

# Recent developments for open heavy flavor observables in URHIC

*NED & TURIC network-workshop*

*Hersonissos (Crete - Greece); 9-14 June 2013*

**P.B. Gossiaux**

SUBATECH, UMR 6457

Université de Nantes, Ecole des Mines de Nantes, IN2P3/CNRS

collaborators

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**J. Aichelin, ...**

# Recent developments for open heavy flavor observables in URHIC



Unknown work on right-handed neutrino physics ?

J. Aichelin, ...

# Recent developments for open heavy flavor observables in URHIC



For sure, famous for his works on strange quarks (& exotic pull-overs)...

J. Aichelin, ...

# Recent developments for open heavy flavor observables in URHIC



But mostly known (to me) for his physics on charm

J. Aichelin, ...

# Recent (*and not so recent*) developments for open heavy flavor observables in URHIC

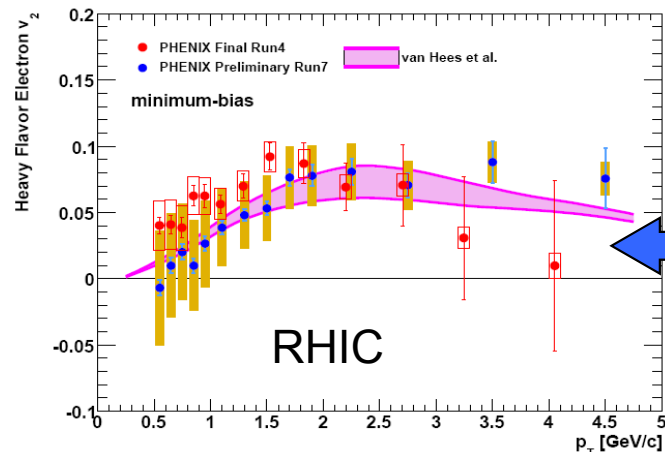


But mostly known (to me) for his physics on charm

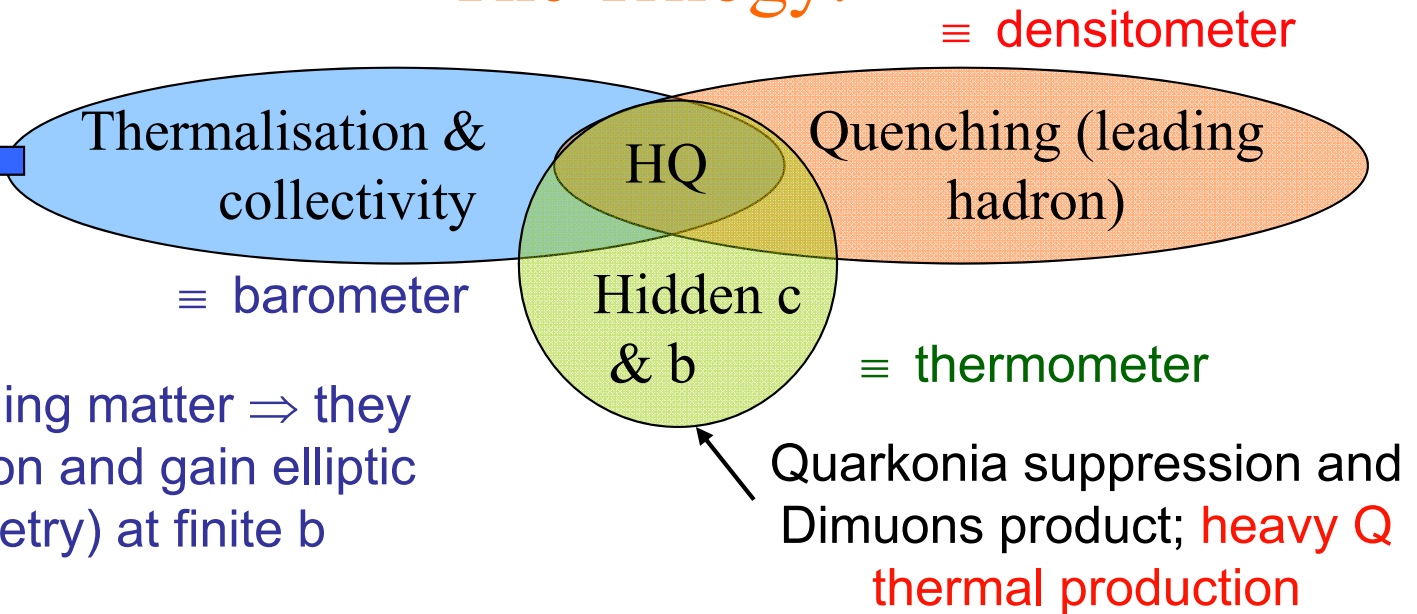
J. Aichelin, ...

# Why *open* heavy flavors in A-A ?

- Those are for sure sensitive to the early stages
- Much simpler than quarkonia and also sensitive to the medium properties ( $t_{\text{equil}} \propto M_Q/T^2 \Rightarrow$  clear hierarchy for s, c and b).
- Mandatory to understand Q-Qbar evolution in QGP & quarkonia production.



## The Trilogy:



HQ are imbedded in expanding matter  $\Rightarrow$  they participate to collective motion and gain elliptic flow ( $v_2$ : azimuthal asymmetry) at finite b

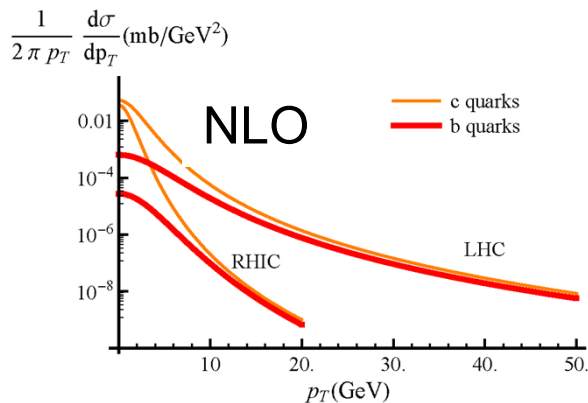
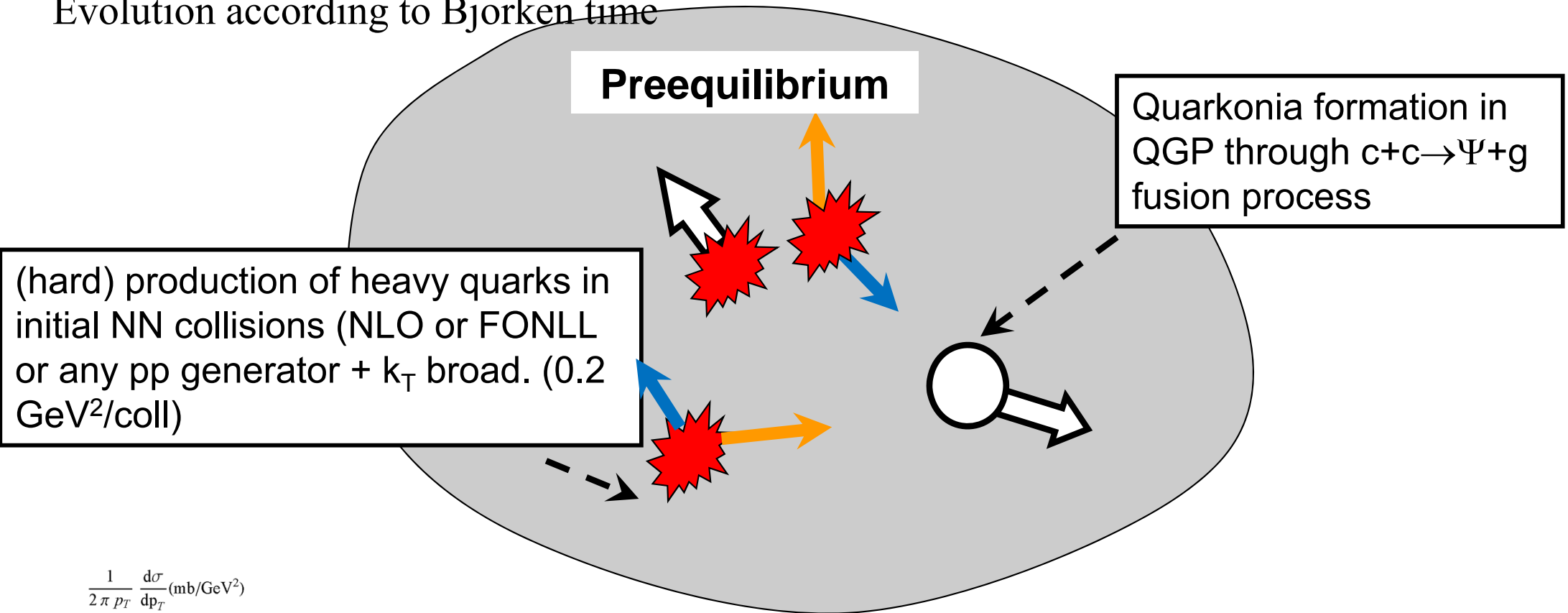
## Challenges:

- Description of HQ E-loss / equilibration from fundamental theory
- Joint  $v_2$ - $R_{AA}$  explanation could help to better constrain free parameters...

# The Monte Carlo @ Heavy Quark Generator

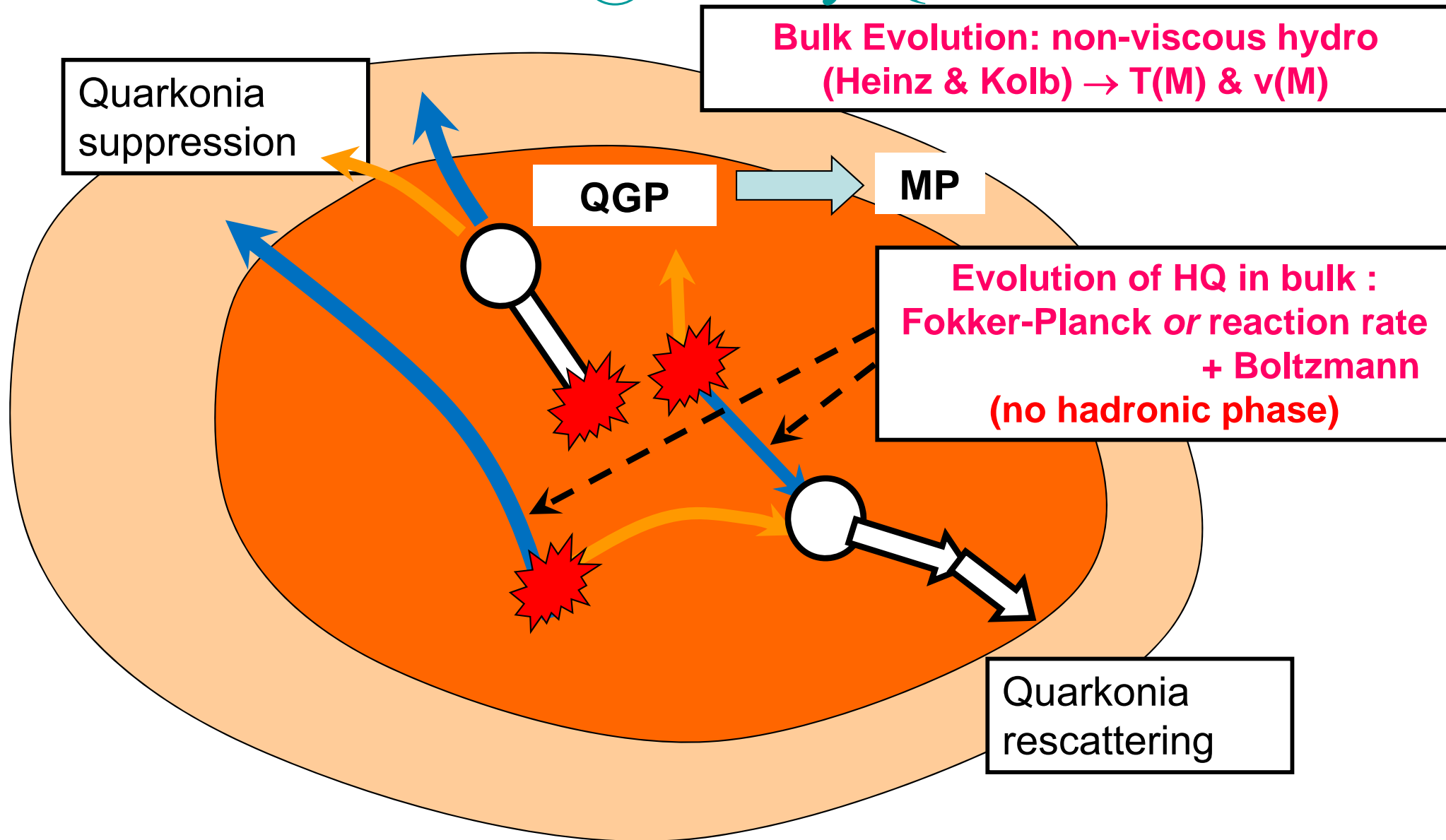
No force on HQ before thermalization of QGP (0.6 fm/c)

Evolution according to Bjorken time





# The Monte Carlo @ Heavy Quark Generator



Recently : coupling to EPOS instead of KH: some point still to be solved

# The Monte Carlo @ Heavy Quark Generator

**Bulk Evolution: non-viscous hydro  
(Heinz & Kolb)  $\rightarrow T(M)$  &  $v(M)$**

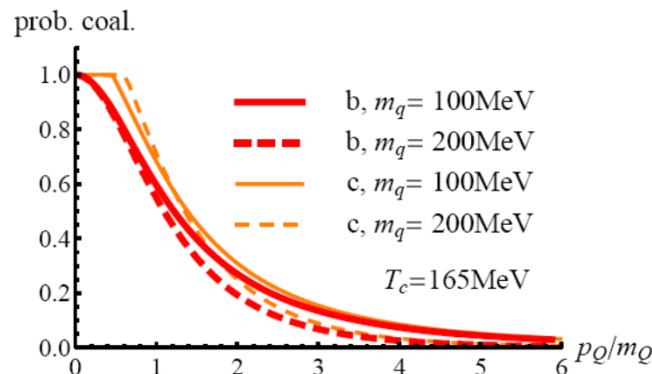
**QGP**

**MP**

**HG**

**Evolution of HQ in bulk :  
Fokker-Planck or reaction rate  
+ Boltzmann  
(no hadronic phase)**

**D/B formation at the  
boundary of QGP (or MP)  
through coalescence of c/b  
and light quark (low  $p_T$ ) or  
fragmentation (high  $p_T$ )**



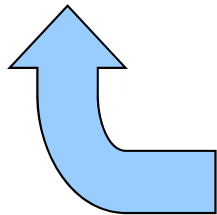
**Nothing spectacular at freeze-out  
(quarkonia are white objects already)**

# Setting the scene: E-Loss and thermalization

$$(init) P_T \approx m_Q$$

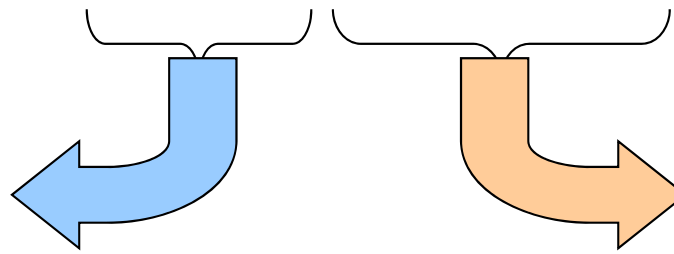
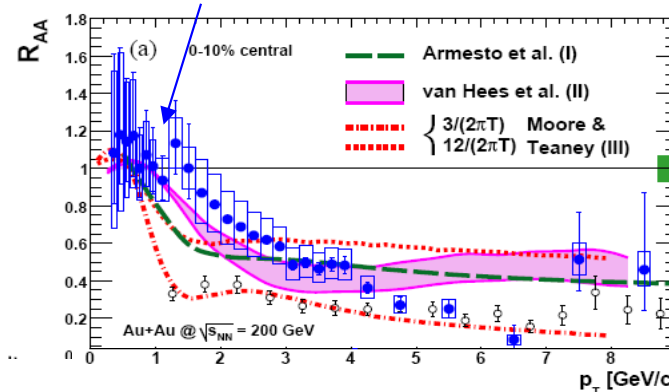
- Bulk part of Q production
- E gain becomes probable
- HQ scatter and can thermalize with the medium
- very  $\neq$  from light quarks
- *Dominated by collisional processes*
- Non perturbative effect (small momentum transfert, coalescence with light quark)
- 1 dominant parameter:  $D_s$

(Langevin Transport)



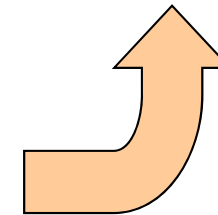
... but one should however avoid to mix those two worlds !!!

Phenix data (hep-ex 0611018)



$$(init) P_T \gg m_Q$$

- Rare processes
- Mostly E loss
- HQ go on nearly straight lines and probe the opacity of matter. Little thermalization
- *~ light quarks*
- *Coherent radiative + collisional processes*
- Good test of pQCD... Theory at work (a priori)
- Several transport coefficients implied ( $dE/dx$ ,  $B_T, \dots$ )



# The early times... (2004-2006)

Charmonia enhancement in QGP with improved description of c-quarks phase-distribution

SQM04

P.-B. Gossiaux (with V. Guiho & J. Aichelin)

2 extreme cases considered in early 2000's:

- PBM, Stachel, Andronic: SHM (c-quarks fully thermalized)
- Thews & Rafelski: "dynamical" coalescence with  $f(c)$  from PDF (no thermalization at all)

I) c-quarks in QGP

- Model
- ~~Results~~ Preliminary

II) J/Psi's in QGP

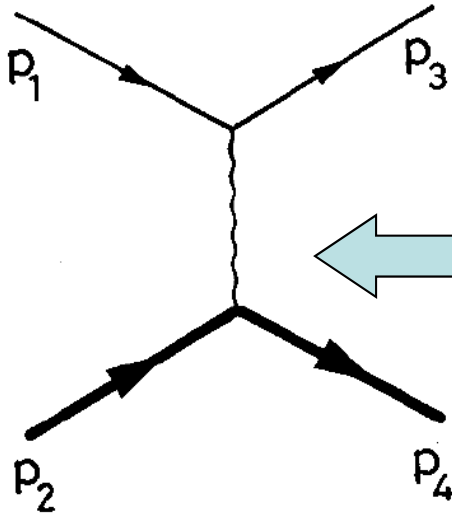
- Model
- ~~Results~~ Preliminary

III) Conclusion & Perspectives

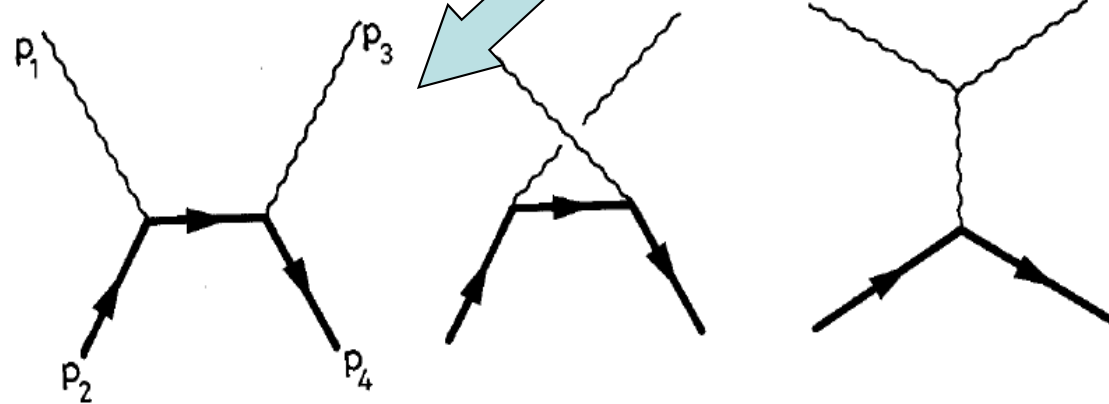
SQM 2004

# Cross sections

Starting from Cambridge (79) as a basis:



$$\Sigma |m|^2 = \frac{64\pi^2 \alpha^2(Q^2)}{9} \frac{(M^2 - u)^2 + (s - M^2)^2 + 2M^2 t}{t^2}$$



$$\Sigma |m|^2 = \pi^2 \alpha^2(Q^2) \left[ \frac{32(s - M^2)(M^2 - u)}{t^2} + \frac{64}{9} \frac{(s - M^2)(M^2 - u) + 2M^2(s + M^2)}{(s - M^2)^2} \right. \\ \left. + \frac{64}{9} \frac{(s - M^2)(M^2 - u) + 2M^2(M^2 + u)}{(M^2 - u)^2} + \frac{16}{9} \frac{M^2(4M^2 - t)}{(s - M^2)(M^2 - u)} \right. \\ \left. + 16 \frac{(s - M^2)(M^2 - u) + M^2(s - u)}{t(s - M^2)} - 16 \frac{(s - M^2)(M^2 - u) - M^2(s - u)}{t(M^2 - u)} \right]$$

