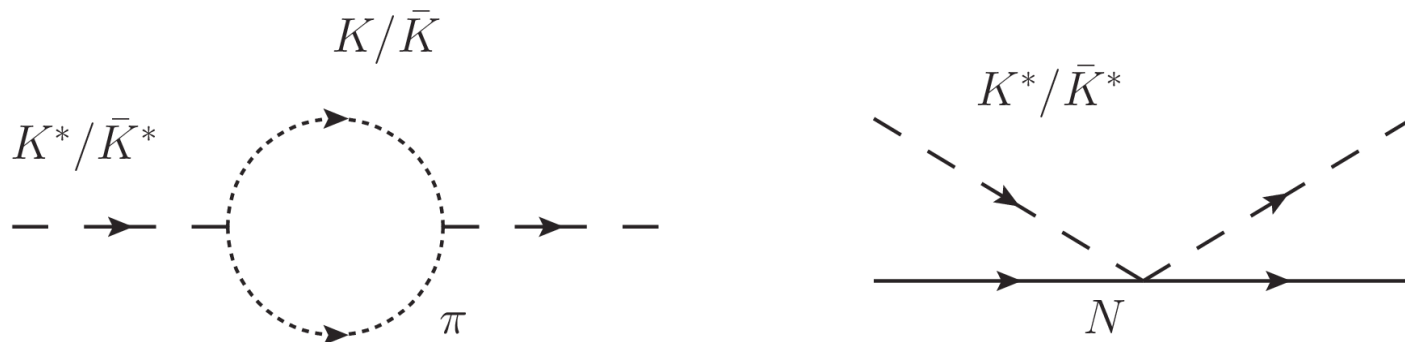
- Experimentally strangeness has been studied since the 1980s
- In-medium properties are studied e.g. in heavy-ion collisions
- For baryonic matter at SIS (and in the future at FAIR) etc. energies
- For hot nuclear matter at RHIC, LHC etc. energies
- Later KaoS collaboration published results which agreed with theoretical predictions **when including K / anti-K in-medium effects**



Figs. by E. Bratkovskaya et al.

# Introduction and motivation

- Goal: study in-medium strange pseudoscalar and vector mesons within Breit-Wigner approach in a consistent way, for a convenient implementation in transport models of strangeness production in HICs
- 1. Dense nuclear matter (FAIR): self-consistent coupled-channel approach (“G-matrix”)
  - $K^*$  and anti- $K^*$  modified from  $K^*N$  and  $K^* \rightarrow K \pi$  [*different behaviour!*]
  - $K^*$  self-energy within the unitarised chiral perturbation theory [*NEW!*]
- 2. Hot nuclear matter (RHIC/LHC): results from Chiral Perturbation Theory in hot meson gas
  - $K^*$  and anti- $K^*$  in-medium effects from  $K^* \rightarrow K \pi$  coupling [behave similarly]
  - Estimation of the real part of the  $K^*$  self-energy [*mass shift!*]



# Framework

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- **G-matrix** results are approximated by the **Breit-Wigner** spectral function
- Evaluation of in-medium **widths** and **masses**, which are connected to **imaginary** and **real** part of the **self-energy** of strange mesons
- Approximation implicitly neglects momentum dependence of self-energy

# Framework

The meson propagator ( $i = K, anti-K; K^*, anti-K^*$ )

$$D_i(\omega, \vec{q}, \rho) = \frac{1}{\omega^2 - \vec{q}^2 - m_i^2 - \Pi_i(\omega, \vec{q}, \rho)}$$

$\omega$ : energy

$\vec{q}$ : momentum

$m_i$ : pole mass

$\Pi_i$ : Self-energy

$\rho$ : baryon density

Spectral function

$$S_i(\omega, \vec{q}, \rho) = -\frac{1}{\pi} \Im(D_i(\omega, \vec{q}, \rho)) = -\frac{1}{\pi} \frac{\Im(\Pi_i(\omega, \vec{q}, \rho))}{|\omega^2 - \vec{q}^2 - m_i^2 - \Pi_i(\omega, \vec{q}, \rho)|^2}$$

Spectral function rewritten in a way more similar to the Cauchy-Lorentz distribution

$$S_i(\omega, \vec{q}, \rho) = -\frac{1}{\pi} \frac{\Im(\Pi_i(\omega, \vec{q}, \rho))}{[\omega^2 - \vec{q}^2 - (m_i^2 + \Re(\Pi_i(\omega, \vec{q}, \rho)))]^2 + [\Im(\Pi_i(\omega, \vec{q}, \rho))]^2}$$

# Framework

Spectral function in the Breit-Wigner approach

$$A_i(M, \rho) = C_1 \frac{2}{\pi} \frac{M^2 \Gamma_i(M, \rho)}{(M^2 - M_0^*(\rho))^2 + (M \Gamma_i(M, \rho))^2}$$

$\Gamma_i$ : width

$M$ : (off-shell) mass or energy

$M_0$ : in-medium mass

$C_1$ : normalisation constant

For  $q=0$  a connection between the imaginary part of the meson propagator and the Breit-Wigner spectral can be established.

$$A_i(M, \rho) = 2 \cdot C_1 \cdot M S_i(M, \rho)$$

The following relations follow from that connection.

$$M_0^{2*} = m_i^2 + \Re(\Pi_i(M, \rho))$$

$$\Gamma_i(M, \rho) = -\frac{\Im(\Pi_i(M, \rho))}{M}$$

Spectral function is normalised

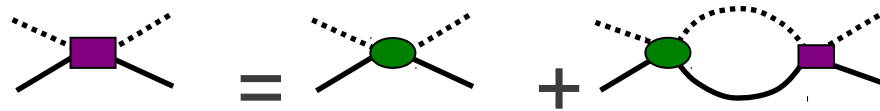
$$\int_0^\infty A_i(M, \rho) dM = 1$$

Energy dependence is omitted



# Dense matter

- Dense matter scenario: results from meson-baryon T (or G)-matrix in Dirac-Brueckner Hartree-Fock.
- Self-consistency, coupled-channels and unitarity.
- The Bethe-Salpeter equation in coupled channels is solved for the in-medium scattering amplitude.



$$\text{Medium: } T_{ij}(p) = V_{ij} + V_{il} G_l(p) T_{lj}(p)$$

*Koch*

*Kaiser, Waas, Weise*

*Lutz, Kolomeitsev;*

*Schaffner-Bielich*

*Ramos, Oset, Tolos*

*Oller, Meissner*

*Hosaka, Jido*

*Nieves, Ruiz-Arriola*

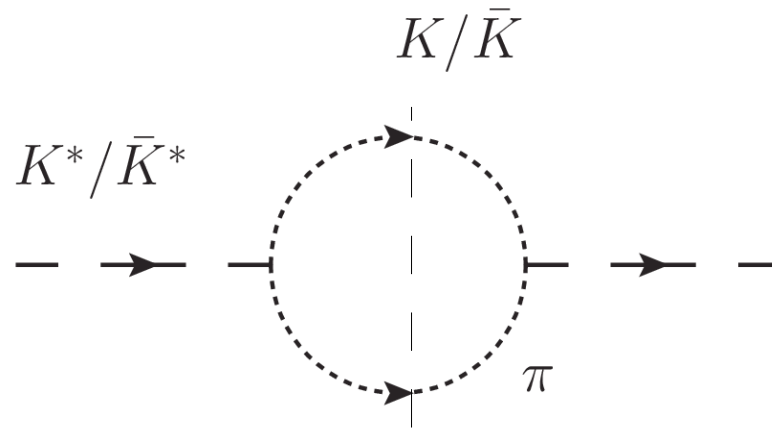
*Cassing, Bratkovskaya,*

*Tolos, Ramos*

- $V$  : LO interaction from chiral Lagrangian
  - KN: meson baryon ChPT (coupling of octet of pseudoscalar mesons to the octet of  $J^P=1/2^+$  baryons)
  - $K^*N$ : Hidden Local Gauge Symmetry Lagrangian (vector-meson octet)
- $G$  : dressed in-medium meson-baryon propagator, including Pauli blocking on nucleon states, baryon potentials and meson self-energies.

# Dense matter

- Additional contribution for strange vector mesons:  $K^*$  decays into  $K\pi$  (two-meson cloud effects)



- It is possible to account for the in-medium width of the  $K^* \rightarrow K\pi$  mode by incorporating the  $K$  spectral function
- *Pions* are also expected to experience in-medium modifications. Neglect this effect for simplicity (future work).