However, t-channel is IR divergent  
 $\Rightarrow$  models

$$\frac{1}{t} \rightarrow \frac{1}{t - \mu^2(T)}$$

Naïve pQCD (f.i. Svetitsky 89)

# The early times... (2004-2006)

C quarks in QGP (or in strongly interacting matter)

SQM 2004

- Starting point: c quarks behave according to Brownian motion (cf. D. Molnar) / Langevin forces  $\Leftrightarrow$  c quarks distribution evolves according to Fokker – Planck equation

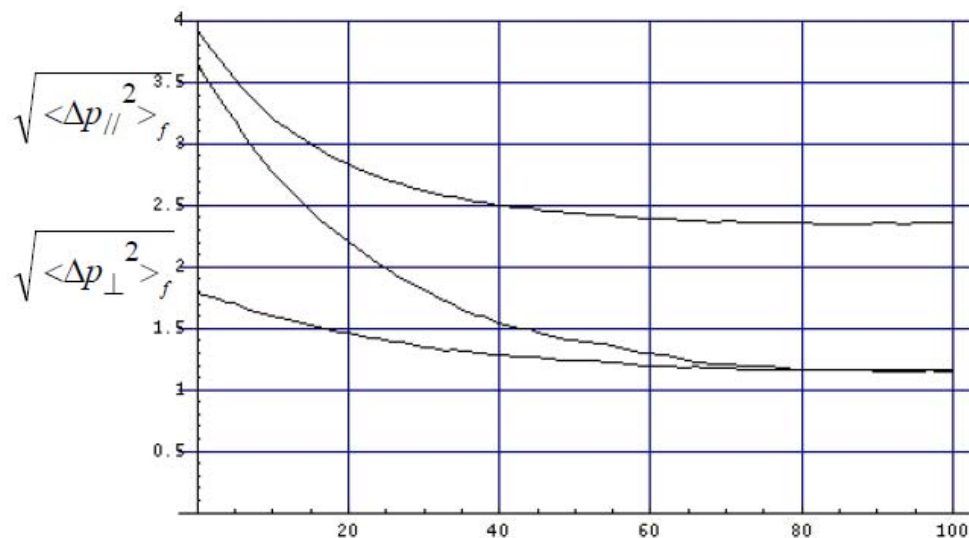
$$\frac{\partial f}{\partial t} = \vec{\nabla}_p \left[ \vec{A} f + \vec{\nabla}_p \left( \vec{B} f \right) \right]$$

- Relaxation time  $\gg$  collision time ; at large momentum (as for all quarks) **but** also at low momentum (thanks to inertia)
- Why not Boltzmann equation ? One first answer: not efficient.

# The early times... (2004-2006)

SQM 2004

## First results on c-quark evolution



Relaxation of  $\langle E \rangle$ , of  $\sqrt{\langle \Delta p_{\perp}^2 \rangle_f}$  and of  $\sqrt{\langle \Delta p_{\parallel}^2 \rangle_f}$  for c-quarks produced in 200 GeV p-p collisions ( $\Delta y=2$ ).

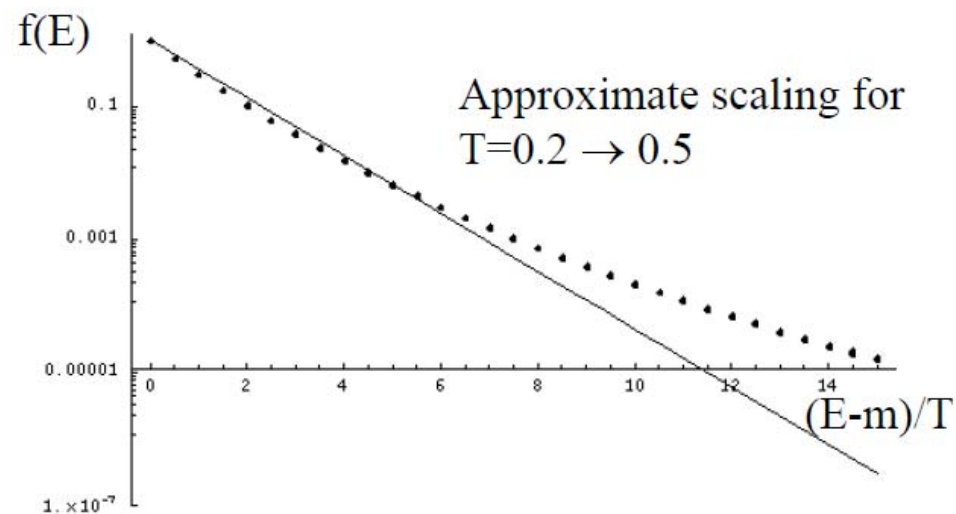
Evolution in a  $\mu=0$  --  $T=400$  MeV QGP.

Once again : **long relaxation times**

Asymptotic energy distribution: no Boltzmann; more like a Tsallis

Walton & Rafelski (1999)

Too much diffusion at large p





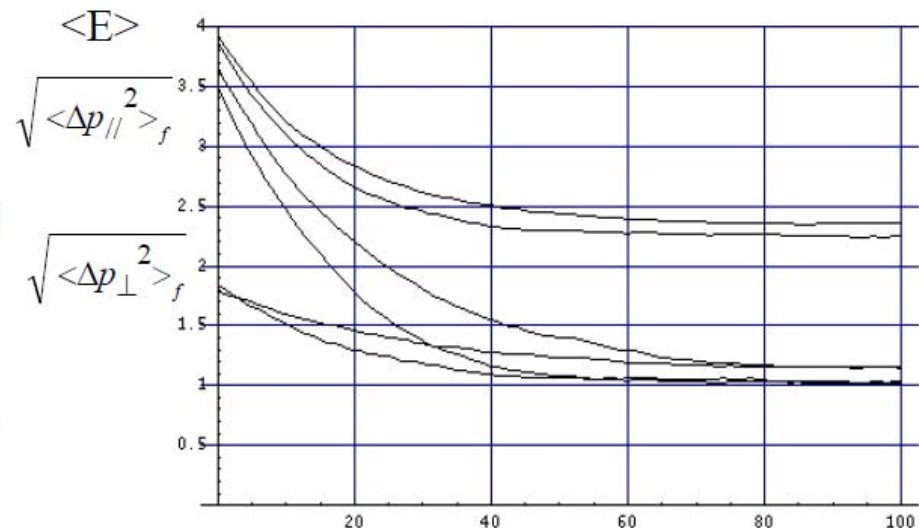
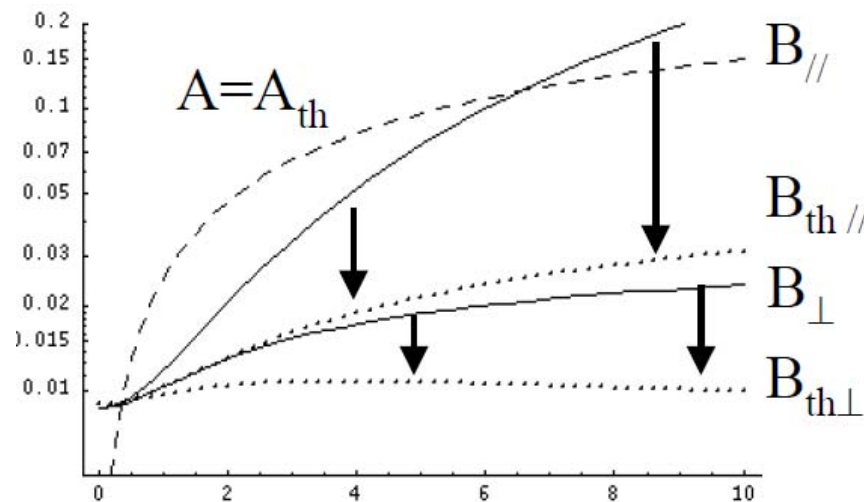
# The early times... (2004-2006)

SQM 2004

So what do we do ???

Two sets:

1. FP coefficients deduced by Mustafa, Pal and Srivastava
2. Adapt  $(A,B) \rightarrow (A_{th}=A, B_{th})$  such then the associated  $f_{asympt}$  is a Boltzmann distribution, and then  $\rightarrow (\kappa A, \kappa B_{th})$  with  $\kappa$  varying from  $0 \rightarrow \infty$  in order to span from free streaming  $\rightarrow$  instantaneous thermalization.

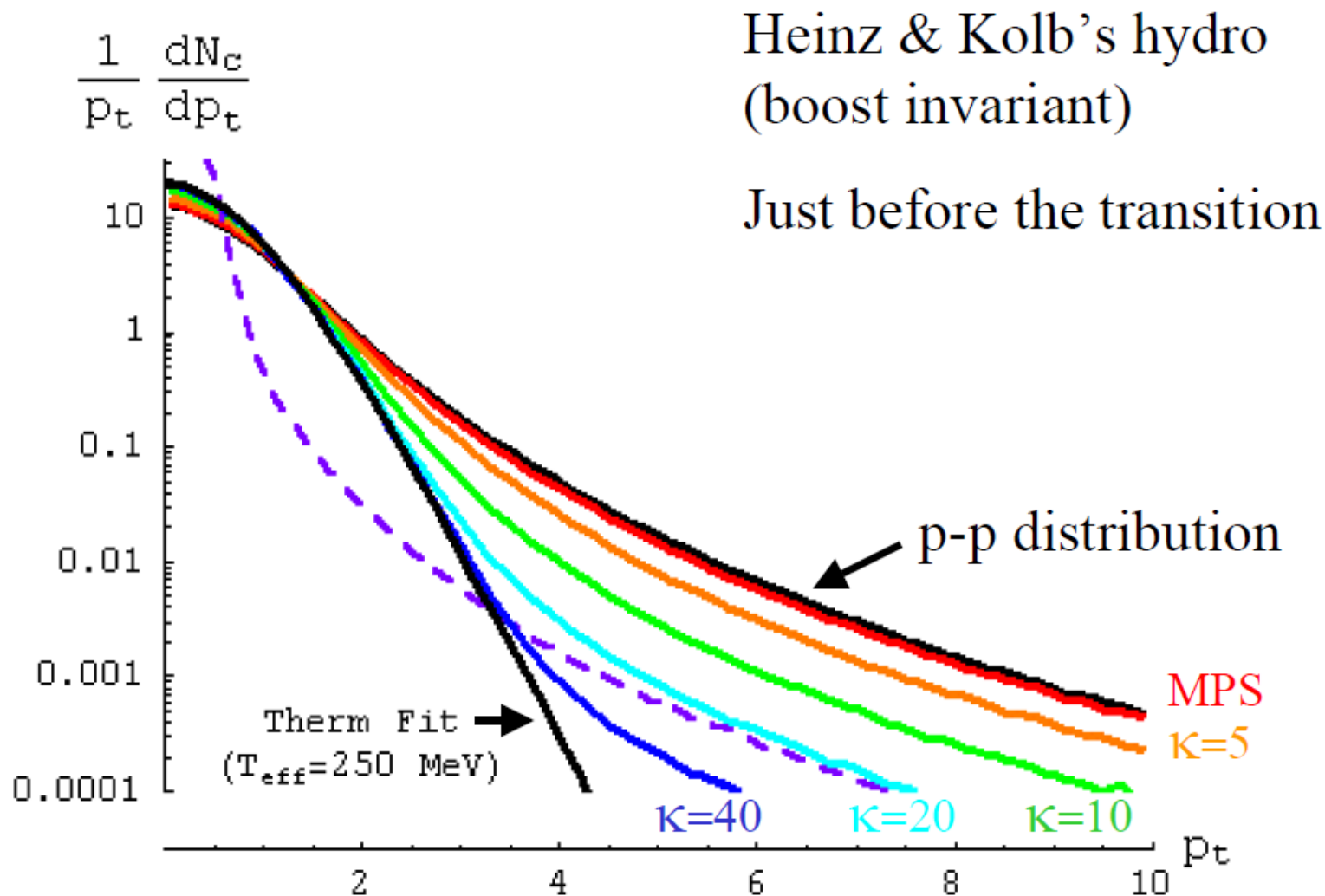




# The early times... (2004-2006)

SQM 2004

c-quarks transverse momentum distribution ( $y=0$ )



# The early times... (2004-2006)

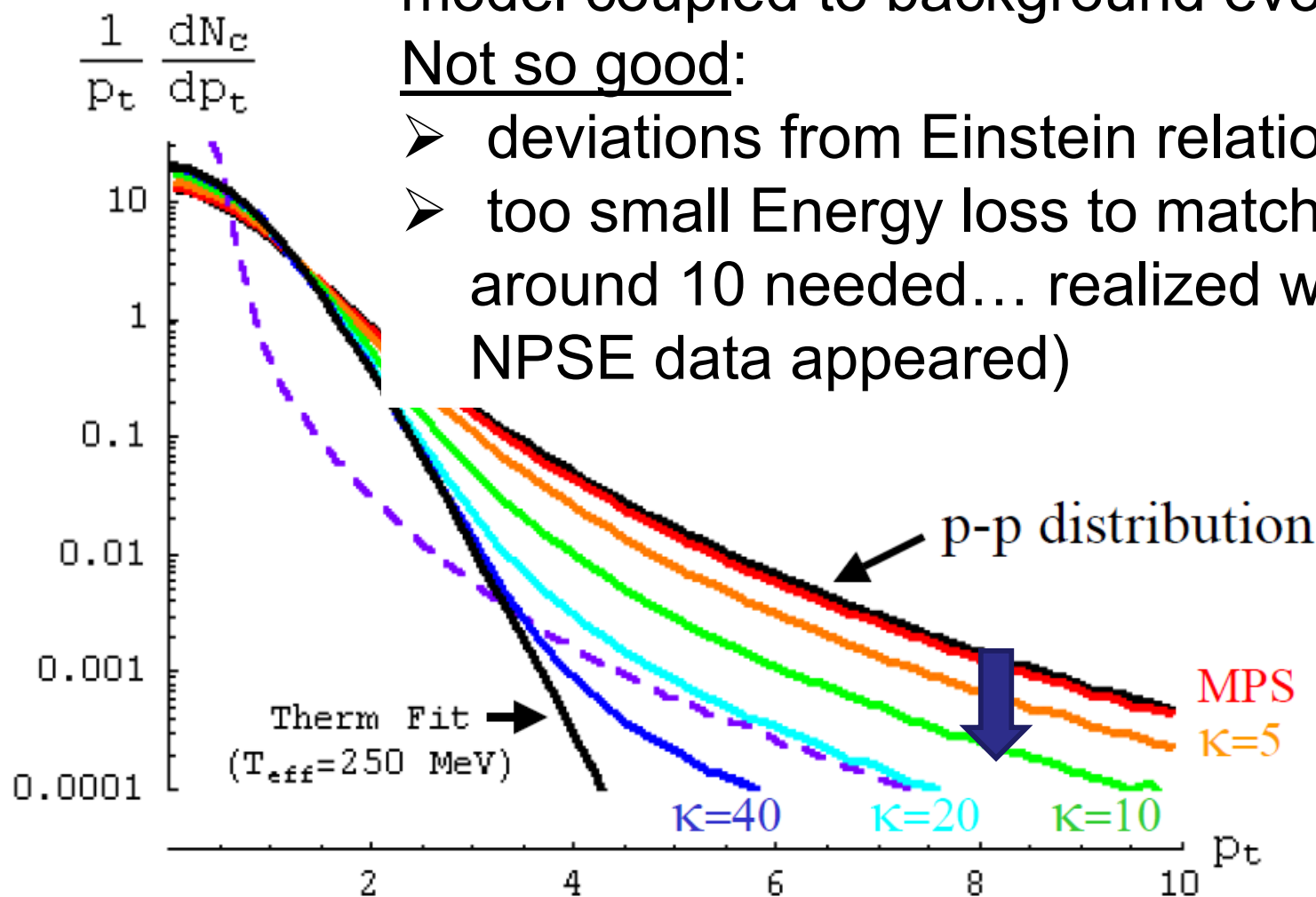
SQM 2004

c-quarks transverse momentum distribution ( $y=0$ )

Good thing: one of the first HQ transport model coupled to background evolution.

Not so good:

- deviations from Einstein relation at large  $p_t$
- too small Energy loss to match the data (K around 10 needed... realized when RHIC NPSE data appeared)



## Naïve regulating of IR divergence:

$$\frac{1}{t} \longrightarrow \frac{1}{t - \mu^2} \quad \text{With } \mu(T) \text{ or } \mu(t)$$

### Models A/B: 2 customary choices

$$\mu^2(T) = m_D^2 = 4\pi\alpha_s(1+3/6)T^2$$

$$\alpha_s(Q^2) \rightarrow \begin{cases} 0.3 \text{ (mod A)} \\ \alpha_s(2\pi T) \text{ (mod B)} (\approx 0.3) \end{cases}$$

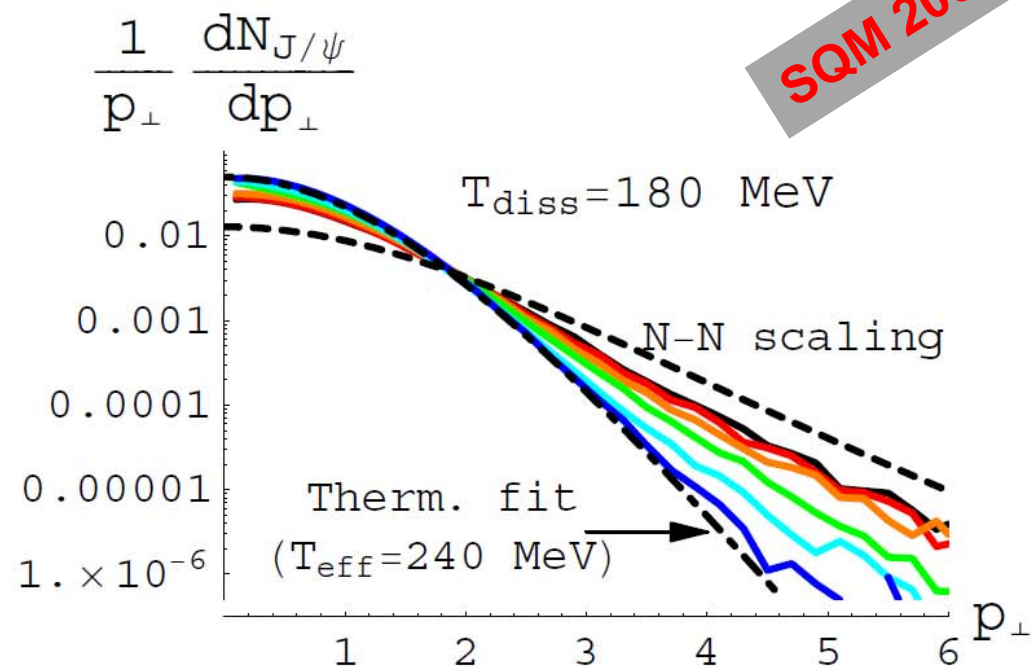
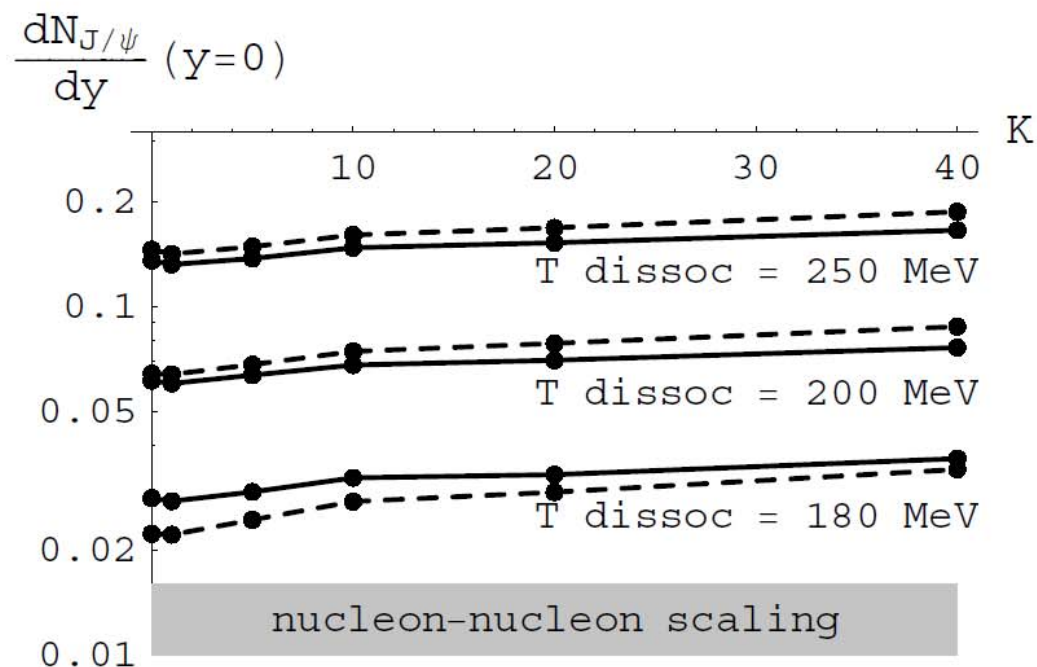
$\frac{dE_{coll}(c)}{dx}$

T(MeV) \ p(GeV/c)	10	20
200	0.18	0.27
400	0.35	0.54

... of the order of a few % !

# The early times... (2004-2006)

Journal of Physics G: Nucl. Part. Phys. **31** (2005) S1079



Despite the caviats: first study of the influence of the c-quark distribution on the number of  $J/\psi$  produced through coalescence + transverse momentum distribution (effective cooling, later on confirmed by RHIC)

2007: our Langevin → Boltzmann « transition » (with A. Peshier)

## Heavy quarks in QGP

SQM 2008

In pQGP, heavy quarks are assumed to interact with partons of type "i" (massless quarks and gluons) with local 2→2 **rate**:

$$R_i = \frac{1}{2E_p} \int \frac{d^3k}{(2\pi)^3 2k} \int \frac{d^3k'}{(2\pi)^3 2k'} \int \frac{d^3p'}{(2\pi)^3 2E'} \\ n_i(k) \times (2\pi)^4 \delta^{(4)}(P+K-P'-K') \sum |\mathcal{M}_i|^2$$

Φ inside

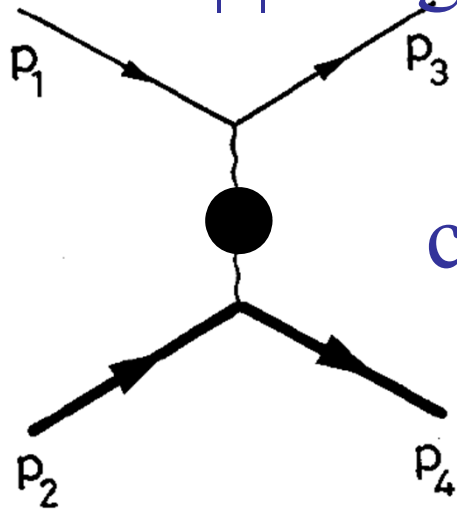
...depends on the QGP macroscopic parameters (T, v, μ) at a given 4-position (t,x). These parameters are extracted from a "standard" hydro-model (Heinz & Kolb: boost invariant)

We follow the hydro evolution of partons and sample the rates  $R_i$  "on the way", performing the  $Qq \rightarrow Q'q'$  &  $Qg \rightarrow Q'g'$  collisions **according to Boltzmann: MC approach**

# Braaten-Thoma:

(Peshier – Peigné)

Low  $|t|$ : large distances



HTL:  
collective  
modes

$$G_{\mu\nu}(Q) = \frac{-\delta_{\mu 0}\delta_{\nu 0}}{q^2 + \Pi_{00}} + \frac{\delta_{ij} - \hat{q}_i\hat{q}_j}{q^2 - \omega^2 + \Pi_T}$$

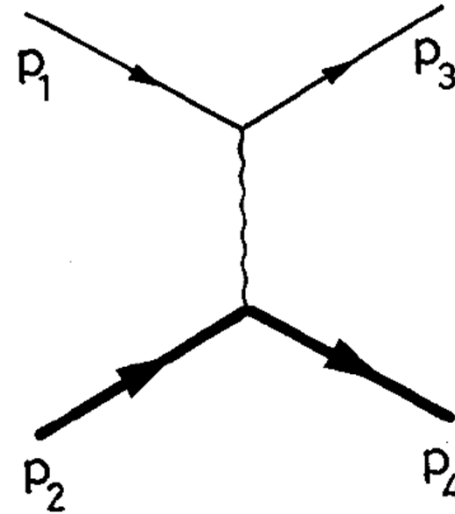
$$\frac{dE_{soft}}{dx} = \frac{2}{3} \alpha m_D^2 \ln\left(\frac{\sqrt{t^*}}{m_D/\sqrt{3}}\right) + \dots$$

**SUM:**  $\frac{dE}{dx} = \frac{2}{3} \alpha m_D^2 \ln\left(\frac{\sqrt{ET}}{m_D/\sqrt{3}}\right)$

HTL: convergent kinetic  
(matching 2 regions)

$|t^*|$

Large  $|t|$ : close coll.



Bare  
propagator

$$G_{\mu\nu}(Q) = \frac{-\delta_{\mu\nu}}{q^2 - \omega^2}$$

$$\frac{dE_{hard}}{dx} = \frac{2}{3} \alpha m_D^2 \ln\left(\frac{\sqrt{ET}}{\sqrt{t^*}}\right) + \dots$$

Indep. of  $|t^*|$  !

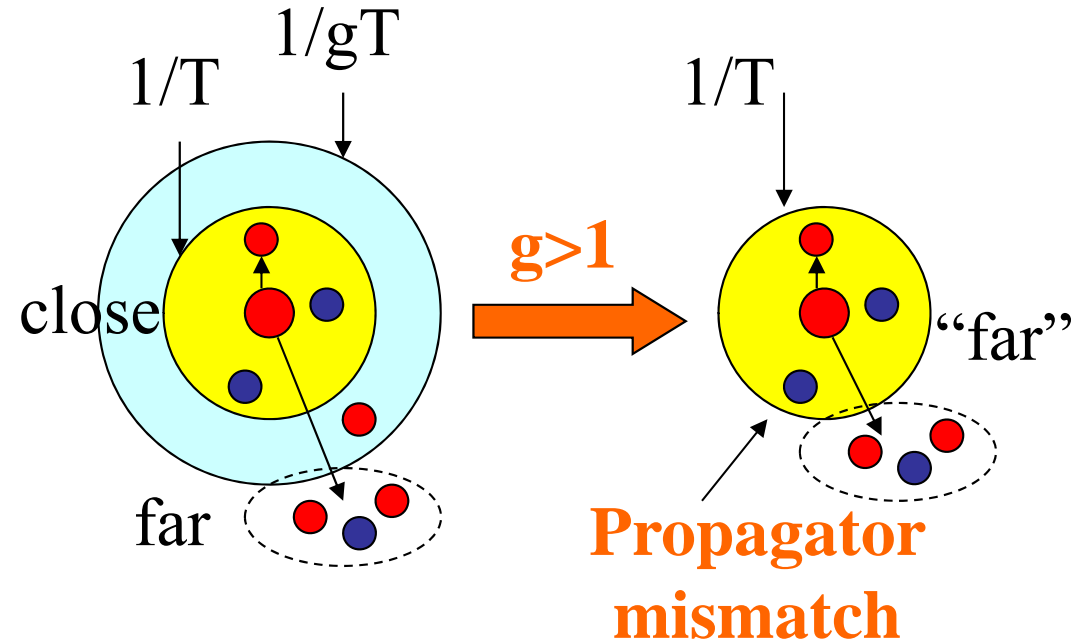
(provided  $g^2 T^2 \ll |t^*| \ll T^2$ )

# HTL at finite (not small) coupling

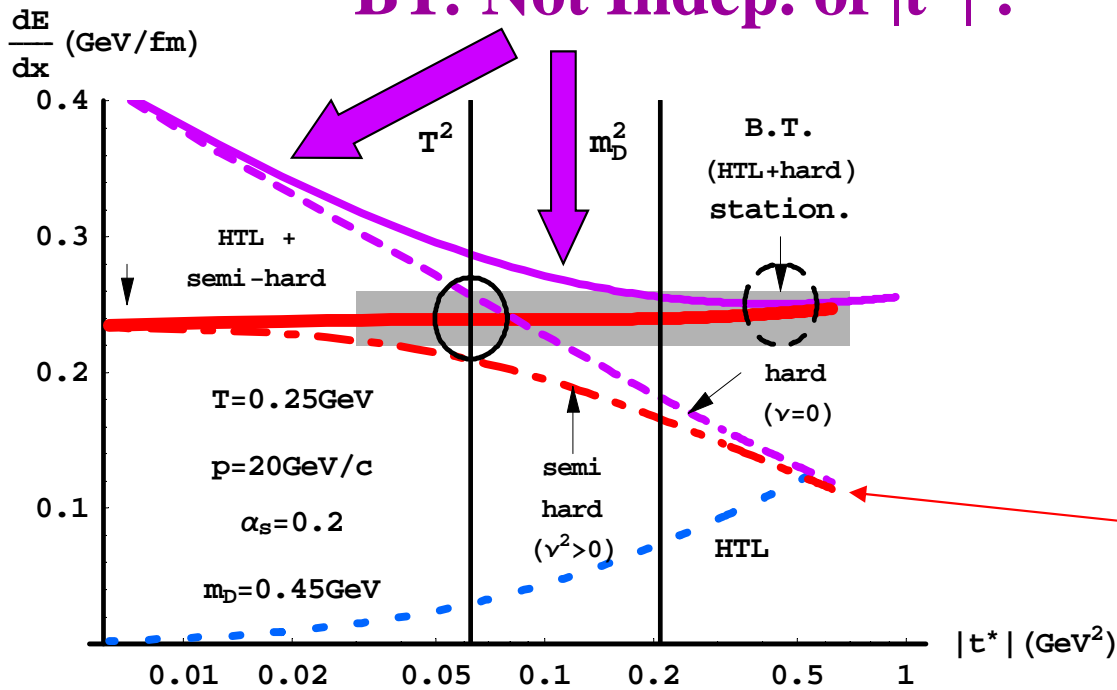


In QGP:  $g^2 T^2 > T^2$  !!!

BT: Not Indep. of  $|t^*|$  !



Our solution: Introduce a **semi-hard propagator**  $1/(t-v^2)$  for  $|t| > |t^*|$  to attenuate the discontinuities at  $t^*$  in BT approach.



**Prescription:**  $v^2$  in the semi-hard prop. is *chosen* such that the resulting E loss is **maximally  $|t^*|$ -independent**.

This allows a matching at a sound value of  $|t^*| \approx T$



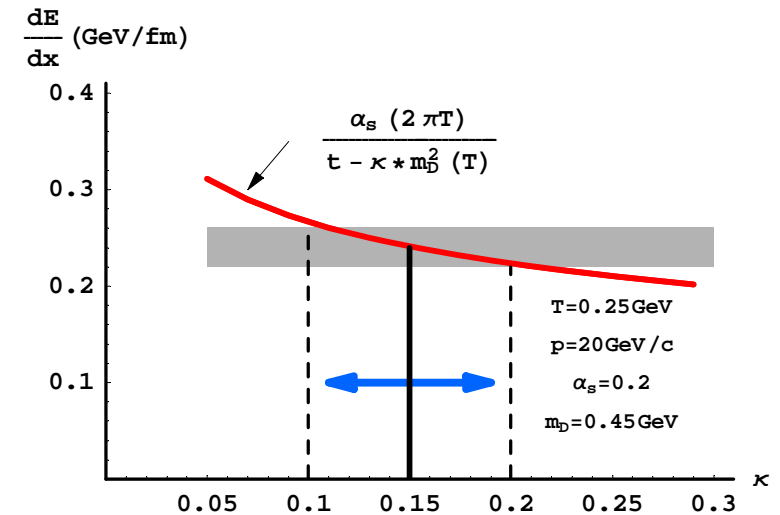
# OBE Model at fixed $\alpha_s$ : optimal $\mu^2$

THEN: Optimal choice of  $\mu$  in our OBE model:

$$\frac{\alpha_s(2\pi T)}{t - \mu^2}$$

$$\mu^2(T) \approx 0.15 m_D^2(T)$$

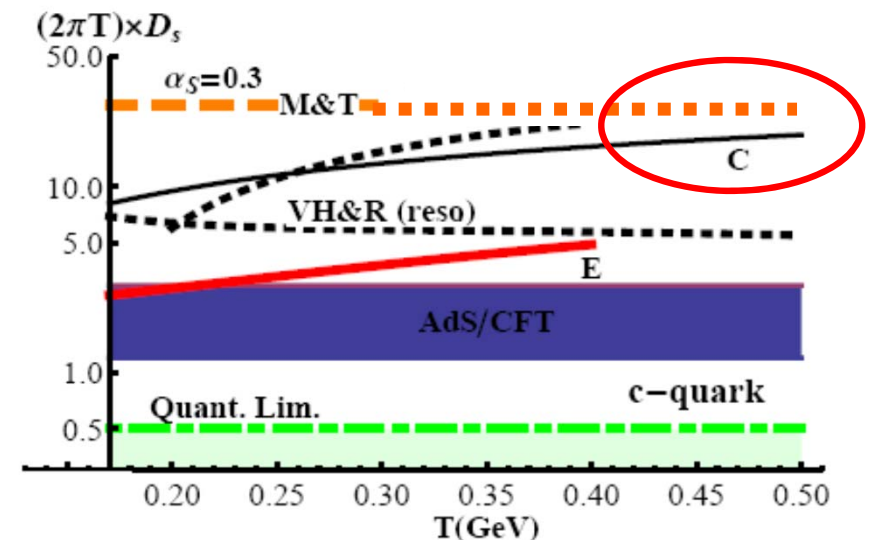
with  $m_D^2 = 4\pi\alpha_s(2\pi T)(1+3/6)\chi T^2$



$\frac{dE_{coll}(c)}{dx}$  ... factor 2 increase w.r.t. naïve pQCD (not enough to explain  $R_{AA}$ )

T(MeV) \ p(GeV/c)	10	20
200	0.36 (0.18)	0.49 (0.27)
400	0.70 (0.35)	0.98 (0.54)

Convergence with “pQCD” at high T





# Running $\alpha_s$ ...

Motivation: Even a fast parton with the largest momentum  $P$  will undergo collisions with moderate  $q$  exchange and large  $\alpha_s(Q^2)$ . The running aspect of the coupling constant has been “forgotten/neglected” in most of approaches

# ...asymptotic freedom and infrared slavery

## Strategy

1. Effective  $\alpha_{\text{eff}}(Q^2)$
2. “generalized BT” / convergent-kinetic  $\Rightarrow dE/dx$
3. Fix the optimal IR regulator in propagator  
i.e. in t-channel, fix the **optimal  $\kappa$**

$$\frac{\alpha_{\text{eff}}(t)}{t - \underbrace{\kappa \tilde{m}_D^2(T)}_{\mu^2(T)}}$$

Self consistent  $m_D$  (Peshier hep-ph/0607275)

$$m_{D\text{self}}^2(T) = (1+n_f/6) 4\pi\alpha_s(m_{D\text{self}}^2) \times T^2$$

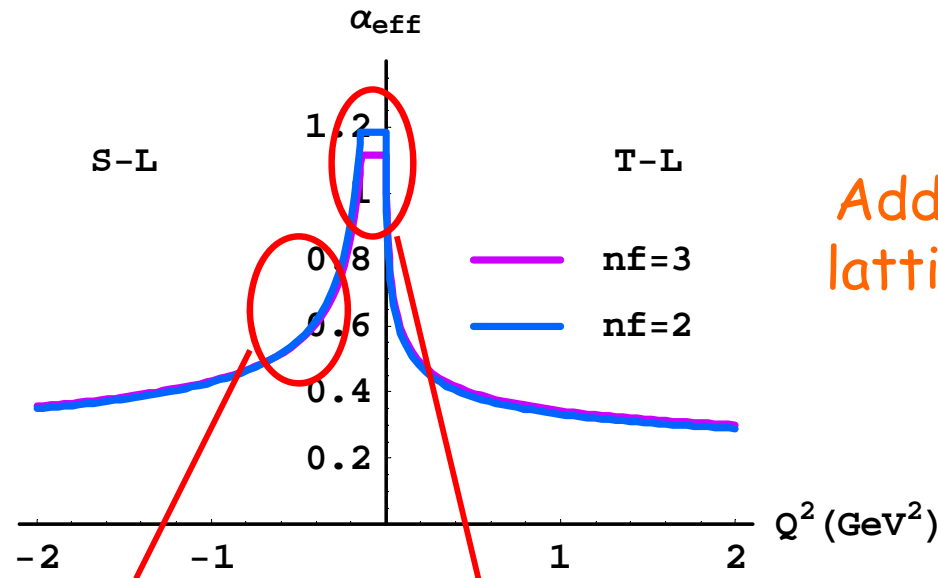
# Model E : running $\alpha_s$ AND optimal $\mu^2$

- Effective  $\alpha_s(Q^2)$  (Dokshitzer 95, Brodsky 02)

Observable = T-L effective coupling \* Process dependent fct

“Universality constrain” (Dokshitzer 02)  
helps reducing uncertainties:

$$\frac{1}{Q_u} \int_{|Q^2| \leq Q_u^2} dQ \alpha_s(Q^2) \approx 0.5$$



Additional inputs (from lattice) could be helpful

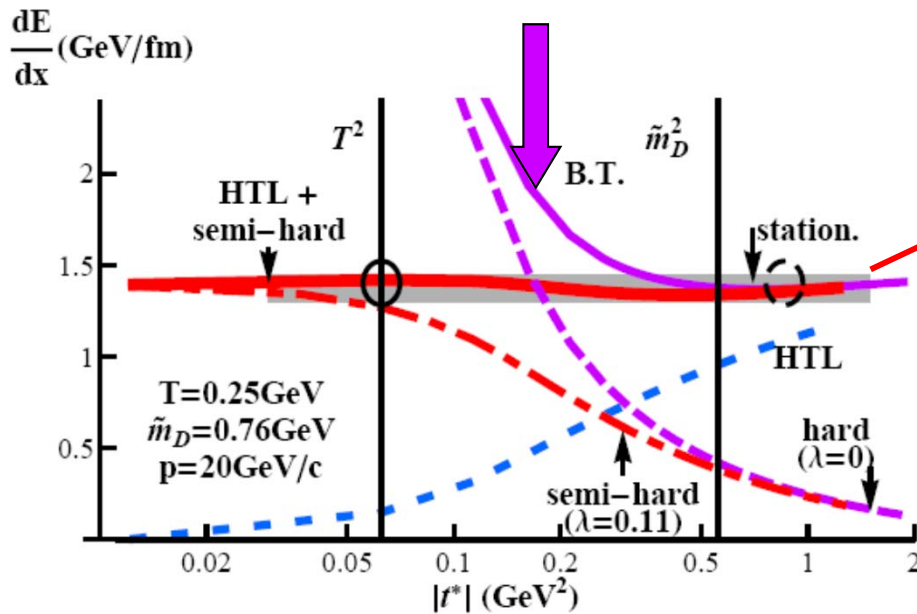
Large values for intermediate momentum-transfer

IR safe. The detailed form very close to  $Q^2 = 0$  is not important does not contribute to the energy loss