# Dense matter

The (p-wave) decay width of the  $K^*$

$$\Gamma_{K^*}(\mu, \rho) = \Gamma_0 \left( \frac{\mu_0}{\mu} \right)^2 \cdot \frac{\int_{M_{min}}^{\mu - m_\pi} A_K(M, \rho) \cdot q(\mu, M)^3 dM}{\int_{M_{min}}^{\mu_0 - m_\pi} A_K(M, 0) \cdot q(\mu_0, M)^3 dM}$$

$M$ : off-shell mass of the  $K$   
 $\mu$ : off-shell mass of the  $K^*$

with

$$q(\mu, M) = \frac{\sqrt{\lambda(\mu, M, m_\pi)}}{2\mu} \qquad q(\mu_0, M) = \frac{\sqrt{\lambda(\mu_0, M, m_\pi)}}{2\mu_0}$$

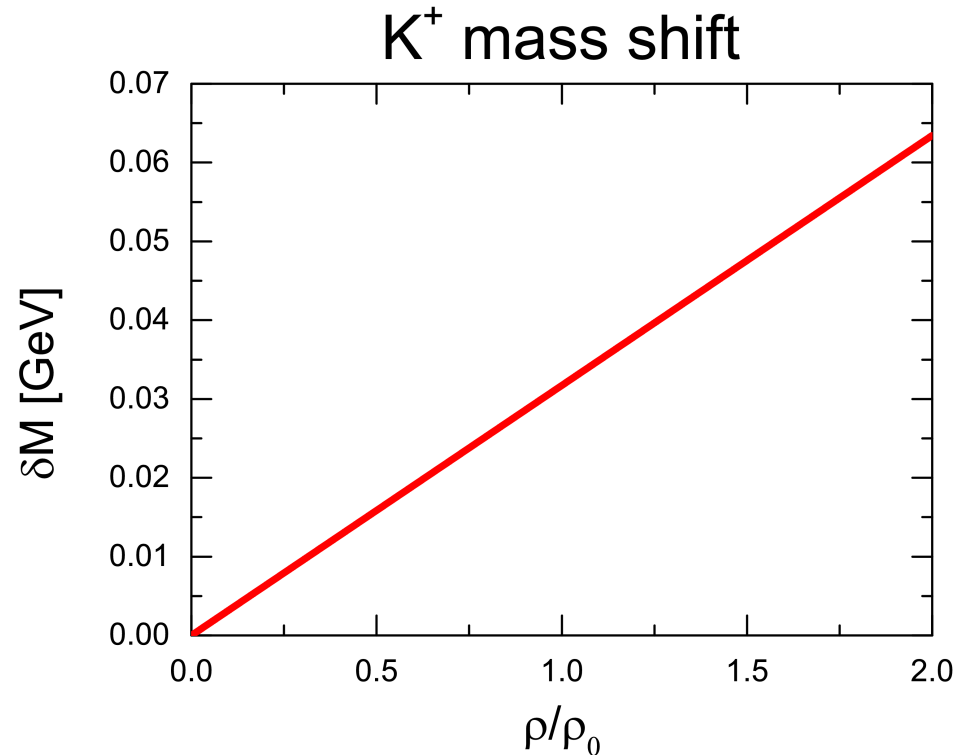
This is a similar approach that was also used for the  $\mathbf{a}_1$  decaying into  $\pi \rho$ .

# Dense matter: Kaons

- In a dense nuclear medium K behaves like a narrow quasi-particle (KN interaction smooth;

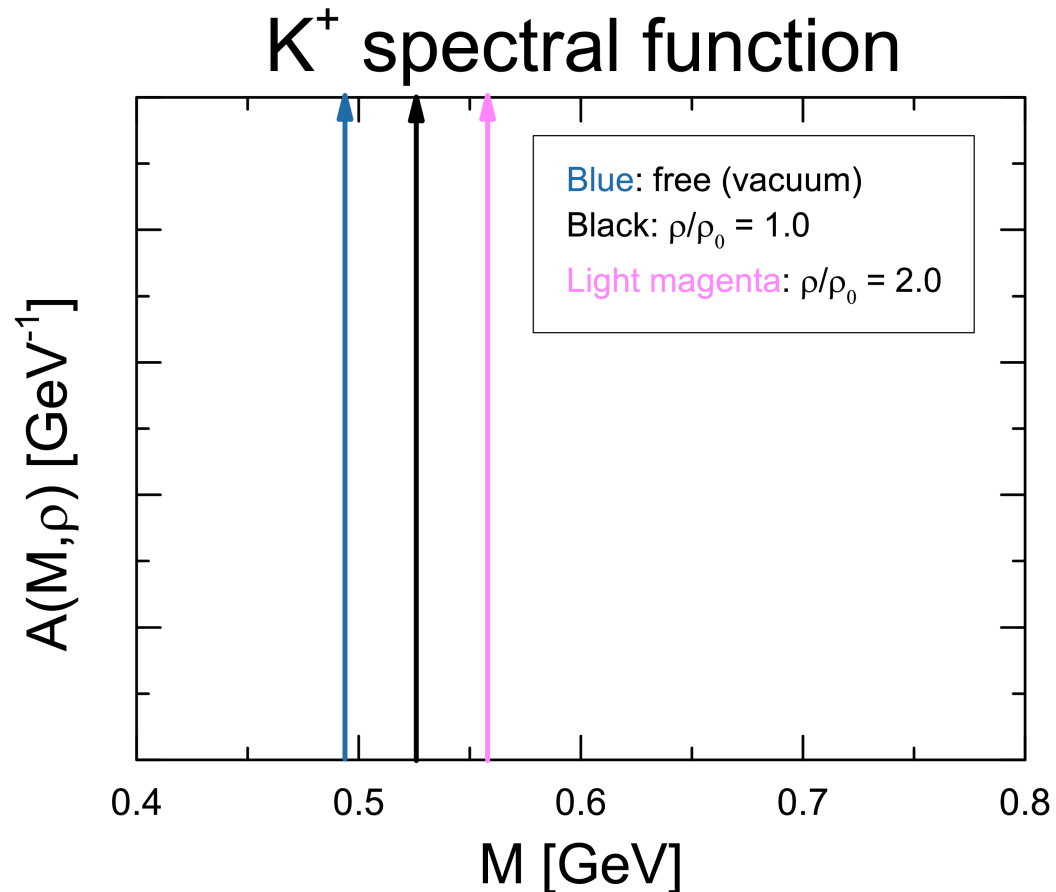
*Kaiser, Siegel, Weise NPA594 (1995) 325; Oset, Ramos, NPA635 (1998) 99*

- Neglect imaginary part of self-energy
- $\text{Re } \Pi \leftrightarrow$  mass shift from chiral Lagrangian dynamics in a  $t$ - $\rho$  approximation

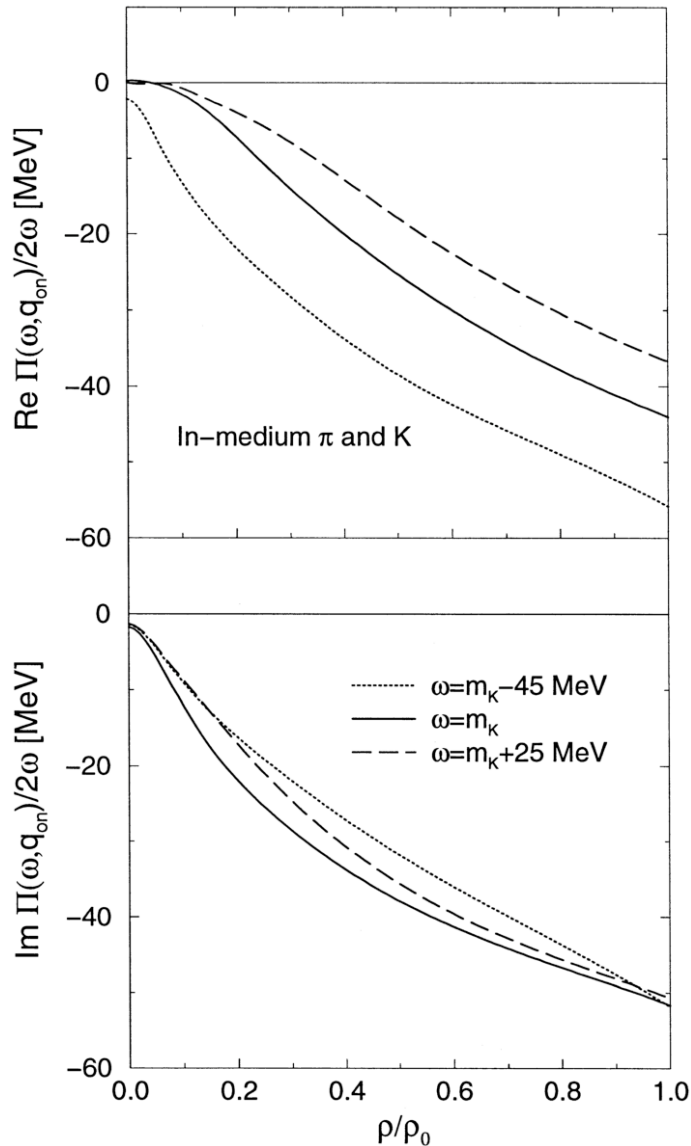


# Dense matter: Kaons

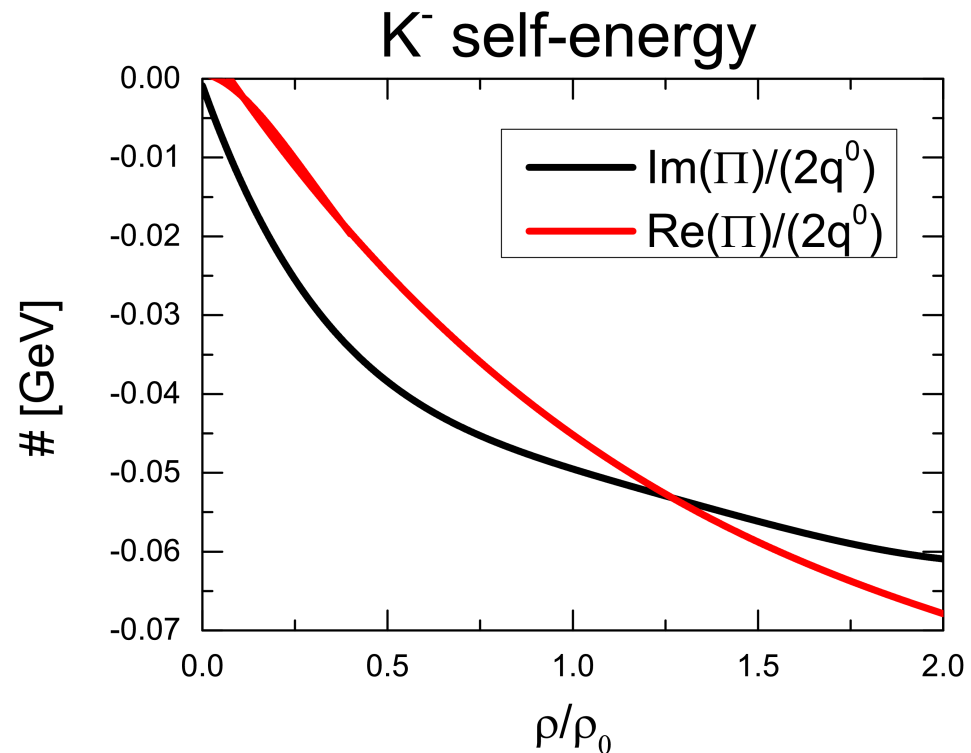
- The K has almost no broadening and behaves like a stable particle when increasing nuclear density (the “full” calculation leads to a very small width)
- K experiences a repulsive potential  $\rightarrow$  spectral function gains a positive mass shift



# Dense matter: anti-Kaons



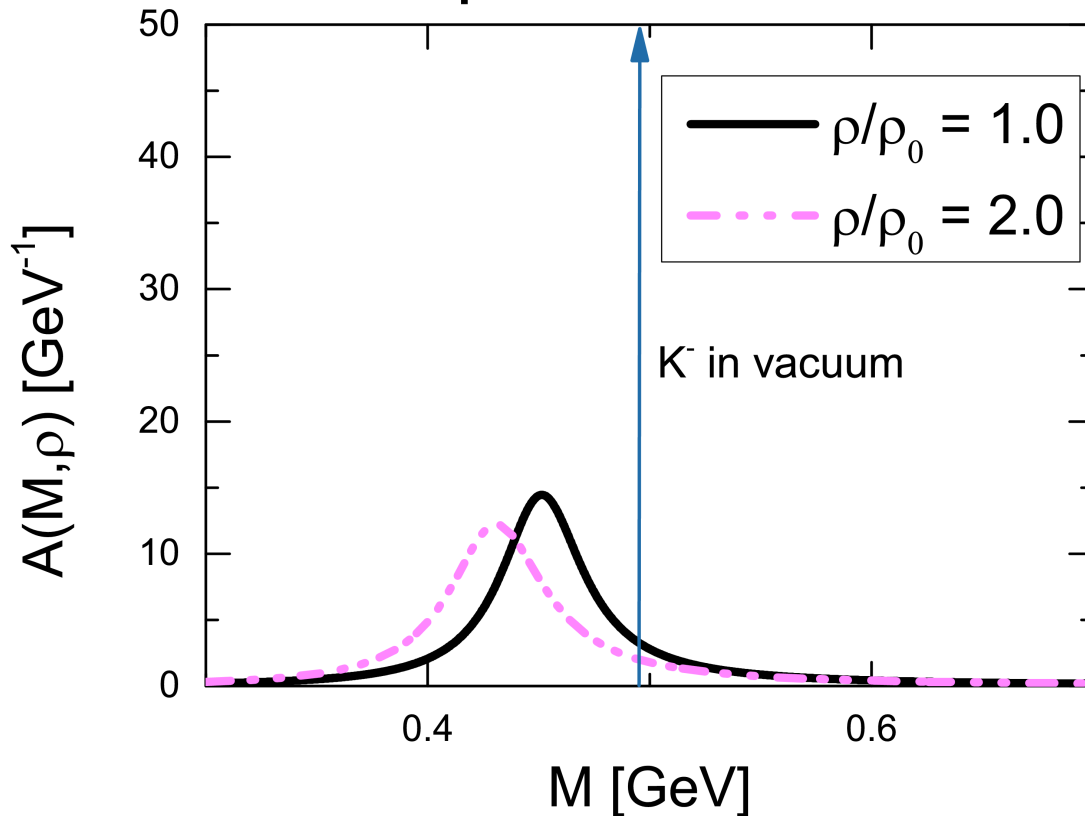
- Self-energy by Ramos et al. from G-matrix approach with ChPT, **anti-K N  $\rightarrow$   $\Lambda(1405)$ !**
- Results were extrapolated to higher densities (i.e. beyond normal density), assuming some saturation