# Model E : running $\alpha_s$ AND optimal $\mu^2$

- Bona fide “running HTL”:  $\alpha_s \rightarrow \alpha_s(Q^2)$

**Brute BT: Not Indep. of  $|t^*|$  !**



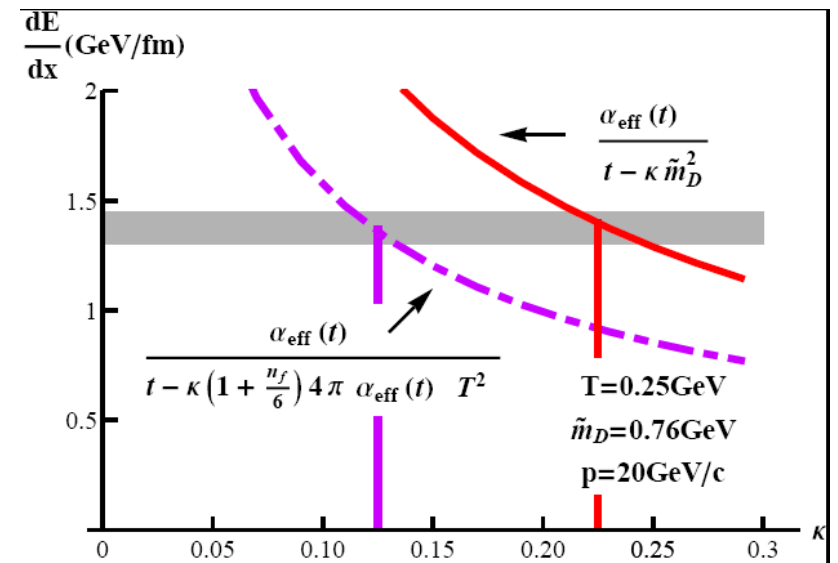
Introducing semi-hard propag...

$$\frac{\alpha_{\text{eff}}(t)}{t} \longrightarrow \frac{\alpha_{\text{eff}}(t)}{t - \lambda m_D^2(T, t)}$$

...leads to stationary results

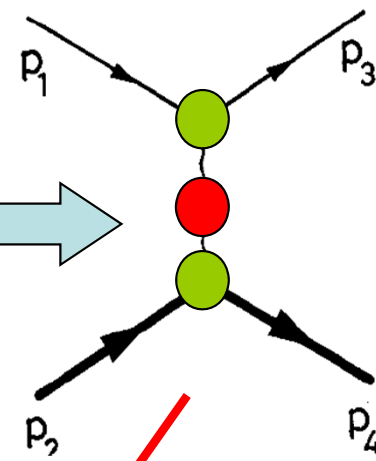
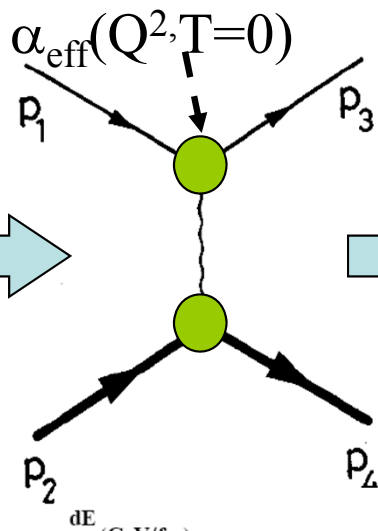
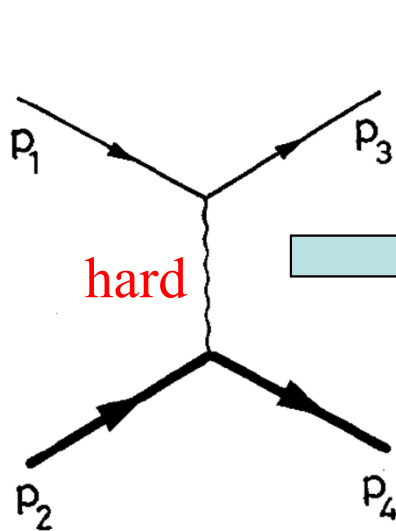
- Optimal regulator:

$$\mu^2(T) \approx 0.2 m_{D\text{self}}^2(T)$$



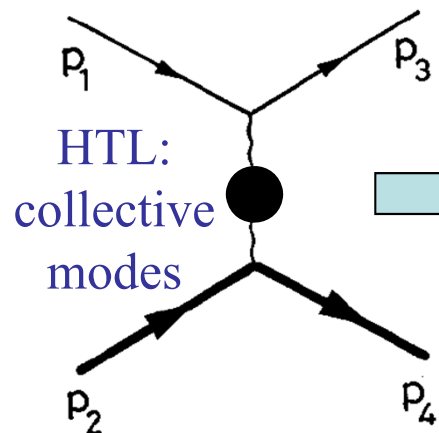
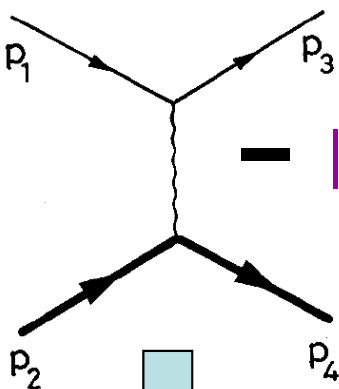
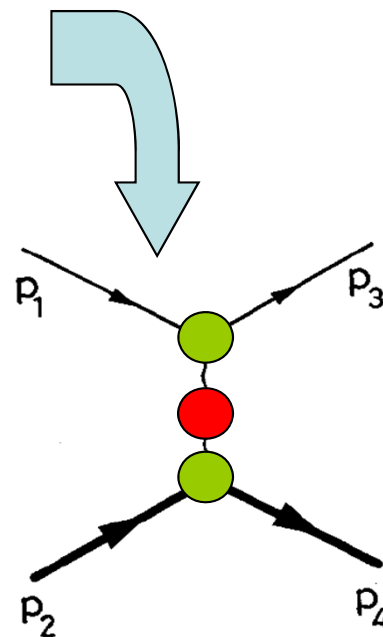
# $\mu$ -local-model: medium effects at finite T in t-channel

Large  $|t|$

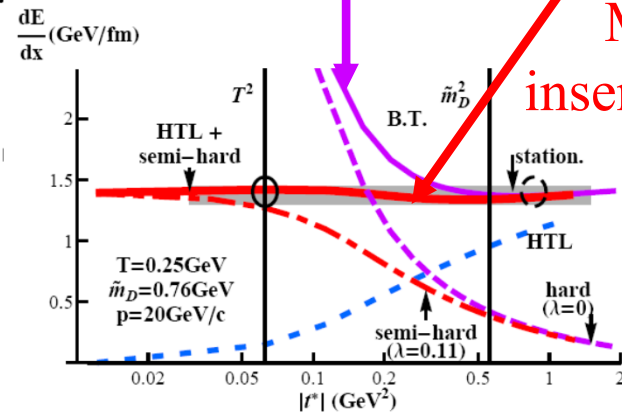


Semi-hard

$$\frac{\alpha_{\text{eff}}(t)}{t - \lambda m_D^2(T, t)}$$



Low  $|t|$



BT

OGE with effective polarisation  
 $\mu^2(T)=0.2 m_{\text{Dself}}^2(T)$

$$m_{\text{Dself}}^2(T) = (1+n_f/6) 4\pi\alpha_{\text{eff}}(m_{\text{Dself}}^2) T^2$$

Bona Fide running HTL:  
 $\alpha_s \rightarrow \alpha_s(t)$  in  $\Pi_L$  and  $\Pi_T$

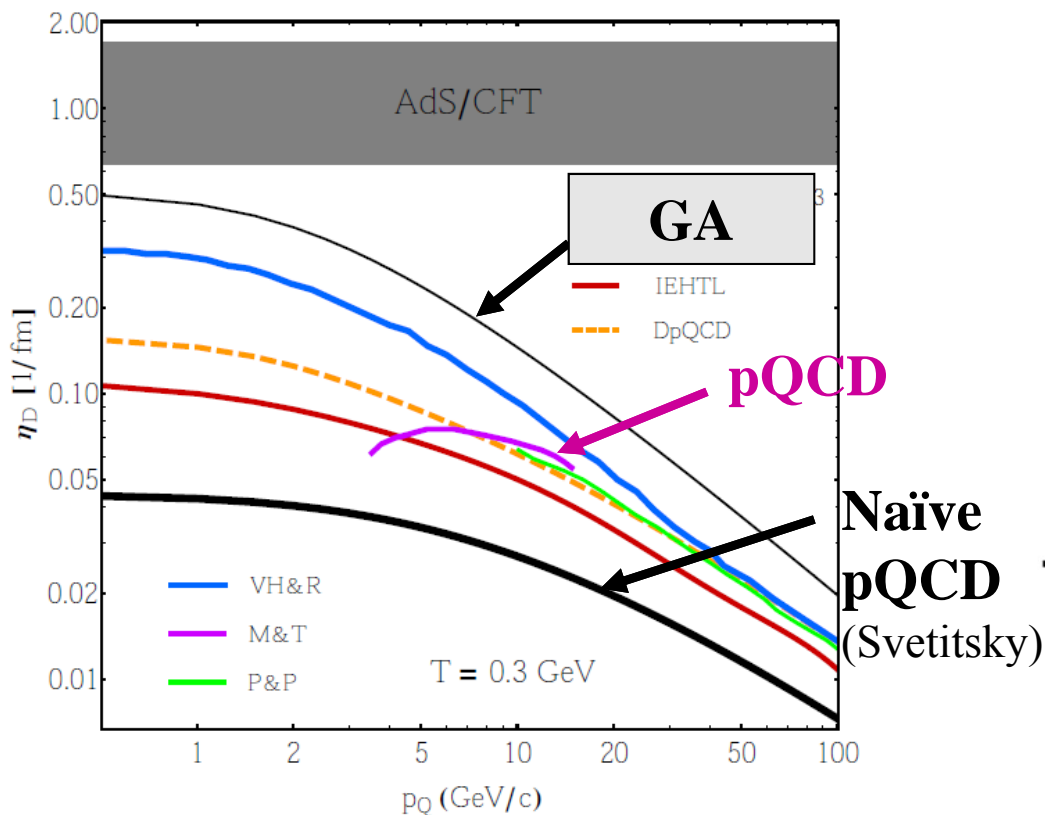
# Running $\alpha_s$ : some Energy-Loss values

$$\frac{dE_{coll}(c/b)}{dx}$$

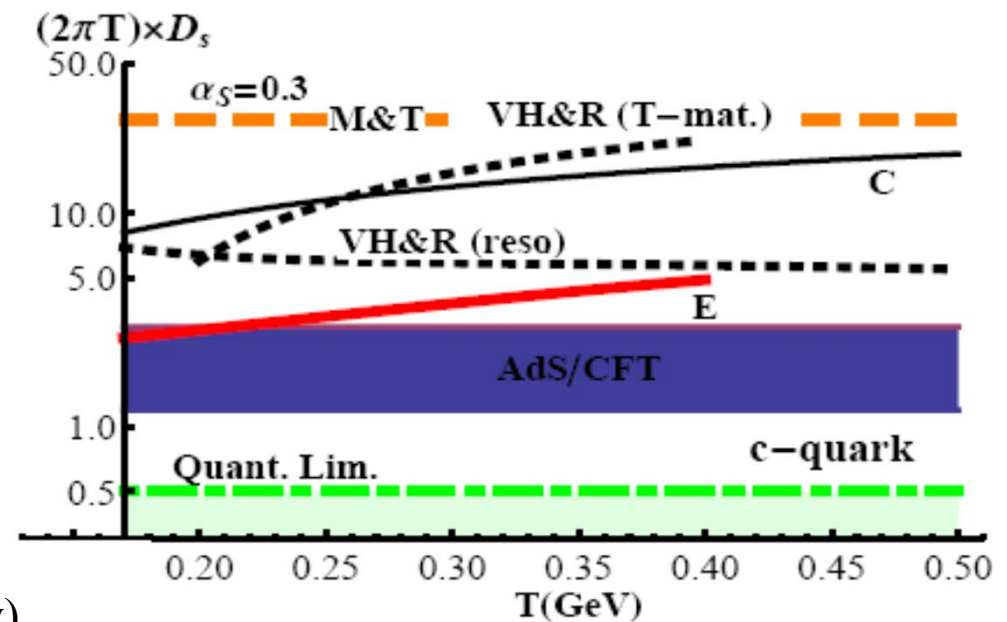
T(MeV) \ p(GeV/c)	10	20
200	1 / 0.65	1.2 / 0.9
400	2.1 / 1.4	2.4 / 2

**$\approx 10\%$  of HQ energy**

## Drag coefficient (inverse relax. time)



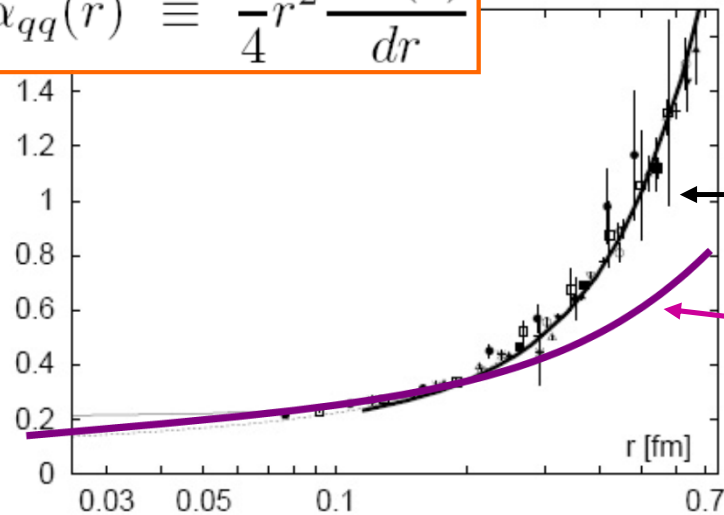
## Diffusion coefficient



# $\mu$ -local-model: Eff. Running $\alpha_s$ vs lQCD

**T=0**

$$\alpha_{qq}(r) \equiv \frac{3}{4} r^2 \frac{dV(r)}{dr}$$



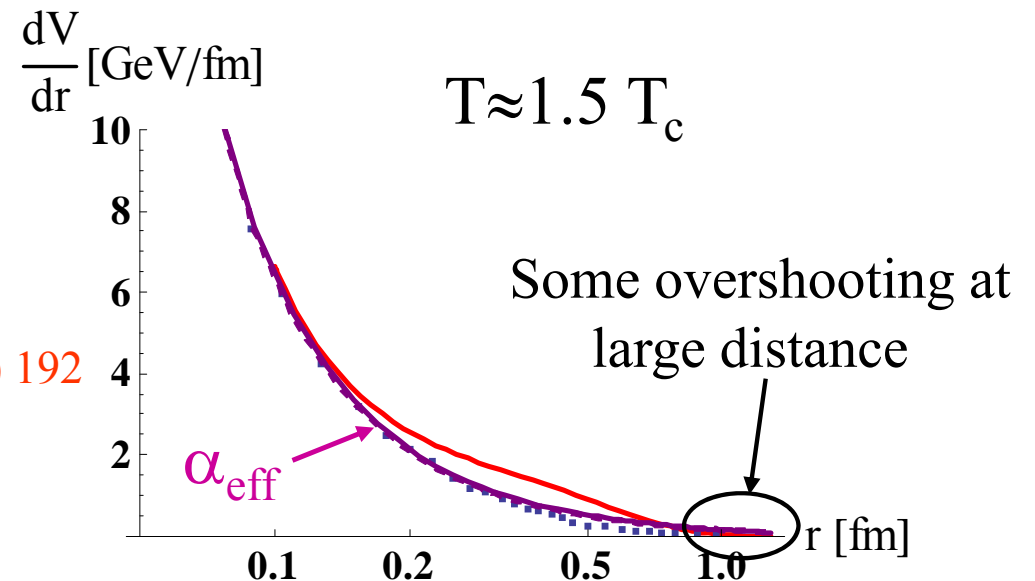
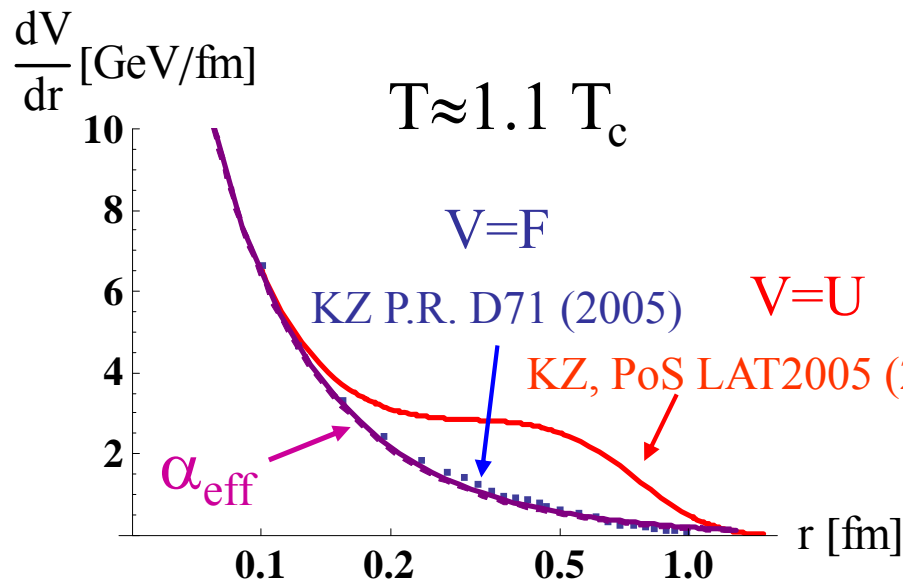
O. Kaczmarek & F. Zantow (KZ) ( $n_f=2$  QCD), P.R.D71 (2005) 114510

Genuine non-pert (flux tube)

optimal  $\mu$ , running  $\alpha_{\text{eff}}$

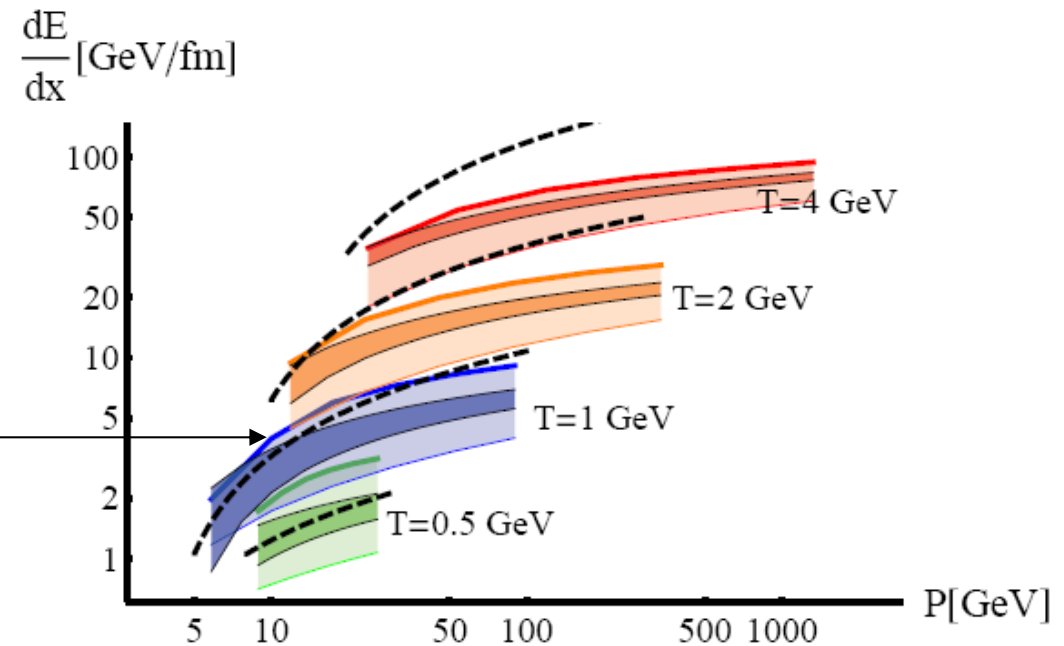
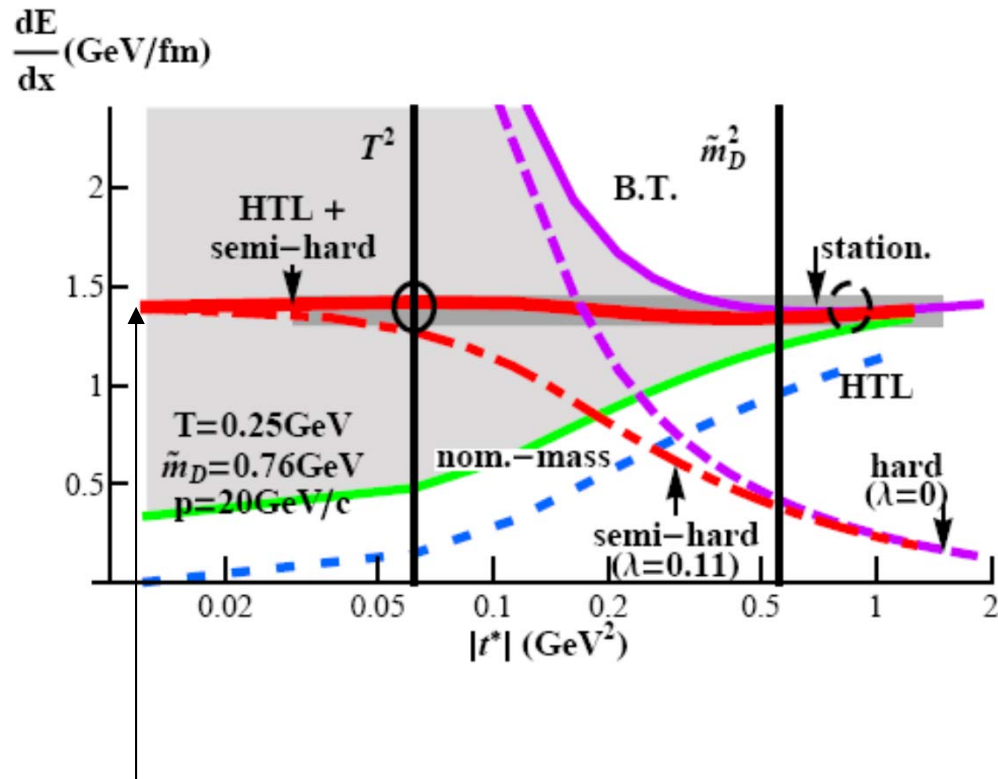
V: $\omega=0$  sector; dE/dx: finite  $\omega$

**Finite T**



**Merging at  $\approx 2 T_c$**

# Running $\alpha_s$ : theoretical uncertainties



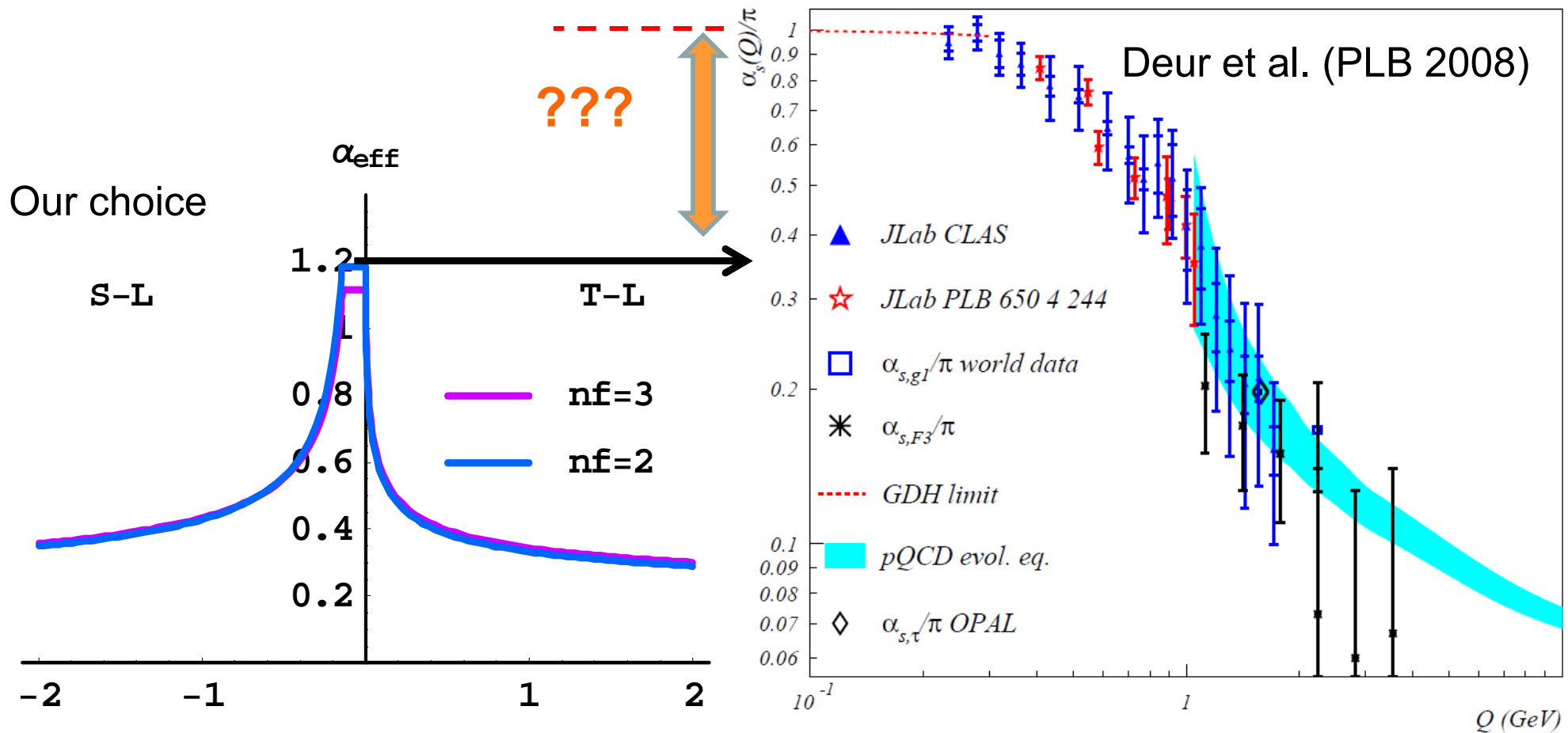
E: optimal  $\mu$ , running  $\alpha_{\text{eff}}$

**Dark zones: Peshier & Peigné (2008)**

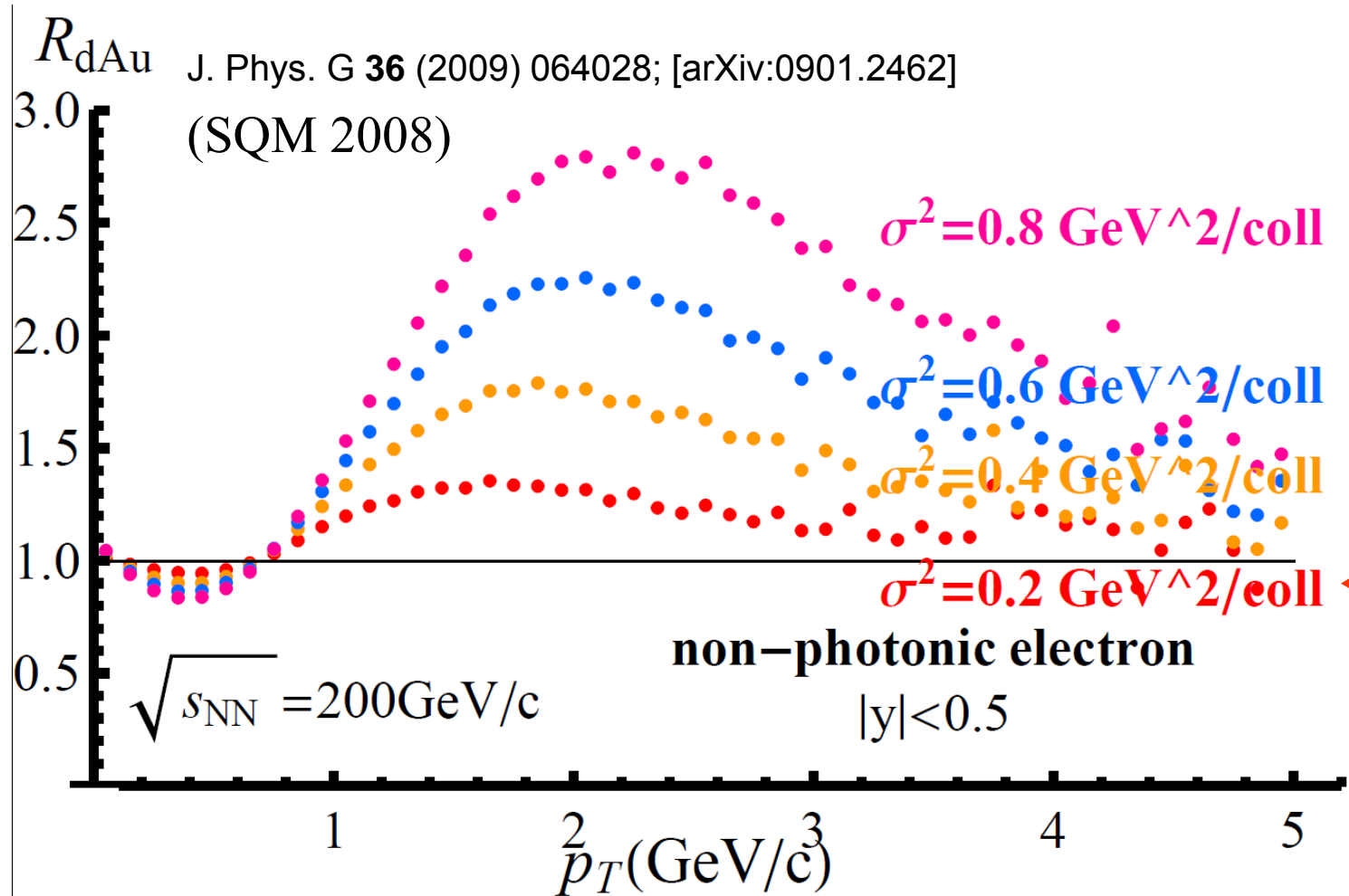


# Elastic Eloss @ RHIC

Still some uncertainties on the level of the coupling constant  
 => we allow for a multiplication of our pQCD (inspired) cross section by a factor K (fixed once and for all by comp. with exp)



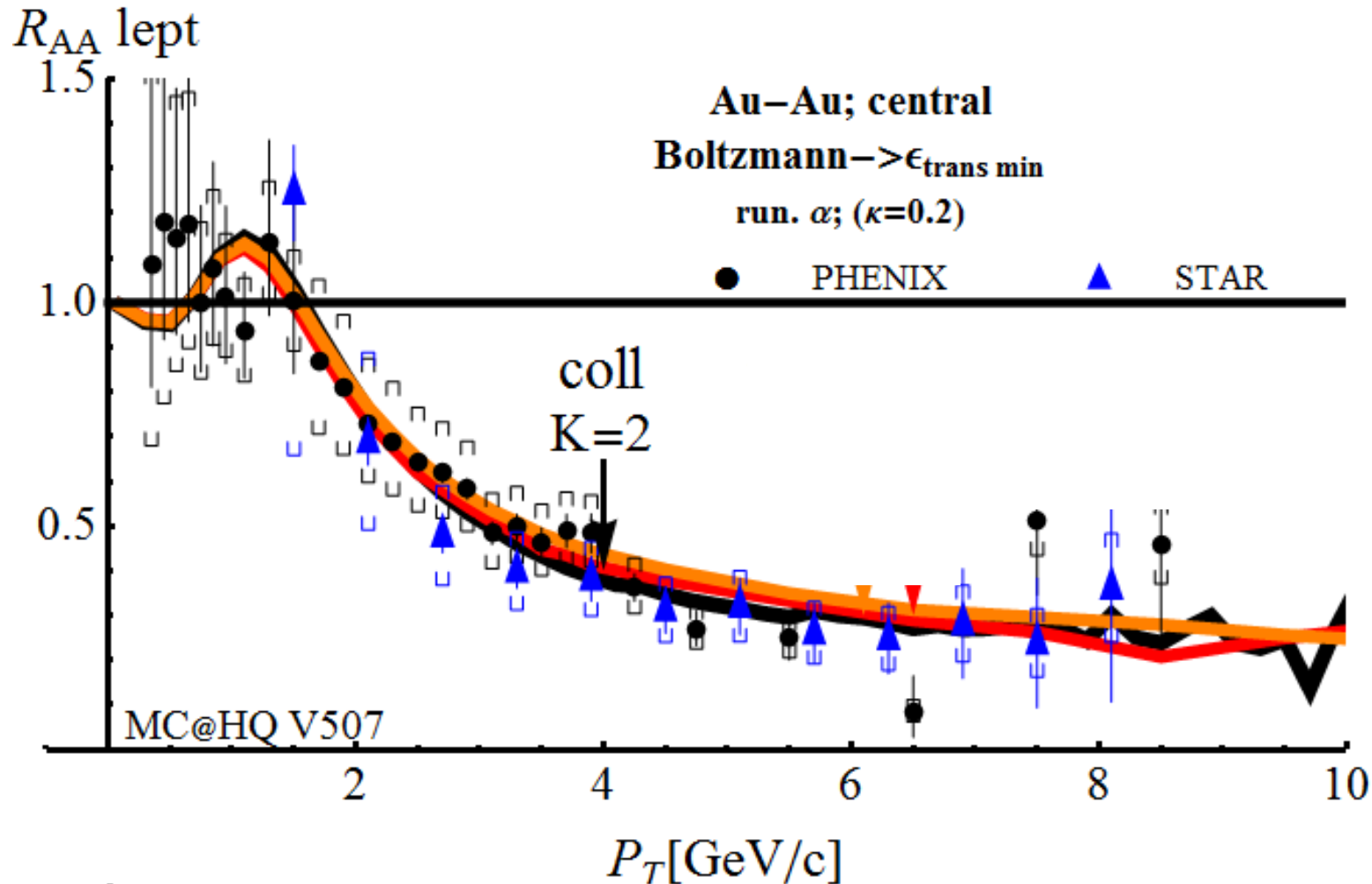
# CNM effects



Selected values; rough agreement with recent RHIC measurement, but physical origin remains unclear

# Elastic for leptons @ RHIC

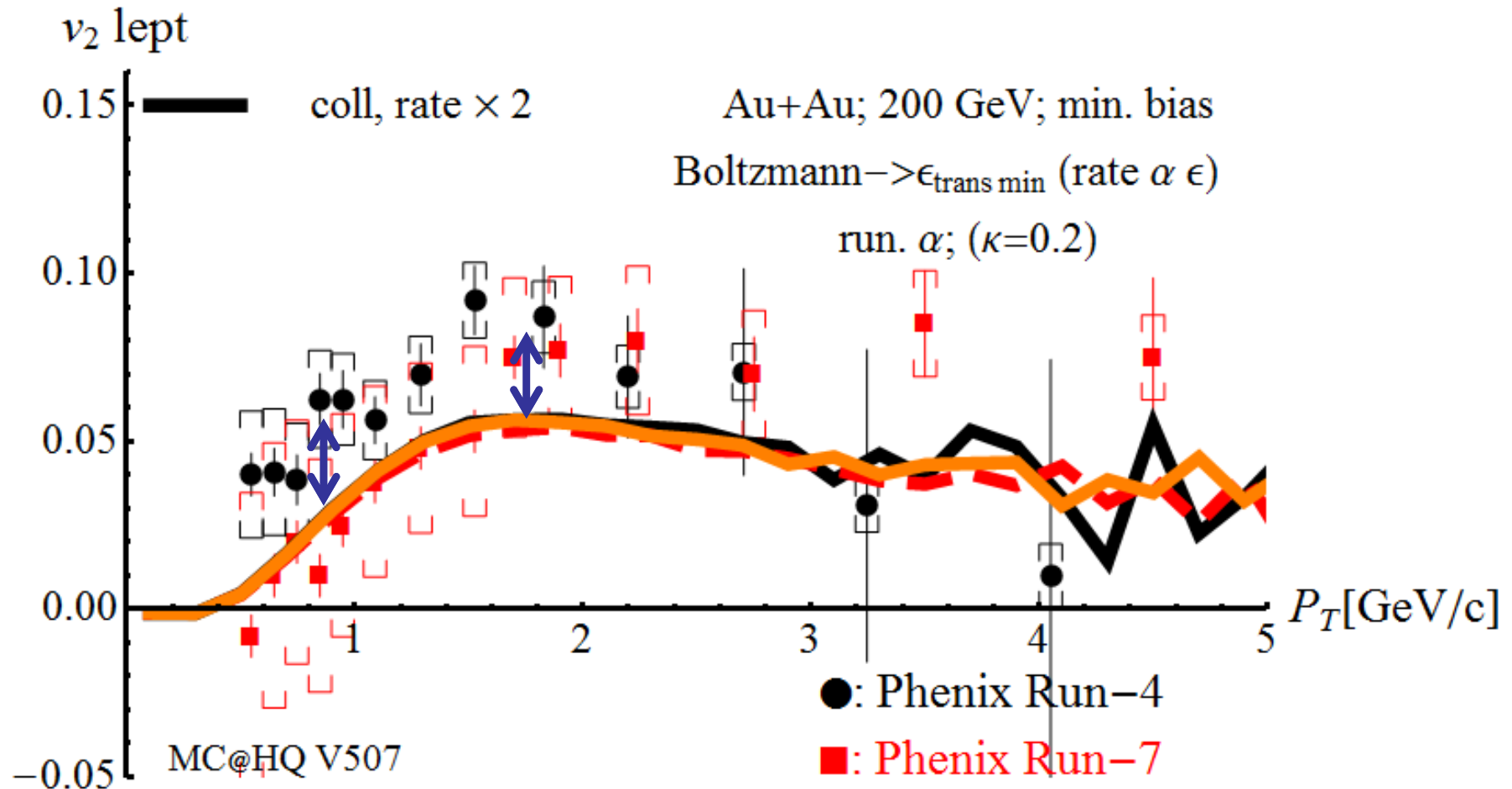
Gossiaux and Aichelin, PRC 78 (2008)



Good agreement for NPSE at the price of a factor  $K=2$

# Elastic for leptons @ RHIC

Gossiaux and Aichelin, PRC 78 (2008)

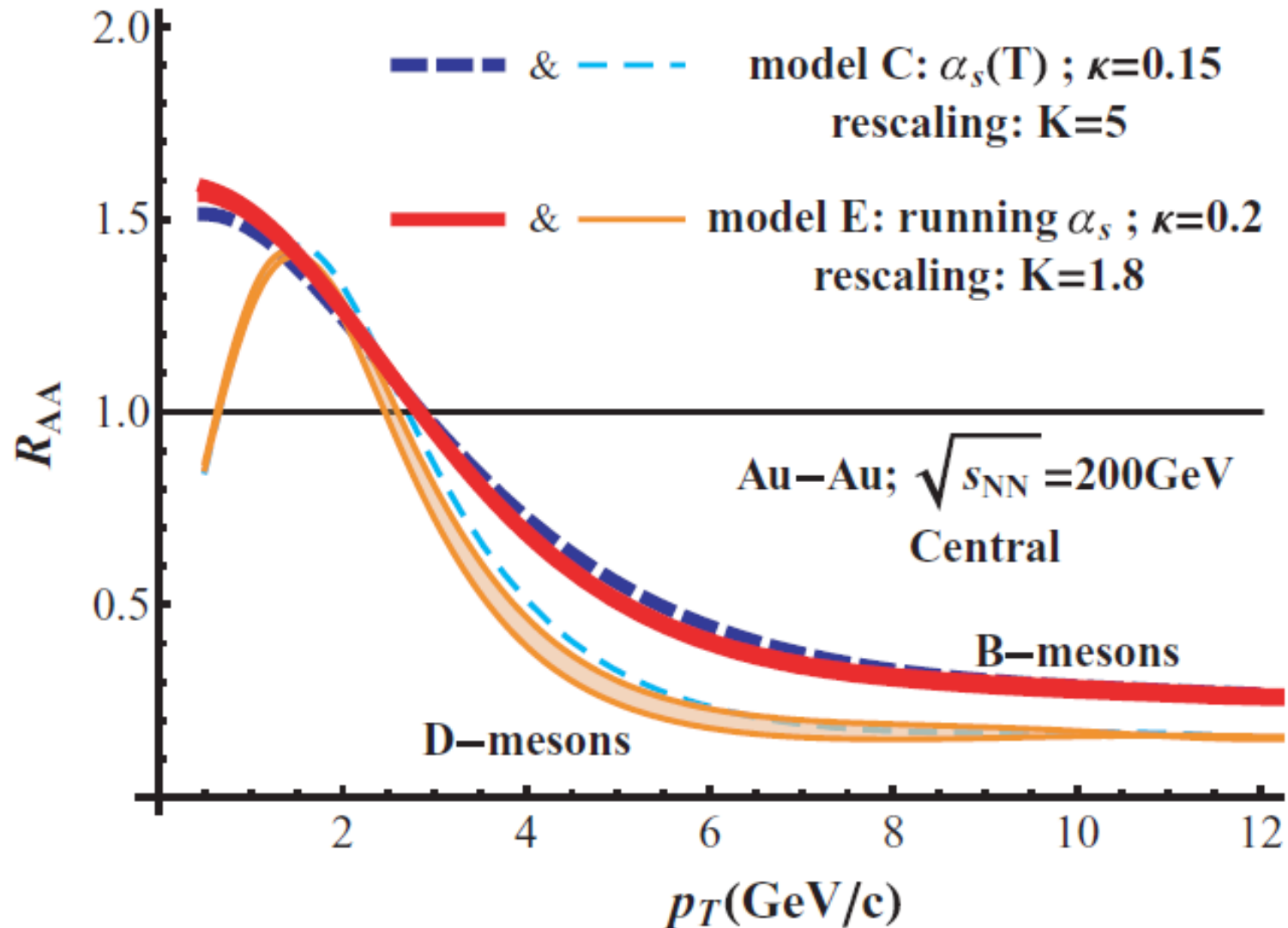


Some contribution from D meson rescattering ?