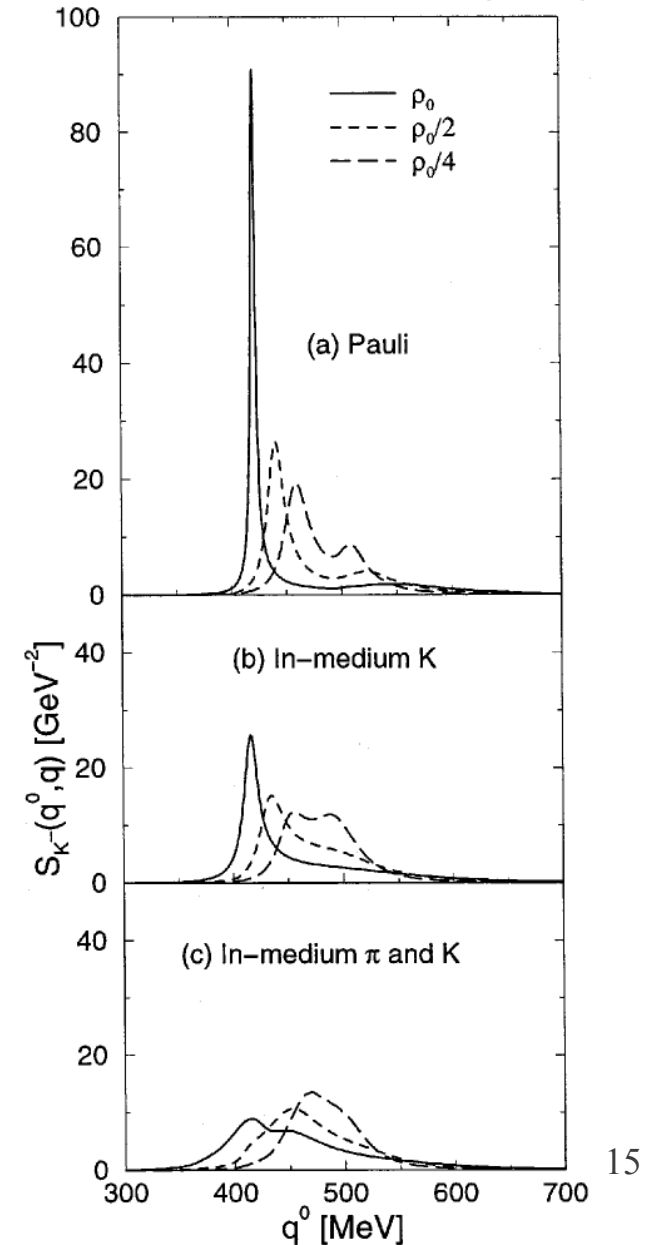
# Dense matter: anti-Kaons

- Spectral function for the anti-K
- In vacuum the particles are stable (Dirac delta)
- The anti-K experiences an **attractive potential**  
→ negative mass shift
- And **considerable broadening!**
- (detailed structure of excitations not retained)

## K<sup>-</sup> spectral function



Ramos, Oset, NPA 671 (2000) 481



# Dense matter: $K^*$

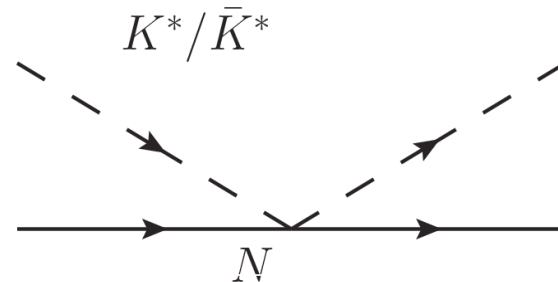
- New contribution:  $K^*$  self-energy from  $K^*N$  interaction

- The  $K^*$  in a dense nuclear medium can be treated just like the  $K$  with respect to the self-consistent chiral coupled-channel calculations based on chiral dynamics (*Tolos et al PRC87 (2010) 045210; Oset et al EPJA44 (2010) 445*)
- Same expression for the transition potential for  $K^*N$  as for the  $KN$ , also for the self-energy

$$\Pi(q^0, \vec{q}, \rho) = 2 \int \frac{n(\vec{p})}{(2\pi)^3} [T_{K^*p}(p^0, \vec{p}, \rho) + T_{K^*n}(p^0, \vec{p}, \rho)] d^3 p \approx \frac{1}{2} (T_{K^*p}(\rho) + T_{K^*n}(\rho)) \rho$$

- $t$ - $\rho$  approximation (no resonances in  $K^*N$ ),  $\Pi$  accounts for  $K^*$  mass shift
- We have unitarised the interaction matrix using the Bethe-Salpeter equation

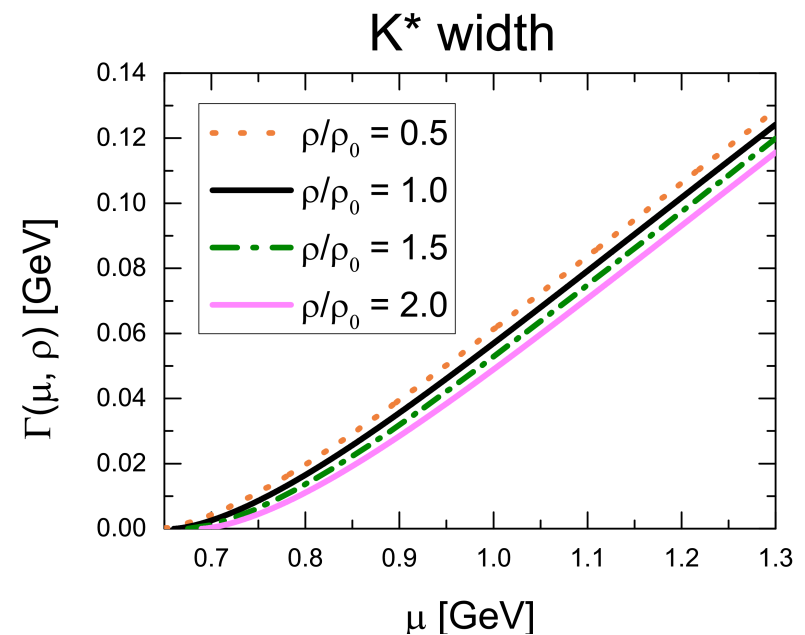
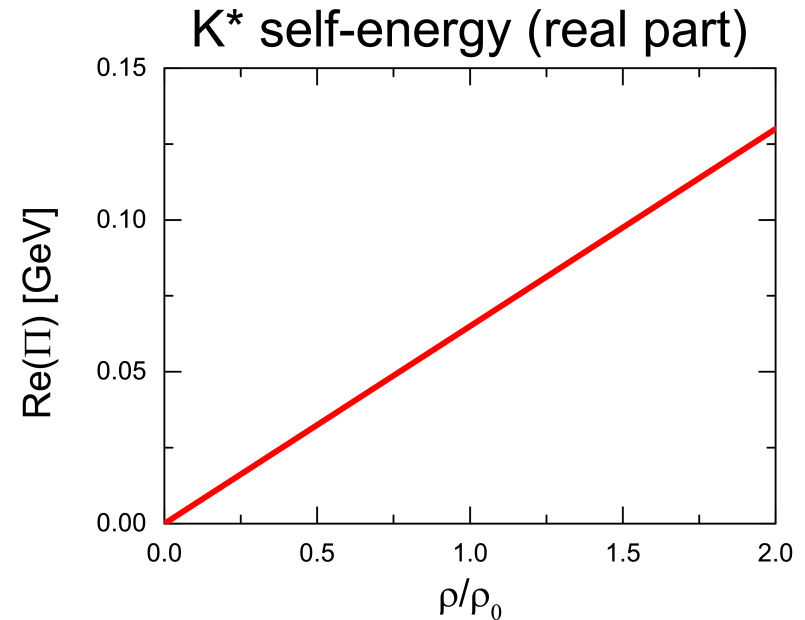
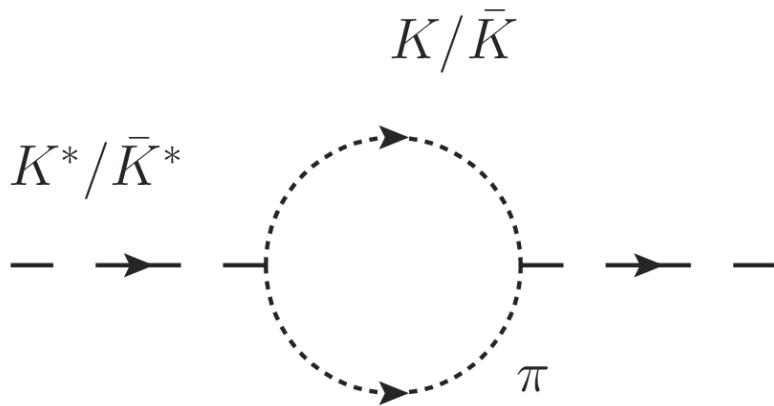
$$T = V/(1 - VG)$$





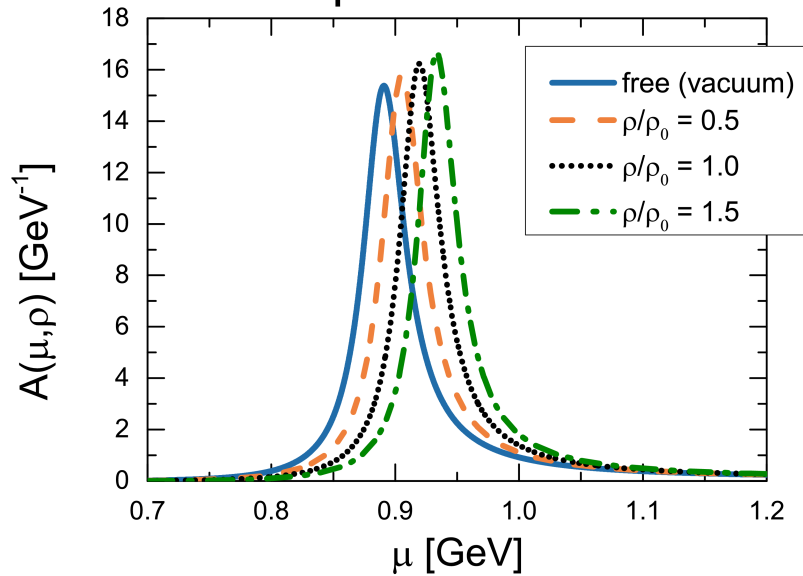
# Dense matter: $K^*$ s

- Real part obtained from self-energy expression (previous slide)
- Width of  $K^*$  self-energy calculated through in-medium modification via  $K^* \rightarrow K \pi$
- Width changes moderately (decreases)

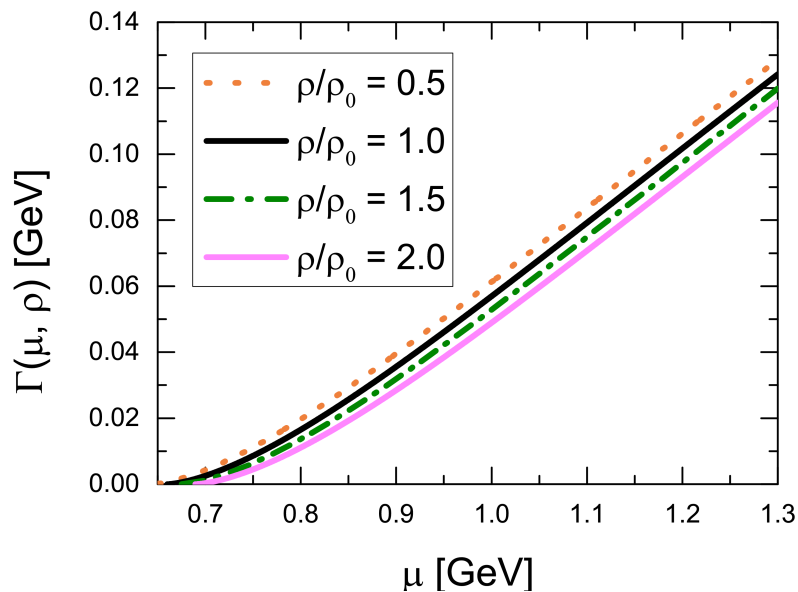


# Dense matter: $K^*$ s

$K^*$  spectral function



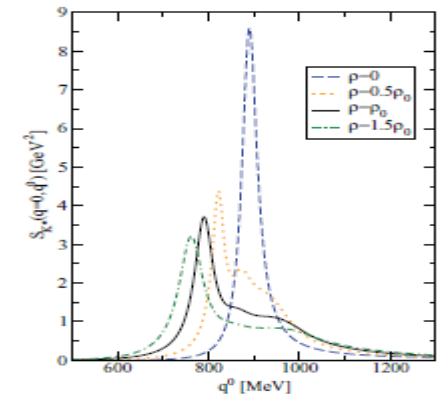
$K^*$  width



- $K^*$  experiences repulsive medium, spectral function shifted to higher masses
- As density increases  $\rightarrow K^*$  width is actually lower due to the heavier Kaon in  $K^* \rightarrow K\pi$
- The two effects compensate: shape of  $K^*$  spectral function practically unchanged

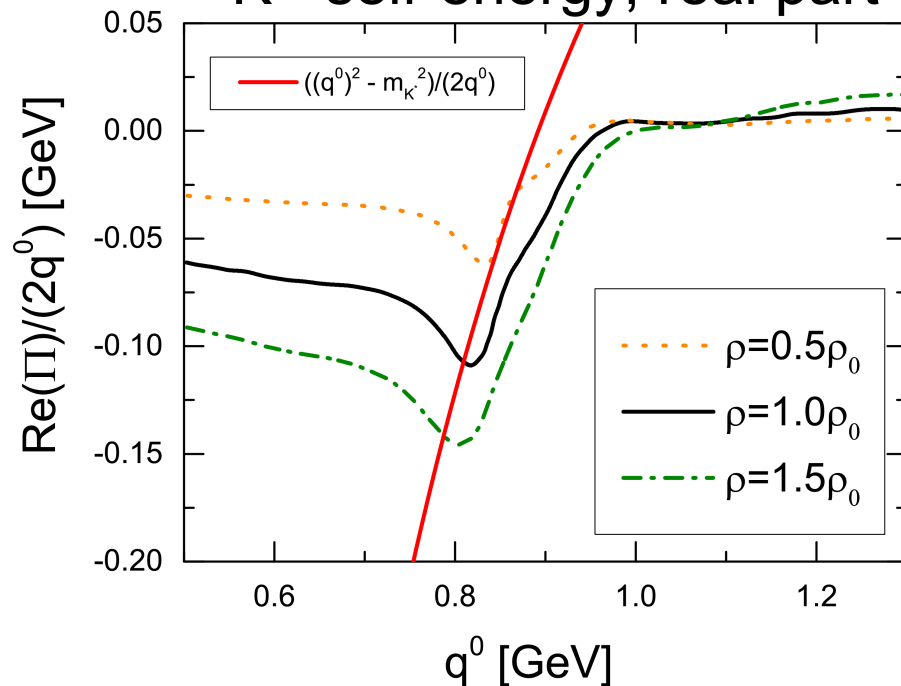
# Dense matter: anti-K\*s

- **anti-K\* N**: dynamics ruled by S=-1 resonances (as for anti-K) → complicated *many-body structure* and *E-dependence* of self-energy
- Parametrise full G-matrix calculation [Tolos et al PRC87 (2010)]
  - 1. Solve dispersion relation: quasi-particle energy  $\omega_{K^*}$
  - 2. Use  $\omega_{K^*}$  to find width:  $\Gamma_{K^*} = \text{Im } \Pi_{K^*} / \omega_{K^*}$