(see V. Ozvenchuk's talk)

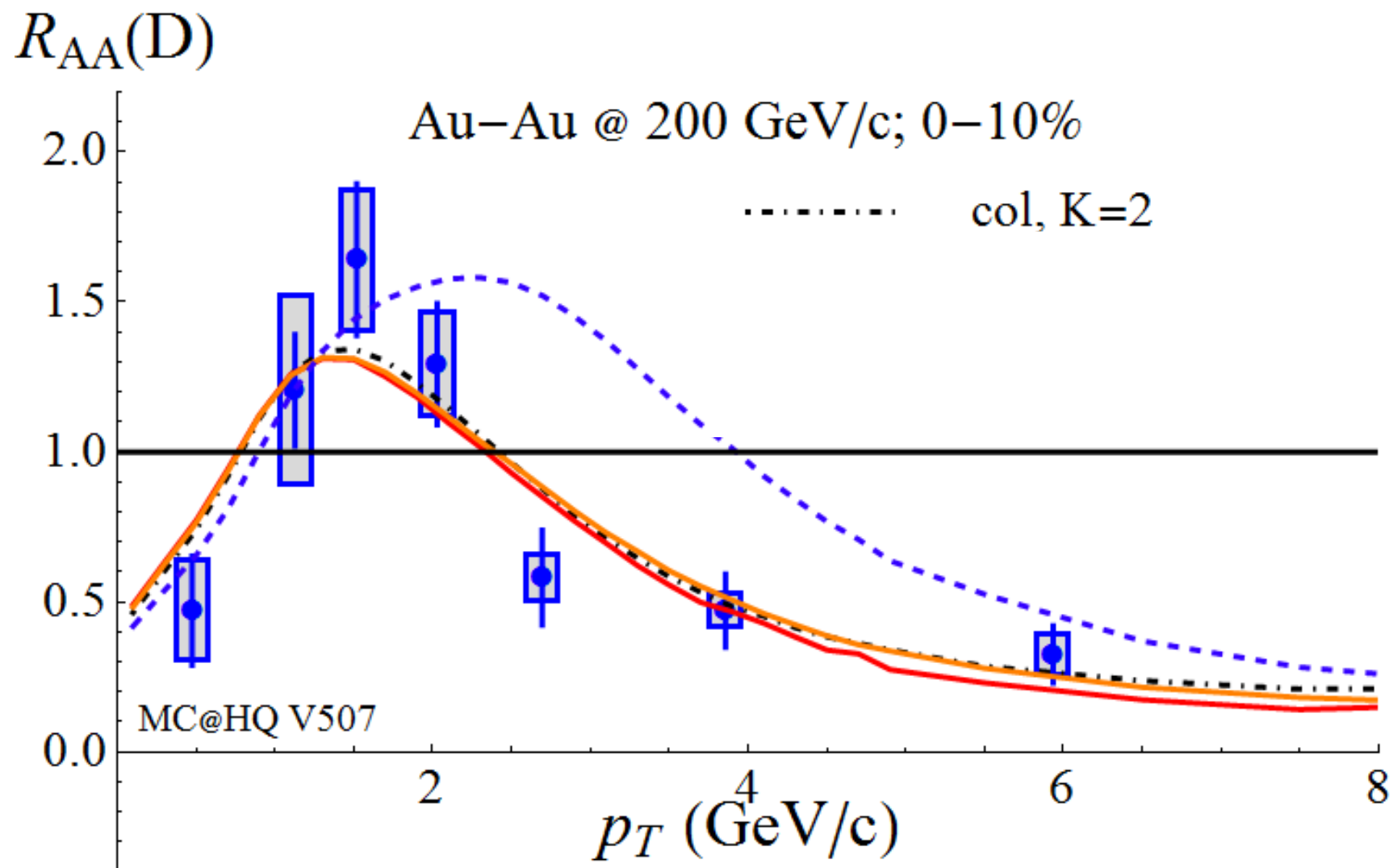
# Elastic D and B mesons @ RHIC

Gossiaux, Bierkandt and Aichelin, PRC 79 (2009)



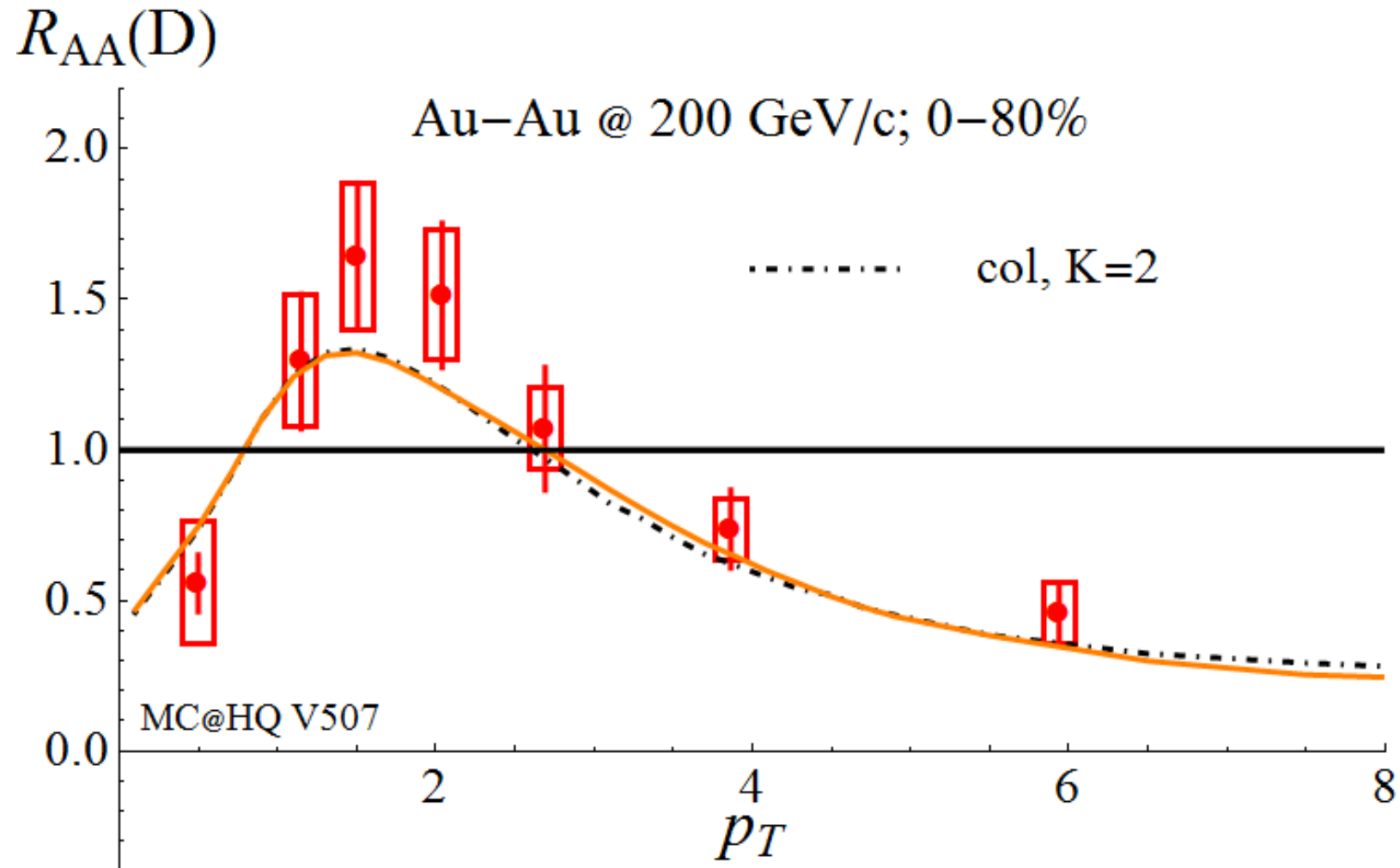
# Elastic D mesons @ RHIC

3 years later: QM 2012.  $R_{AA}(D)$  measured by STAR



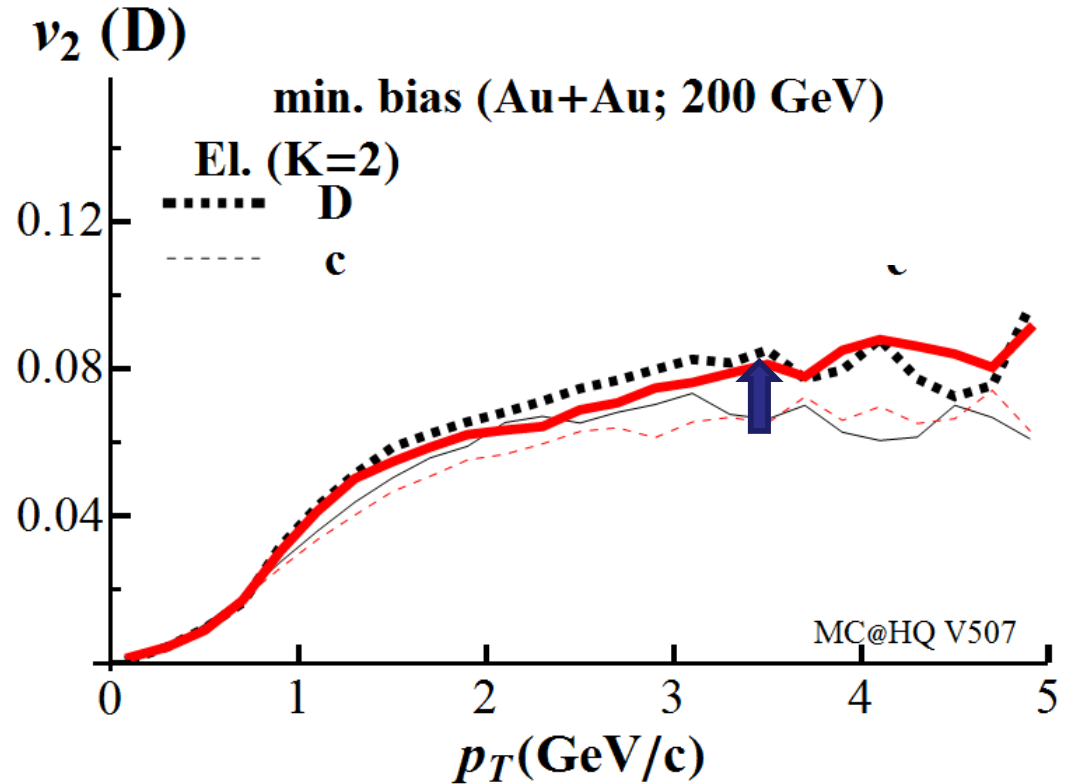
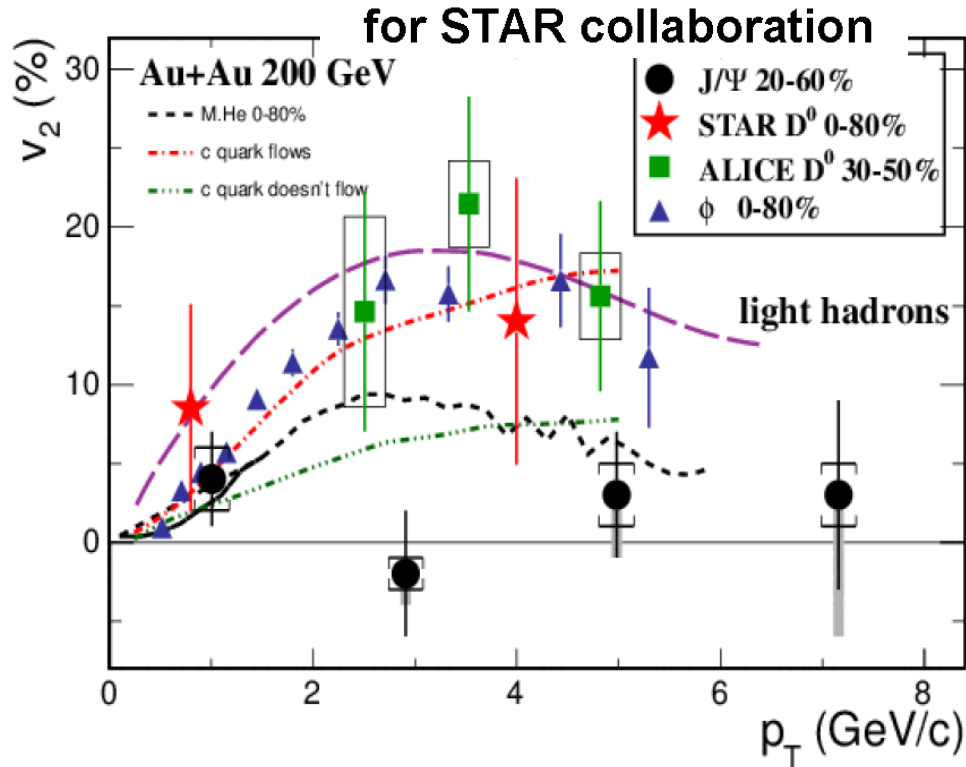
# Elastic D mesons @ RHIC

3 years later: QM 2012.  $R_{AA}(D)$  measured by STAR



# Elastic D mesons @ RHIC

Jaroslav Bielčík



Rather little contribution from the light quark in our treatment... but conclusion may depend on the parameters ( $m_q$ , wave function)

Coalescence according to extended Dover framework

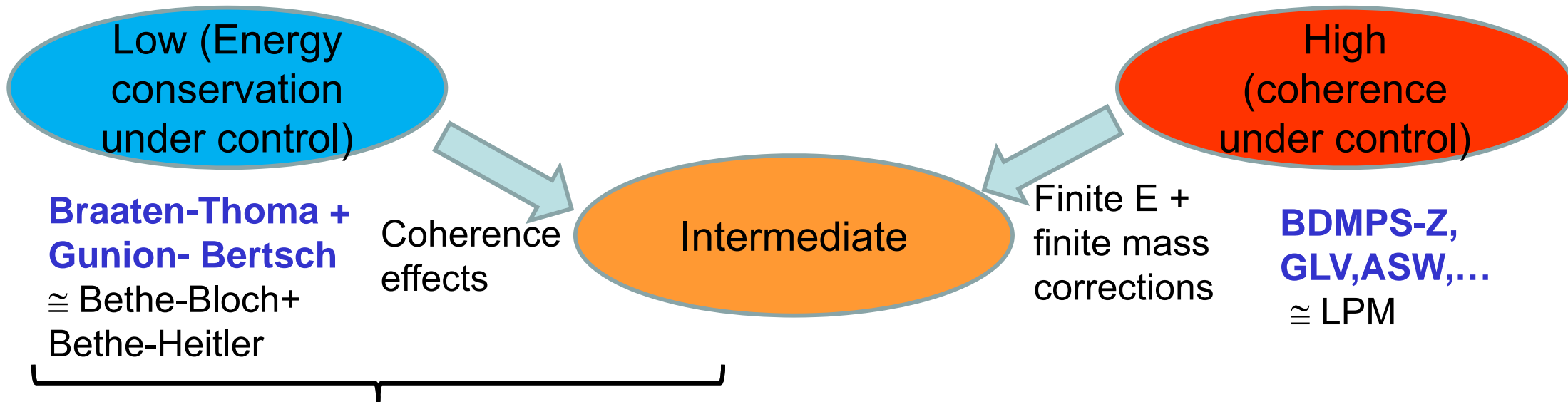
(PRC 79 044906)

$$N_{\Phi} = \int \frac{d^3 p_q}{(2\pi\hbar)^3} \frac{p_q \cdot \hat{d}\sigma}{E_q u_Q \cdot \hat{d}\sigma} f_q(x_Q, p_q) (\sqrt{2\pi} R_c)^3 \times F_{\Phi}(p_Q, p_q),$$



# Radiative E loss at intermediate $p_T$ (Aichelin & Gousset)

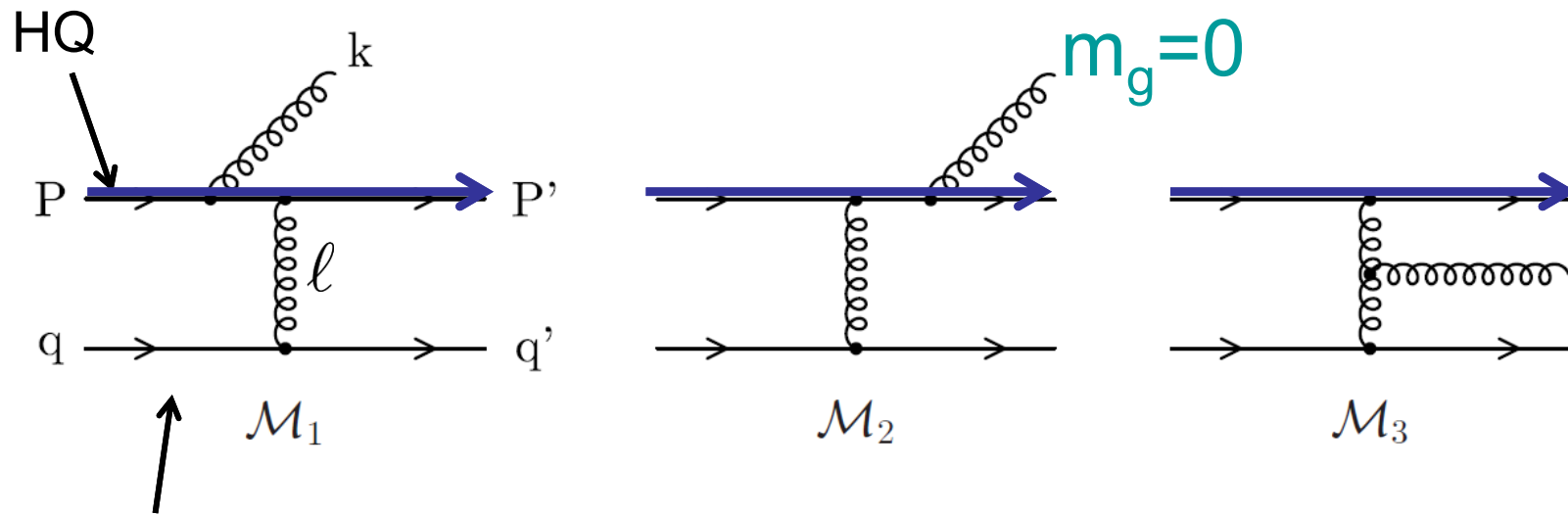
- Most of the *interesting* HF observables so far: located at *intermediate*  $p_T$   
( $\approx 3$  GeV-50 GeV)
- Intermediate  $p_T$ : hope that pQCD (or pQCD inspired models) apply (as compared to low  $p_T$ )
- Intermediate  $p_T$ : mass effect still present and thus hope to learn something more as compared to large  $p_T$



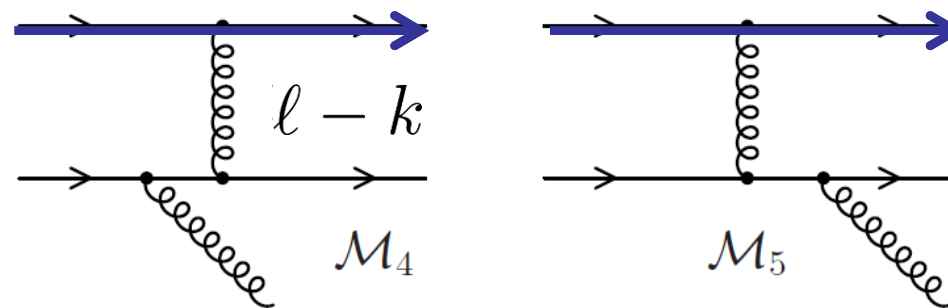
Approach pursued in our **models...**

=> Need for falsification (more observables; IQCD): **Azimuthal correlations** ?

# $qQ \rightarrow qQg$ “in the Vacuum” (see Th. Gousset’s talk)



Dynamical light quark



Sudakov decomposition:  $P = p + \frac{m_Q^2}{s - m_Q^2} q$   $p$  and  $q$  : light-like

$$k = xp + yq + \vec{k}_t$$

Momentum transfer:  $\ell = q - q'$ ,  $t = \ell^2$

# qQ → qQg “in the Vacuum”: Exact Relation

Exact relation: 
$$\frac{d\sigma^{Qq \rightarrow Qgq}}{dx d^2 k_t d^2 \ell_t} = \frac{1}{2(s - M^2)} |\mathcal{M}|^2 \frac{1}{4(2\pi)^5 \sqrt{\Delta}} \Theta(\Delta)$$

With:

$\Delta$ : phase-space

and

$$\mathcal{M} = \mathcal{M}^{\text{QCD}} \oplus \mathcal{M}^{\text{QED-like}}$$



Rapidity-plateau



Fragmentation region

(subdominant for  $\tilde{s} \gg \{l_t^2, k_t^2\}$ )

$$\mathcal{M}^{\text{QCD}} \simeq \mathcal{M}^{\text{SQCD}} + \mathcal{O}(x^2)$$



$$\mathcal{M} \simeq \mathcal{M}^{\text{SQCD}} = g C_3 \left( \frac{-4 g^2 P \cdot q}{\ell^2} \right) \left( \frac{(2(1-x) - x') \vec{\epsilon}_t \cdot \vec{k}_t}{\vec{k}_t^2 + x^2 m_Q^2} - \frac{2(1-x-x') \vec{\epsilon}_t \cdot (\vec{k}_t - \vec{l}_t)}{(\vec{k}_t - \vec{l}_t)^2 + (x+x')^2 m_Q^2} \right).$$

$x'(\vec{k}_t, \vec{l}_t, x)$  Recoil momentum of the l.q. (in the Sudakov decomposition)

Seeked extension of the Gunion-Bertsch model

# qQ → qQg “in the Vacuum”: High Energy Limit

One can show:  $x'(\vec{k}_t, \vec{l}_t, x) \ll 1 \Leftrightarrow \underbrace{x(s - m_Q^2)}_{\text{High energy condition}} \gg \{l_t^2, k_t^2\}$



High energy condition  
(when  $s$  disappears from the  $d\sigma$  : GB)

$$\frac{d\sigma^{Qq \rightarrow Qgq}}{dx d^2 k_t d^2 l_t} \xrightarrow{\text{HE}} \frac{d\sigma_{\text{el}}}{d^2 l_t} P_g(x, \vec{k}_t, \vec{l}_t)$$

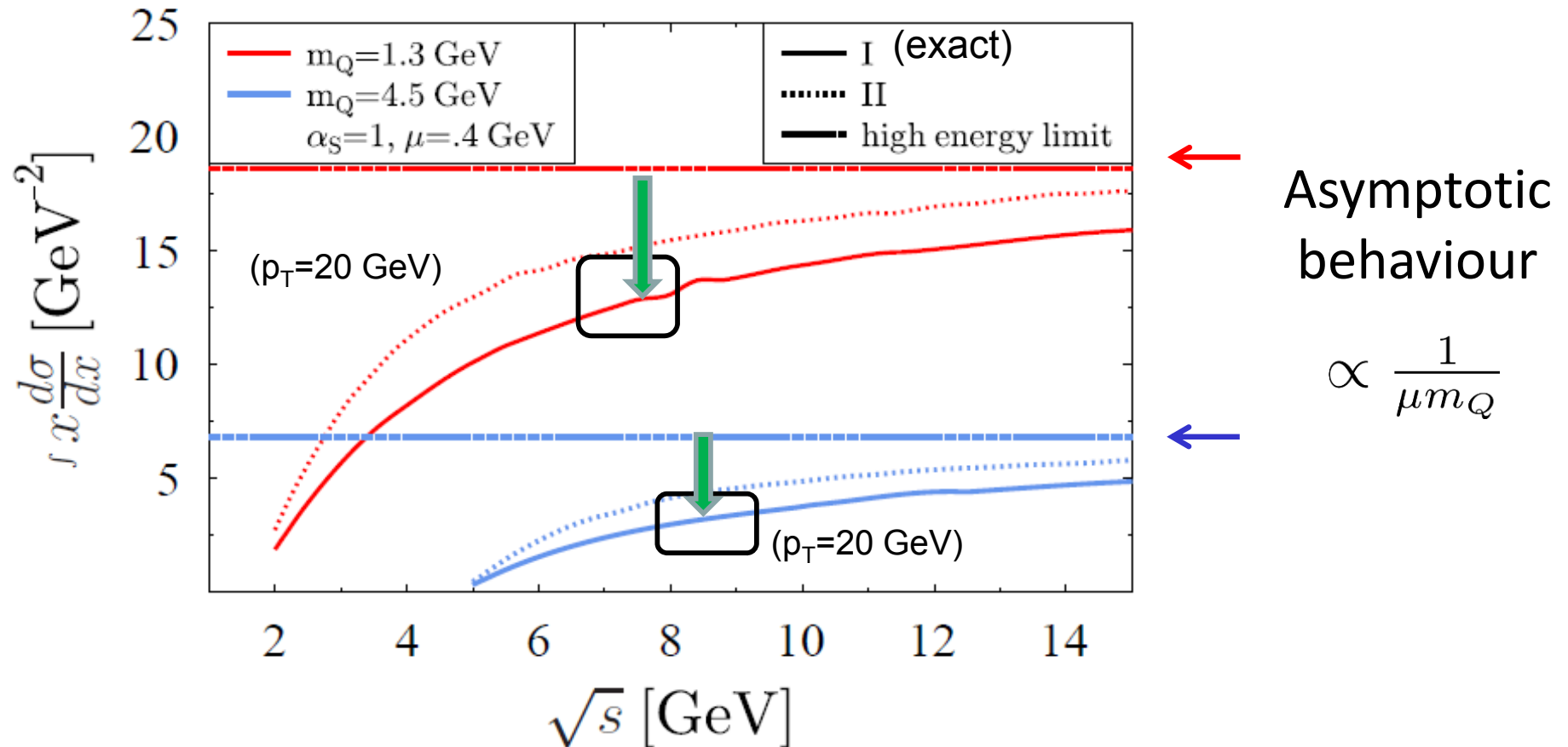
with:  $P_g = \frac{C_A \alpha_s}{\pi^2} \frac{1-x}{x} \left( \frac{\vec{k}_t}{\vec{k}_t^2 + x^2 m_Q^2} - \frac{\vec{k}_t - \vec{l}_t}{(\vec{k}_t - \vec{l}_t)^2 + x^2 m_Q^2} \right)^2$

No collinear divergence thanks to HQ mass (finite formation time),  
but (usual) IR divergence in the  $d\sigma_{\text{el}}$  => prescription: IR regulator  $\mu$ .

$$\frac{d\sigma_{\text{el}}}{d^2 l_t} \propto \frac{1}{t^2} \rightarrow \frac{1}{(t - \mu^2)^2} \quad \mu : \text{Natural scale for } l_t$$

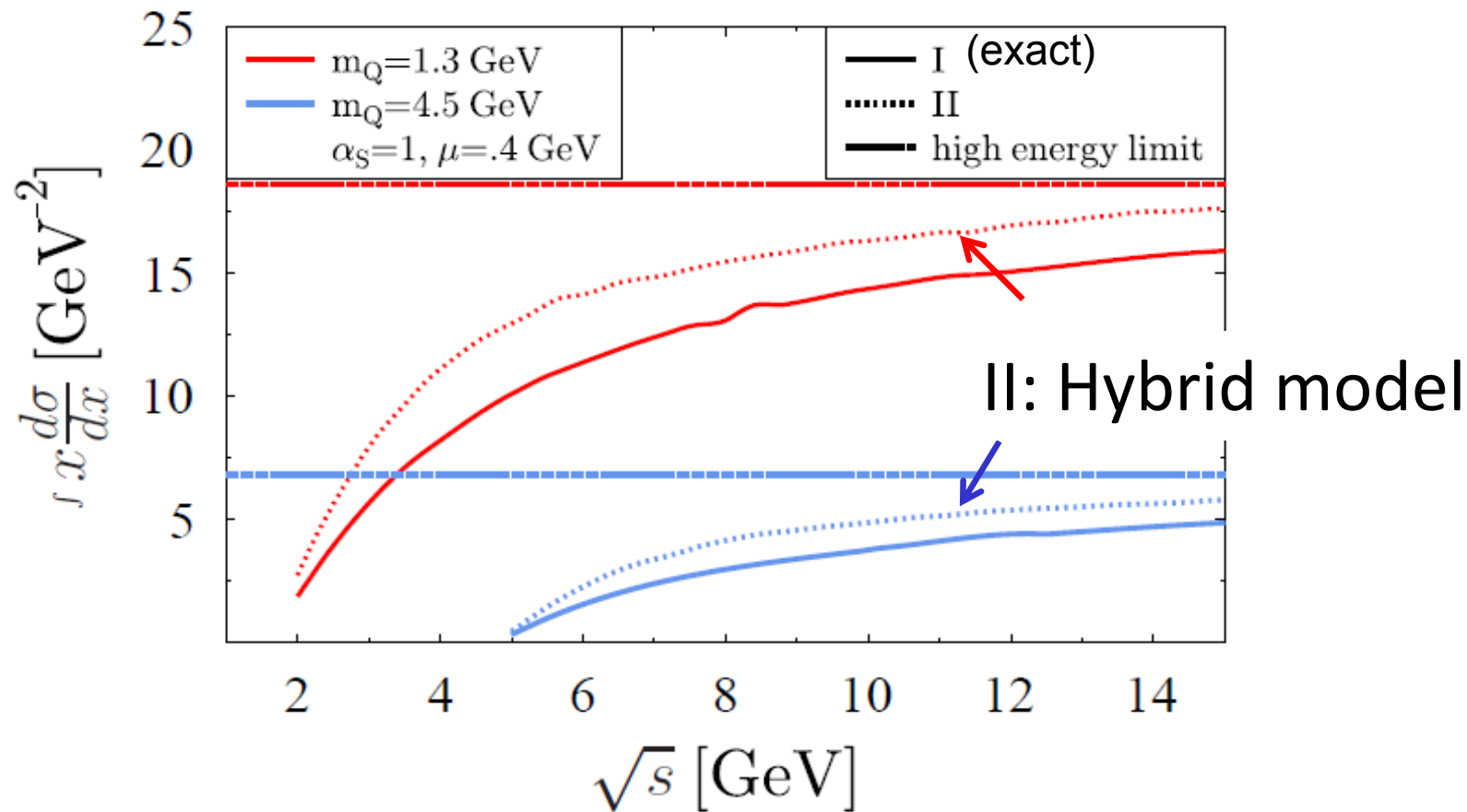
# Incoherent Induced Energy Loss at Finite Energy

$$\frac{dE_{\text{rad}}}{dz} \approx \rho \int \omega \frac{d\sigma}{d\omega} d\omega \approx \rho E_{\text{beam}} \int x \frac{d\sigma}{dx} dx. \quad \text{Contribution from both } x < x_M \text{ and } x > x_M$$



Finite energy lead to strong reduction of the radiative energy loss at intermediate p<sub>T</sub>

# Incoherent Induced Energy Loss at Finite Energy



$$\frac{d\sigma_{II}^{Qq \rightarrow Qgq}}{dx d^2 k_t d^2 \ell_t} = \frac{d\sigma_{el}}{d^2 \ell_t} P_g(x, \vec{k}_t, \vec{\ell}_t) \Theta(\Delta) \quad \text{High energy } P_g + \text{finite phase space}$$

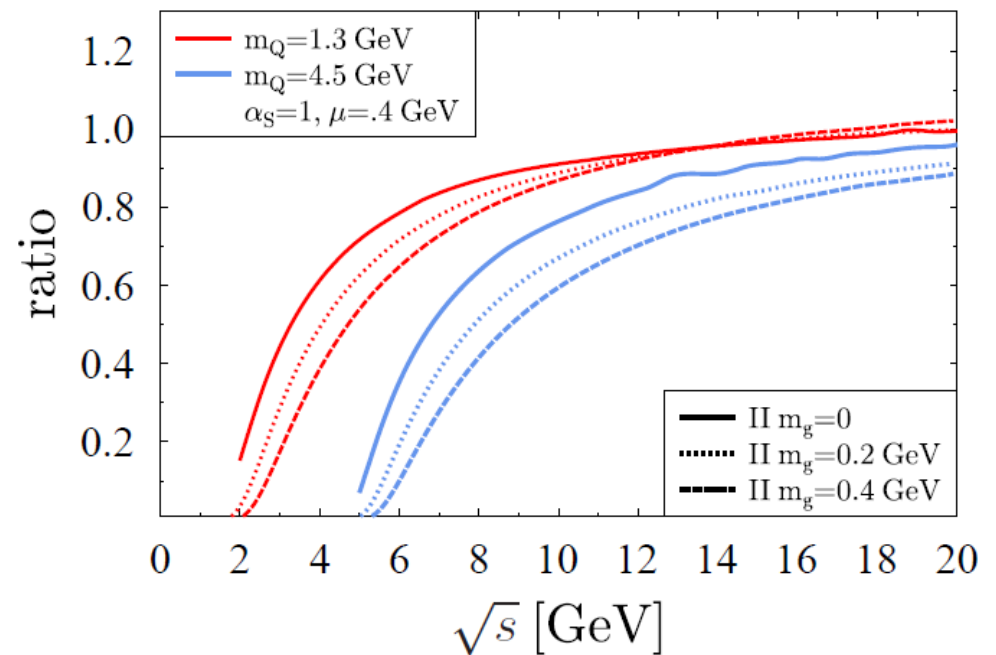
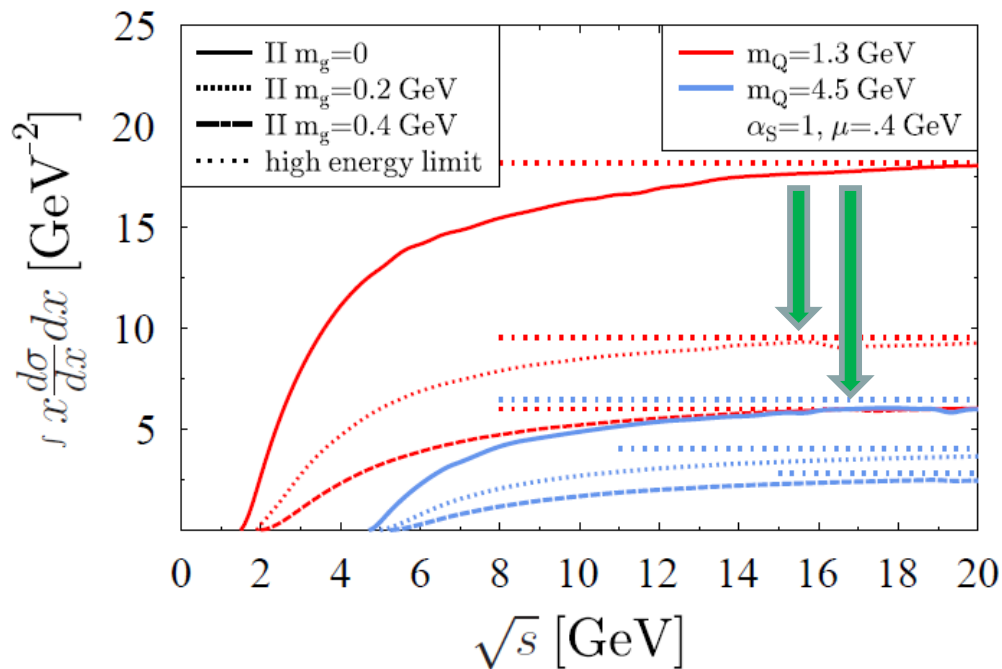
Useful for a) MC simulations & b)  $gQ \rightarrow gQg$

# Incoherent Induced Energy Loss at Finite T ( $m_g$ )

Our Prescription: Hybrid Model **with**

➤ modified phase space

➤ matrix el.  $P_g$  modified according to  $x^2 m_Q^2 \rightarrow x^2 m_Q^2 + (1-x)m_g^2$

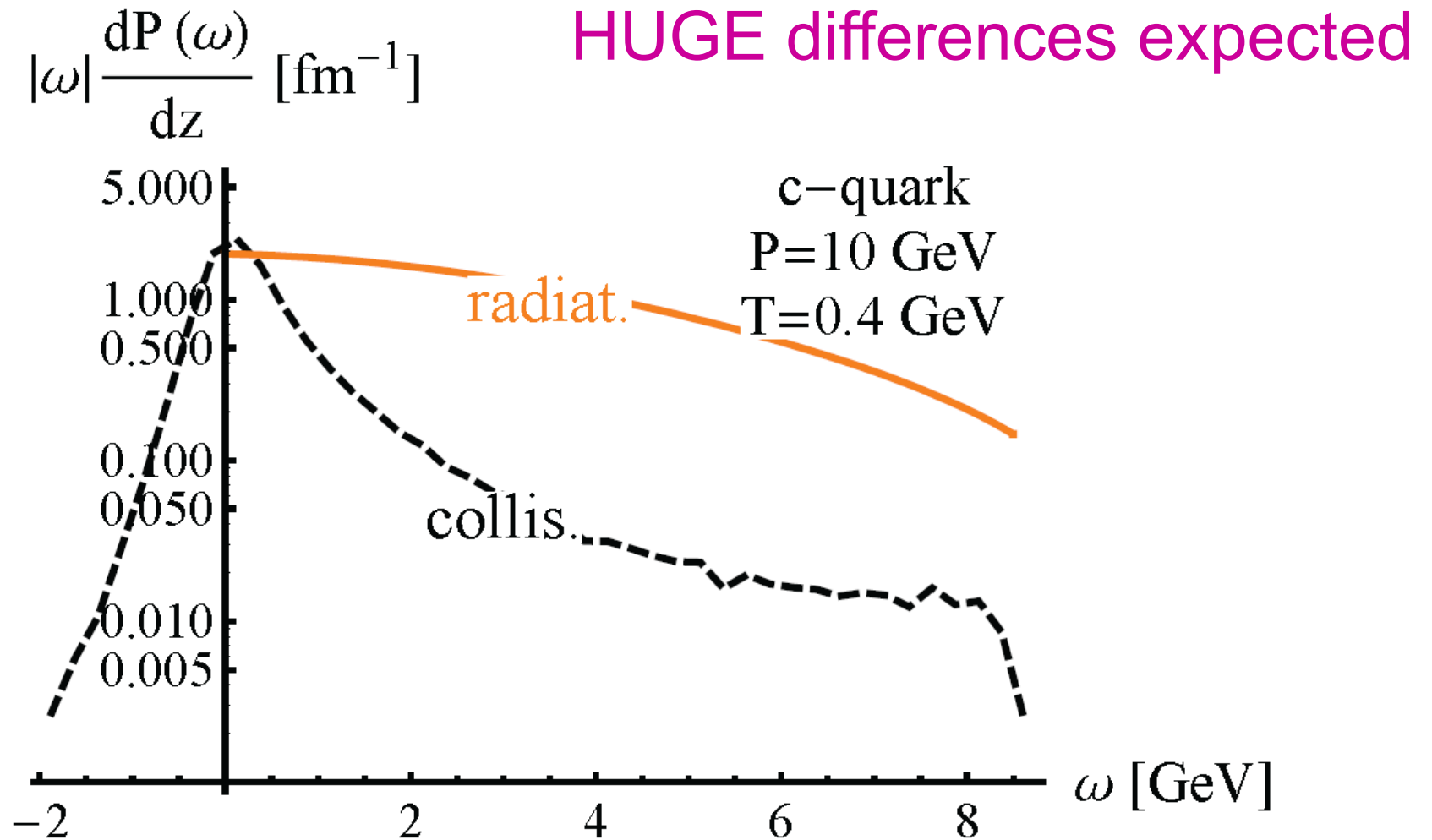


➤ Large reduction of the power spectra and average p-loss; scales roughly like asymptotic behaviour.