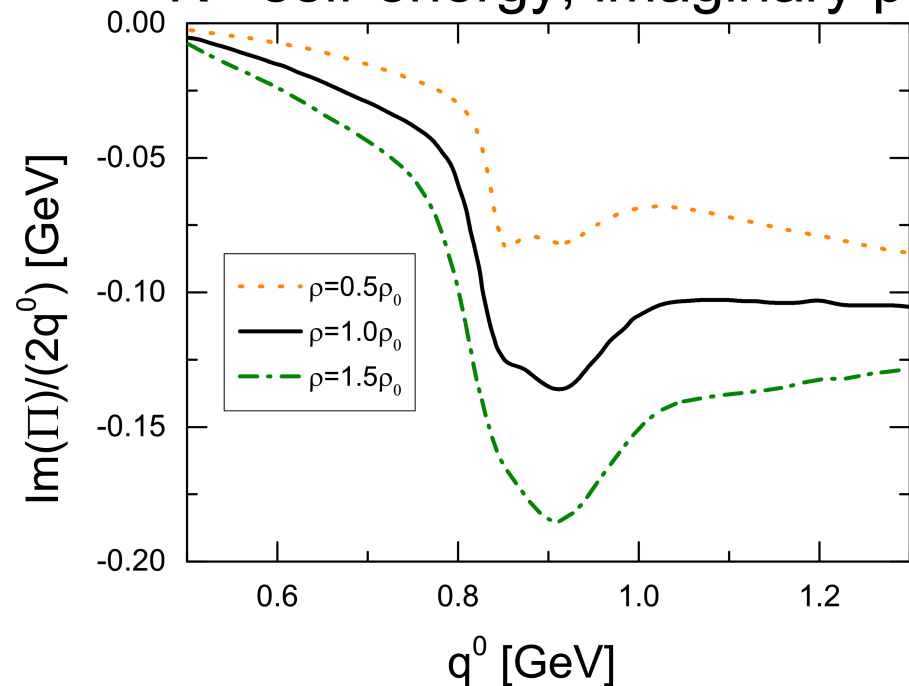


Tolos et al., PRC 82 (2010) 045210

K\*- self-energy, real part

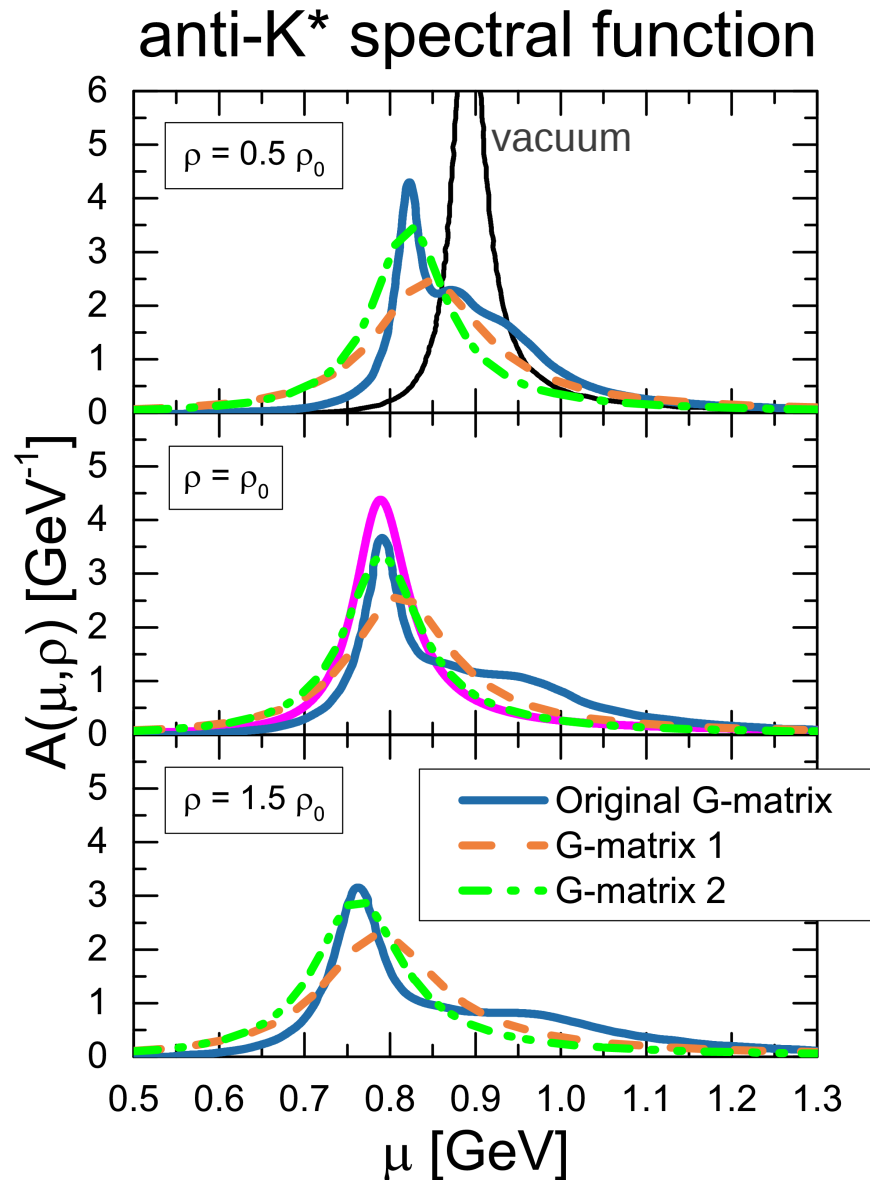


K\*- self-energy, imaginary part



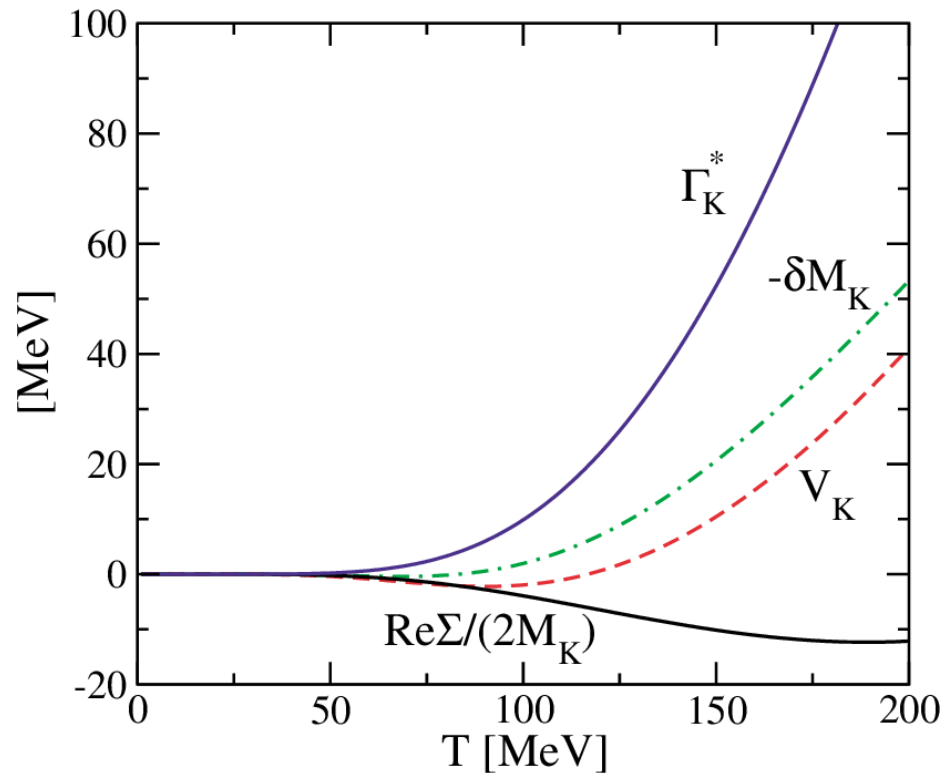
# Dense matter: anti-K\*s

- Blue: Original G-matrix calculation
- Orange: Breit-Wigner spectral function
- Green: Breit-Wigner spectral function with corrected mass shift
- Middle plot: Magenta line denotes evaluation of  $K\pi$  width with in-medium kaons
- Breit-Wigner does not retain multi-pole structure and overestimates the strength at low energies, but *keeps essential features*



# Hot matter: kaons

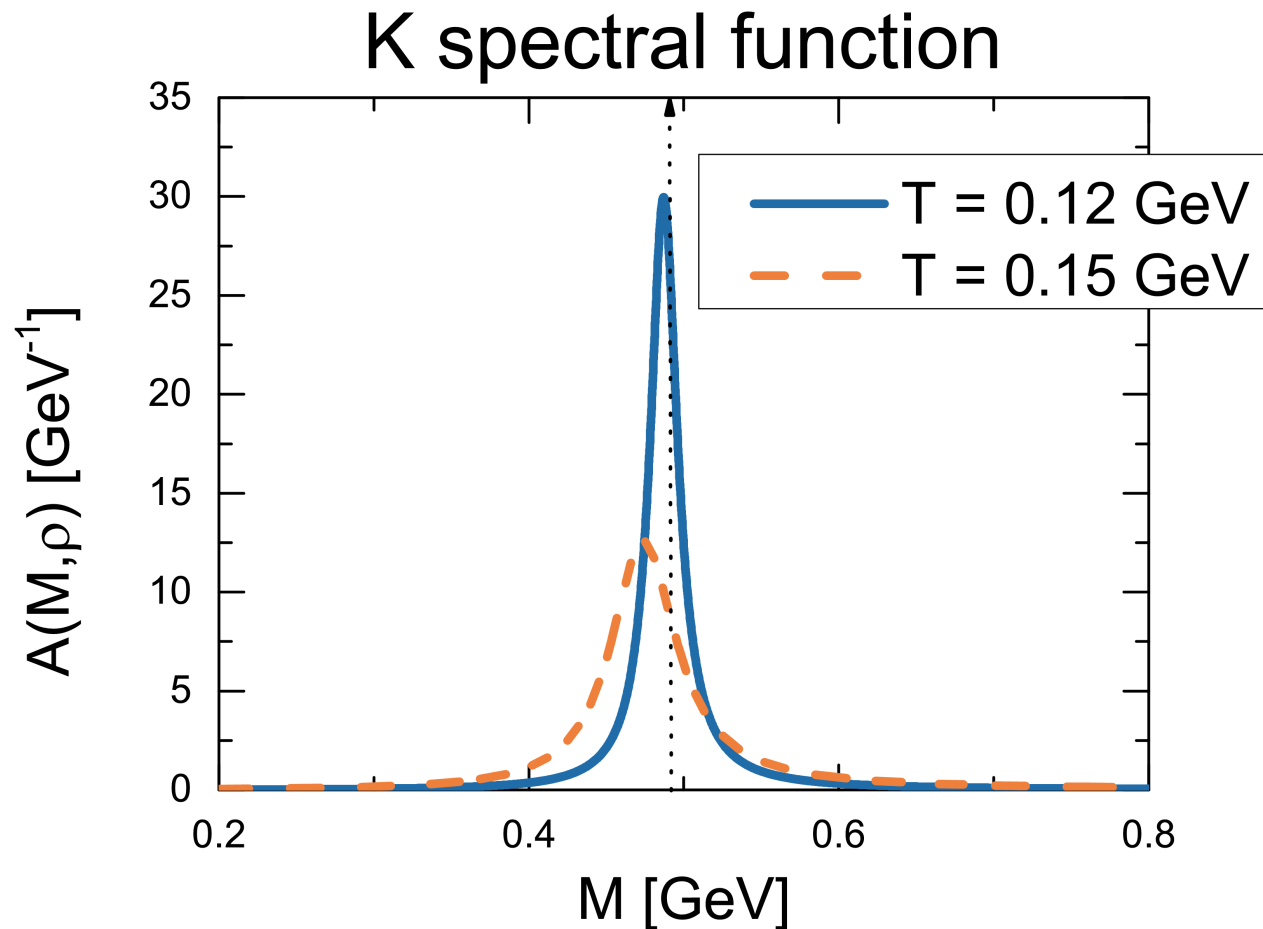
- Consider hot, isotopically symmetric gas of pions:  $K^*$  and anti- $K^*$  identical
- Medium effects tied to  $K^* \rightarrow K \pi$  decay mode
- **K in hot pion gas**: evaluated by Martemyanov *et al.* in meson-meson ChPT + phenomenological extension for higher energies
- (pions considered stable)



The quantities of interest in this case are the width  $\Gamma_{K^*}$  and the mass shift  $\delta M_K$  to build the  $K^*$  selfenergy

# Hot matter: kaons

- Use Breit-Wigner to construct K spectral function at different temperatures

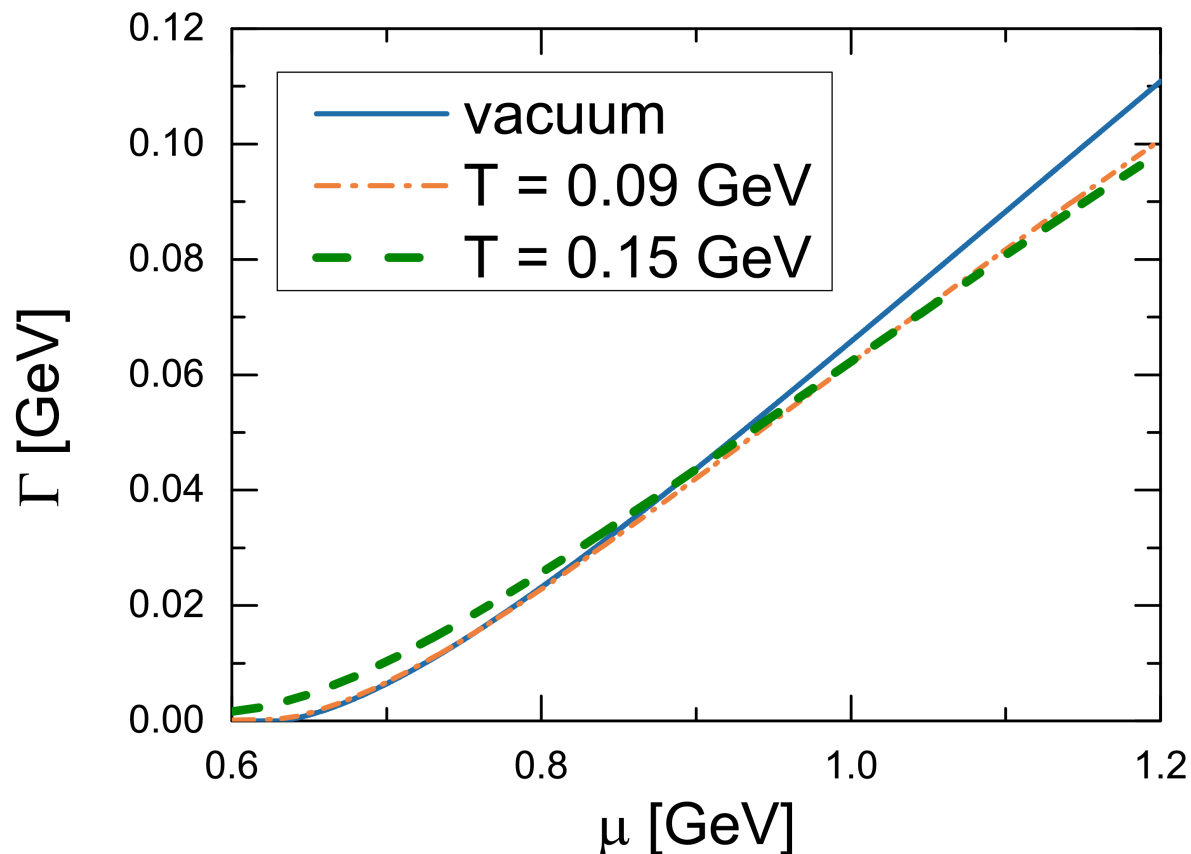


# Hot matter: $K^*$ s

- Use K spectral function to obtain  $K^*$  width

$$\Gamma_{K^*}(\mu, \rho) = \Gamma_0 \left( \frac{\mu_0}{\mu} \right)^2 \cdot \frac{\int_{M_{min}}^{\mu - m_\pi} A_K(M, \rho) \cdot q(\mu, M)^3 dM}{\int_{M_{min}}^{\mu_0 - m_\pi} A_K(M, 0) \cdot q(\mu_0, M)^3 dM}$$

## $K^*$ in-medium width



# Hot matter: K\*s

- Use dispersion relation to calculate the real part using the imaginary part of the self-energy!

$$\Re(\Pi(\mu)) - \Re(\Pi_{vac}(\mu)) = -\frac{2}{\pi} \int_{m_\pi}^{\infty} \frac{\mu'}{\mu'^2 - \mu^2} [\Gamma^{dec}(\mu', T) - \Gamma^{vac}(\mu')] d\mu'$$

- Unfortunately the emerging integral is divergent
- Use phenomenological form factor in  $K^* \rightarrow K \pi$  vertex to regularise integral

$$F(\Lambda, \mu) = \left( \frac{\Lambda^2 + q(\mu_0, M_0)^2}{\Lambda^2 + q(\mu, M)^2} \right)^2$$

*M*: off-shell mass of the K  
*μ*: off-shell mass of the K\*  
*μ*<sub>0</sub>: pole mass of the K  
*M*<sub>0</sub>: pole mass of the K\*

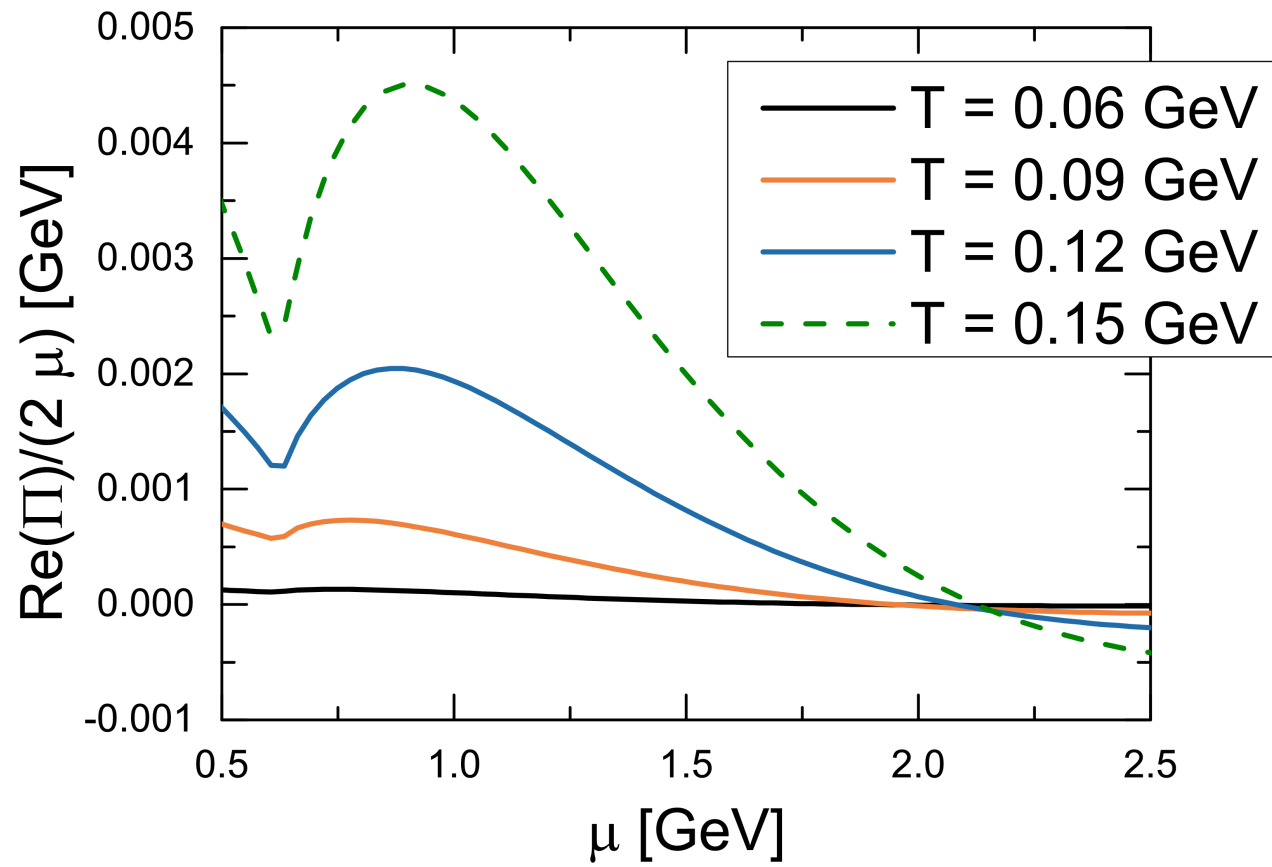
$$q(\mu, M) = \frac{\sqrt{\lambda(\mu, M, m_\pi)}}{2\mu}$$

$$q(\mu_0, M) = \frac{\sqrt{\lambda(\mu_0, M, m_\pi)}}{2\mu_0}$$



# Hot matter: $K^*$ s

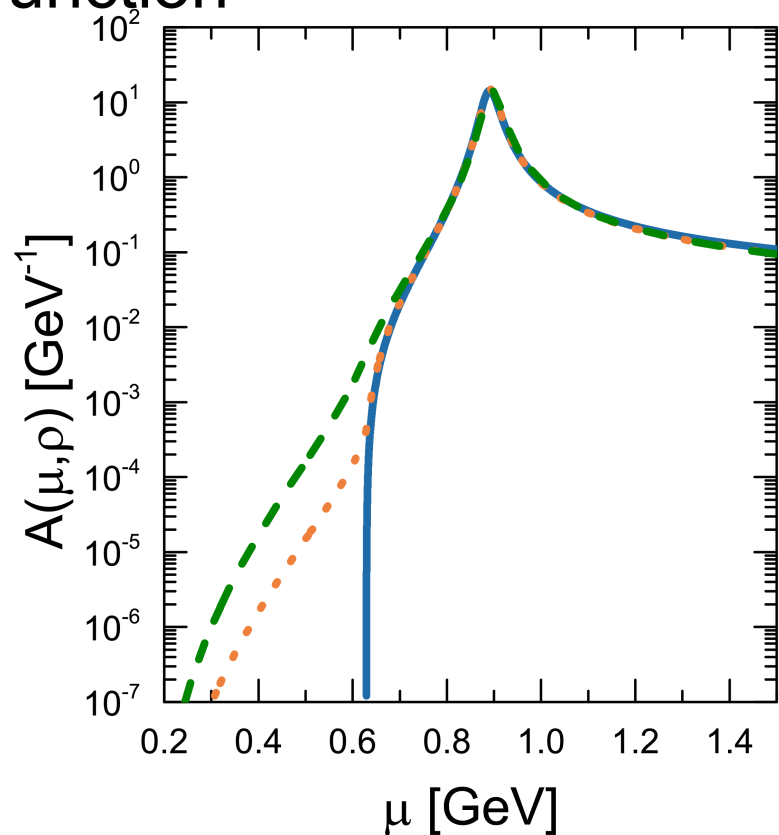
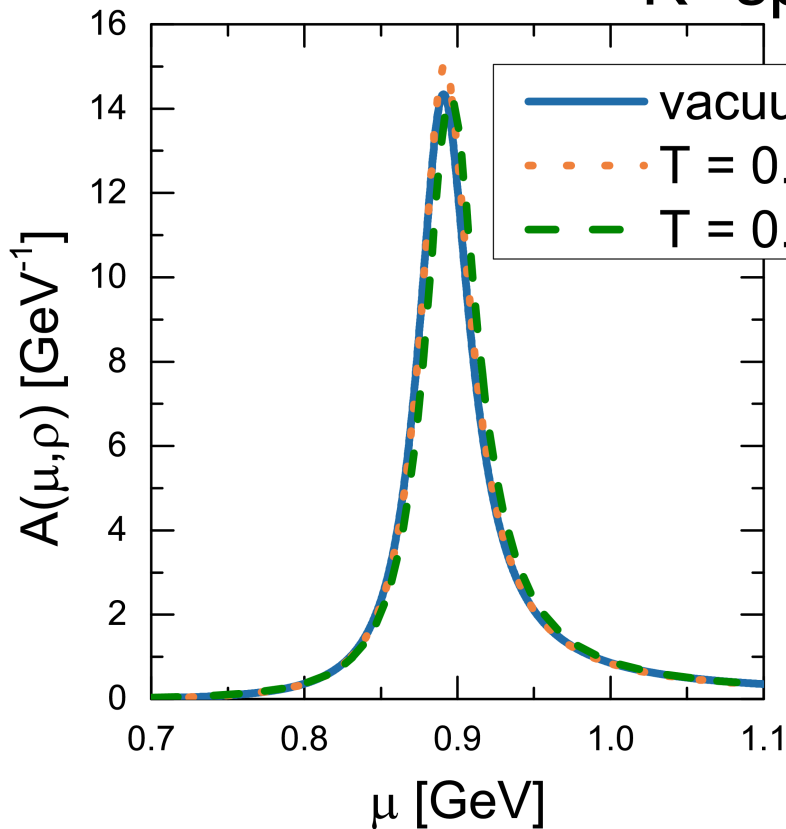
- This results in the following real part of the self-energy ( $\leftrightarrow$  mass shift)  
*(repulsive and VERY small)*



# Hot matter: $K^*$ s

- We obtain the following spectral function (for different temperatures)
- Spectral function is fairly stationary with respect to temperature
- Barely any broadening at the  $qp$  peak (some strength below threshold)

$K^*$  spectral function



# Summary and outlook

- The in-medium properties and the behaviour of the strange mesons  $K$ , anti- $K$ ,  $K^*$  and anti- $K^*$  bar in a hot, pionic and dense, baryonic nuclear medium have been studied within a Breit-Wigner parametrisation of the spectral function.
- In dense nuclear matter, the  $S=+1$  mesons keep their vacuum structure, and can be easily cast in BW form with mild changes in their masses and widths.
- In the  $S=-1$  sector, only an approximate (“average”) description of the spectral function is achieved, retaining essential features as attractive potential and broadening.
- A new contribution for the  $K^*$  self-energy in dense matter was calculated in ChPT, leading to a positive mass shift 40 MeV at normal matter density.
- In hot hadronic matter, the  $K^*$  experiences a mild broadening and negligible mass shift only at very high temperatures, from changes in the kaon spectral function.
- These results can now be implemented into transport models and used in simulations to get more realistic behaviour for strange particles in HICs.

# The end.

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Thank you for your attention.