➤  $\Delta E_{\text{rad}} \approx \Delta E_{\text{el.}}$

# Incoherent Induced Energy Loss

Probability P of energy loss  $\omega$  per unit length (T,M,...):



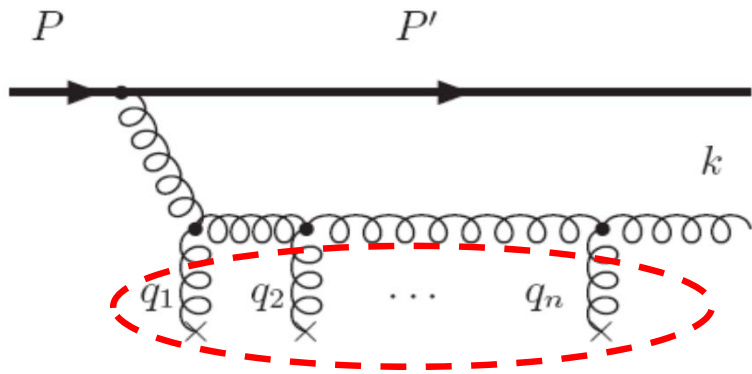
Caveat: no detailed balance implemented yet



# Corrections from Coherence

## Coherent Induced Radiative

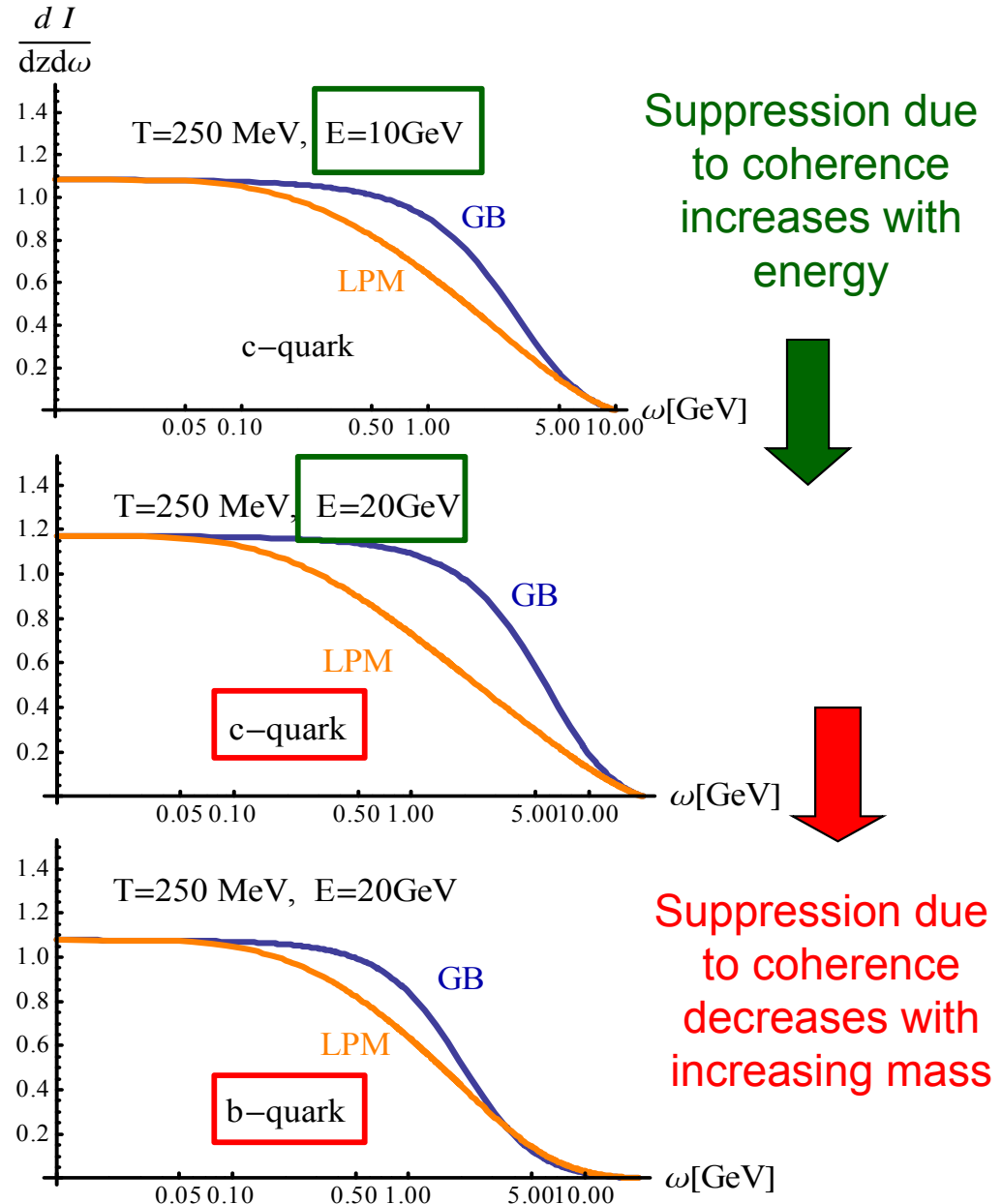
Formation time picture: for  $l_{f,mult} > \lambda$ , gluon is radiated coherently on a distance  $l_{f,mult}$



Model: all  $N_{coh}$  scatterers act as a single effective one with probability  $p_{N_{coh}}(Q_{\perp})$  obtained by convoluting individual probability of kicks

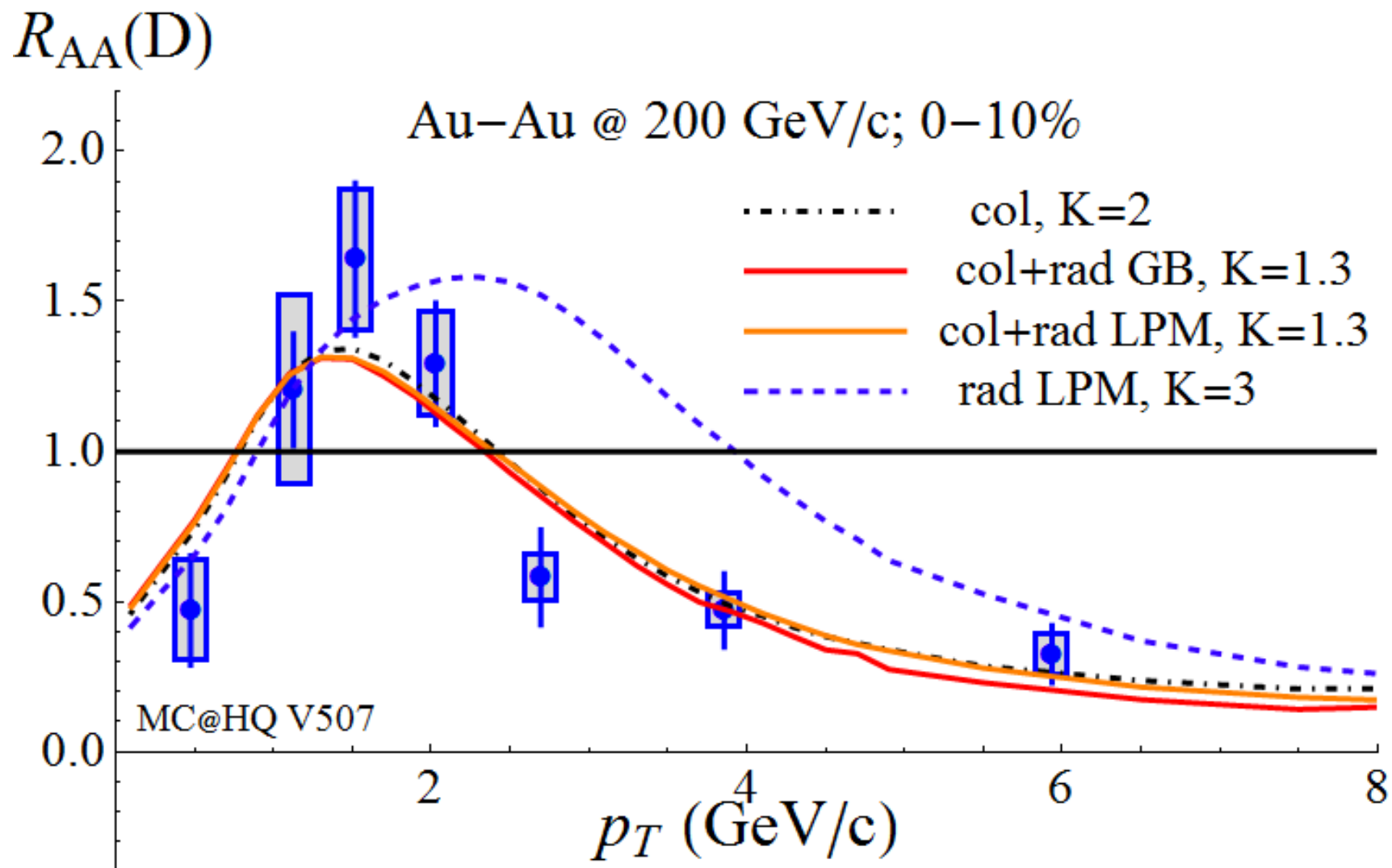
$$\frac{d^2 I_{eff}}{dz d\omega} \sim \frac{\alpha_s}{N_{coh} \tilde{\lambda}} \ln \left( 1 + \frac{N_{coh} \mu^2}{3 (m_g^2 + x^2 M^2 + \sqrt{\omega \hat{q}})} \right)$$

Nuclear Physics A (2013), 301, [arXiv:1209.0844]



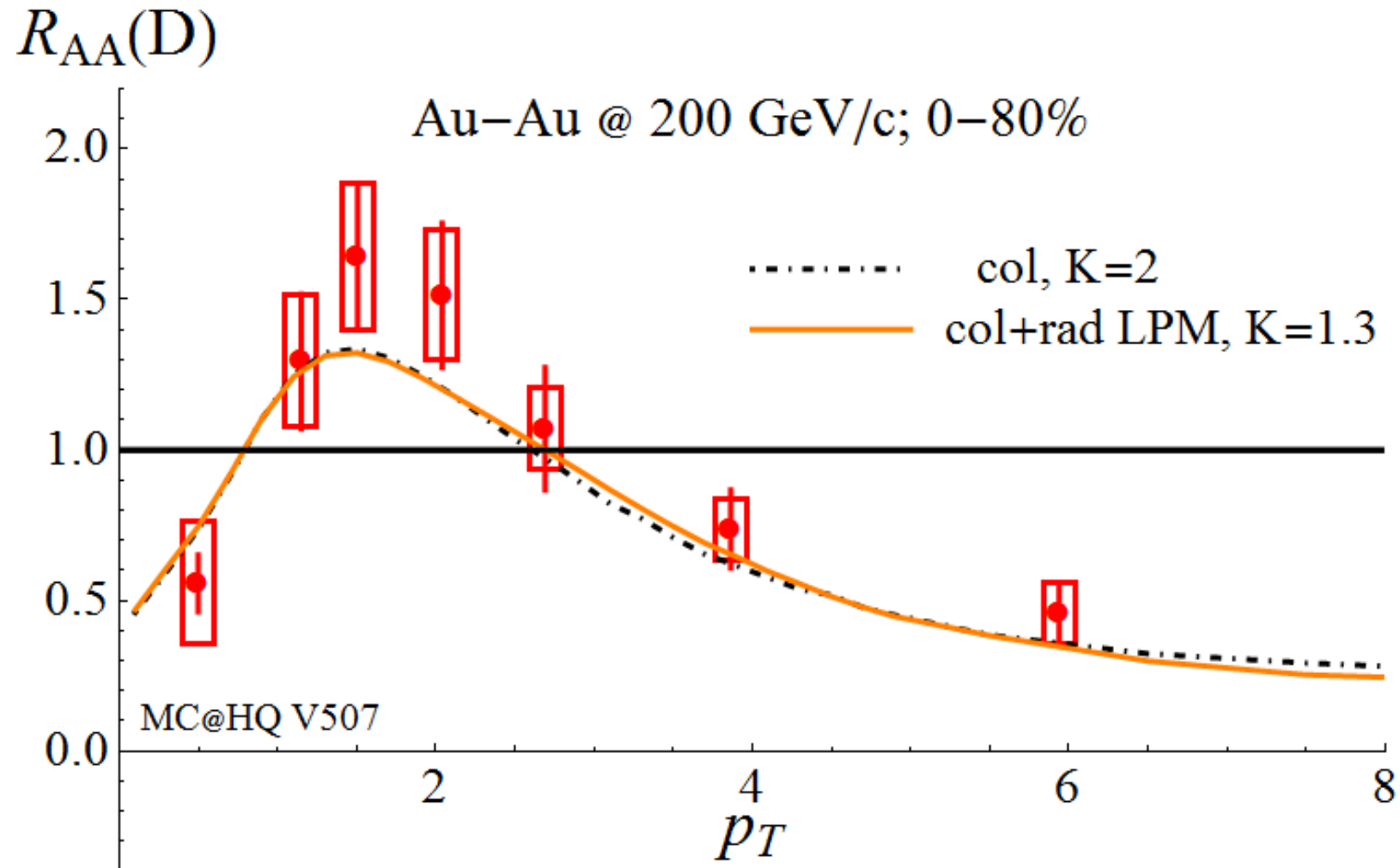
# {Radiative + Elastic} vs Elastic for D mesons @ RHIC

=> Allow for some global rescaling of the rates: “K” fixed on experiment



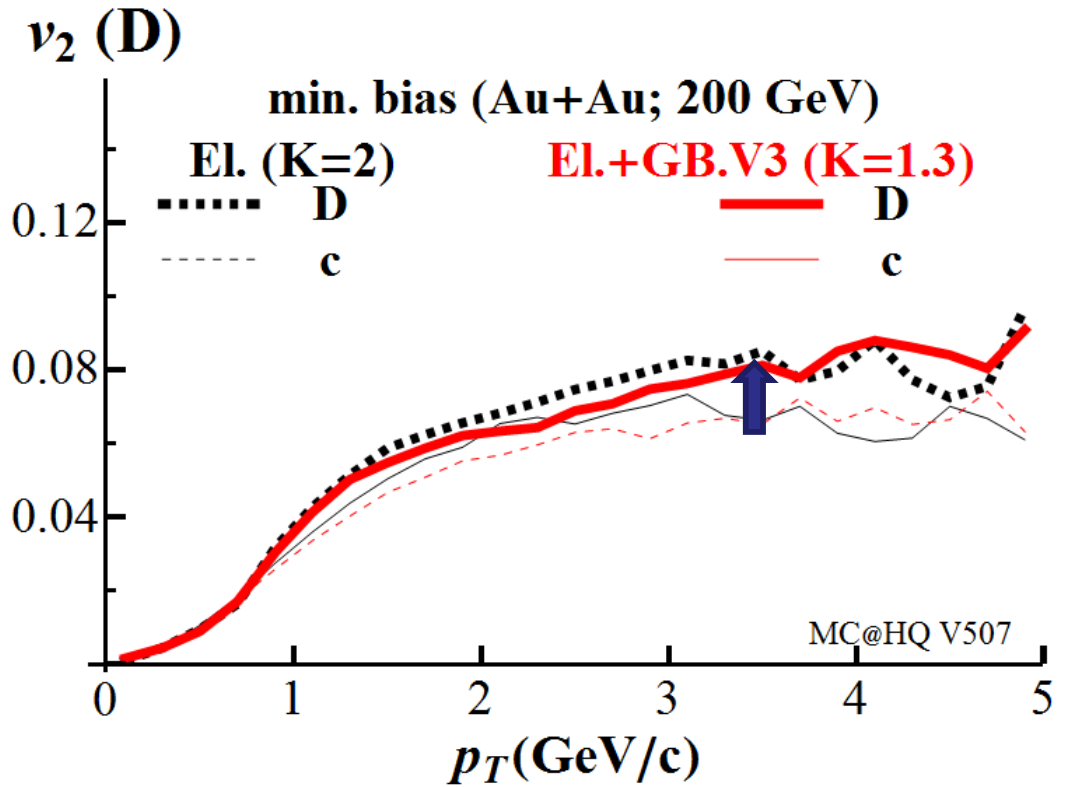
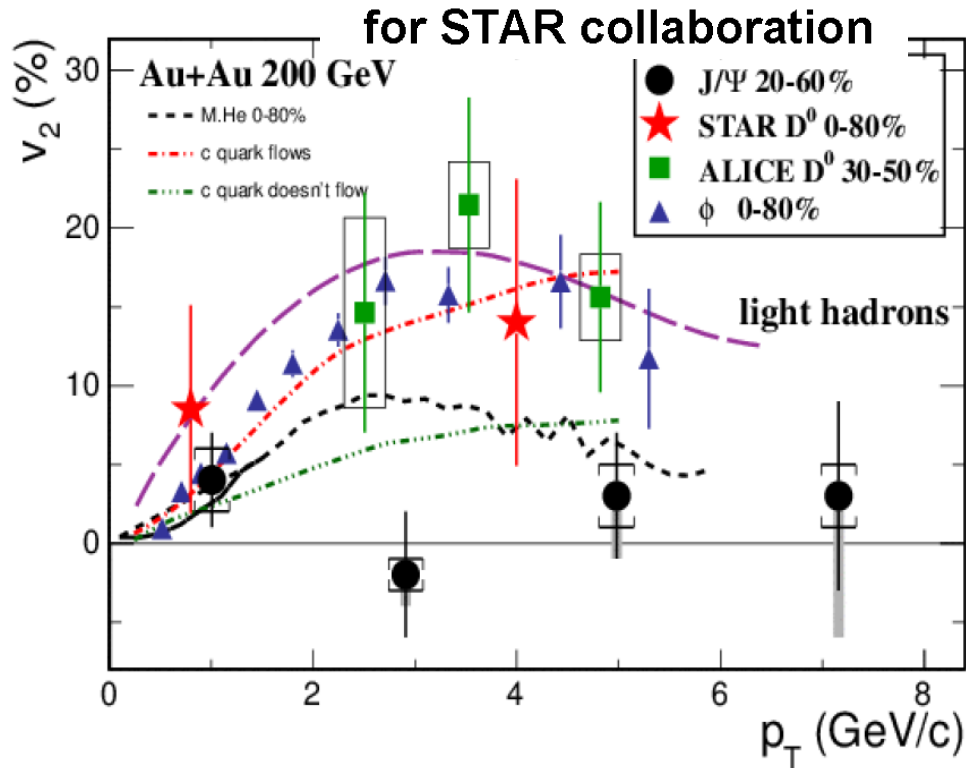
**K coming closer to unity if radiation included**

# {Radiative + Elastic} vs Elastic for D mesons @ RHIC



# {Radiative + Elastic} vs Elastic for D mesons @ RHIC

Jaroslav Bielčík



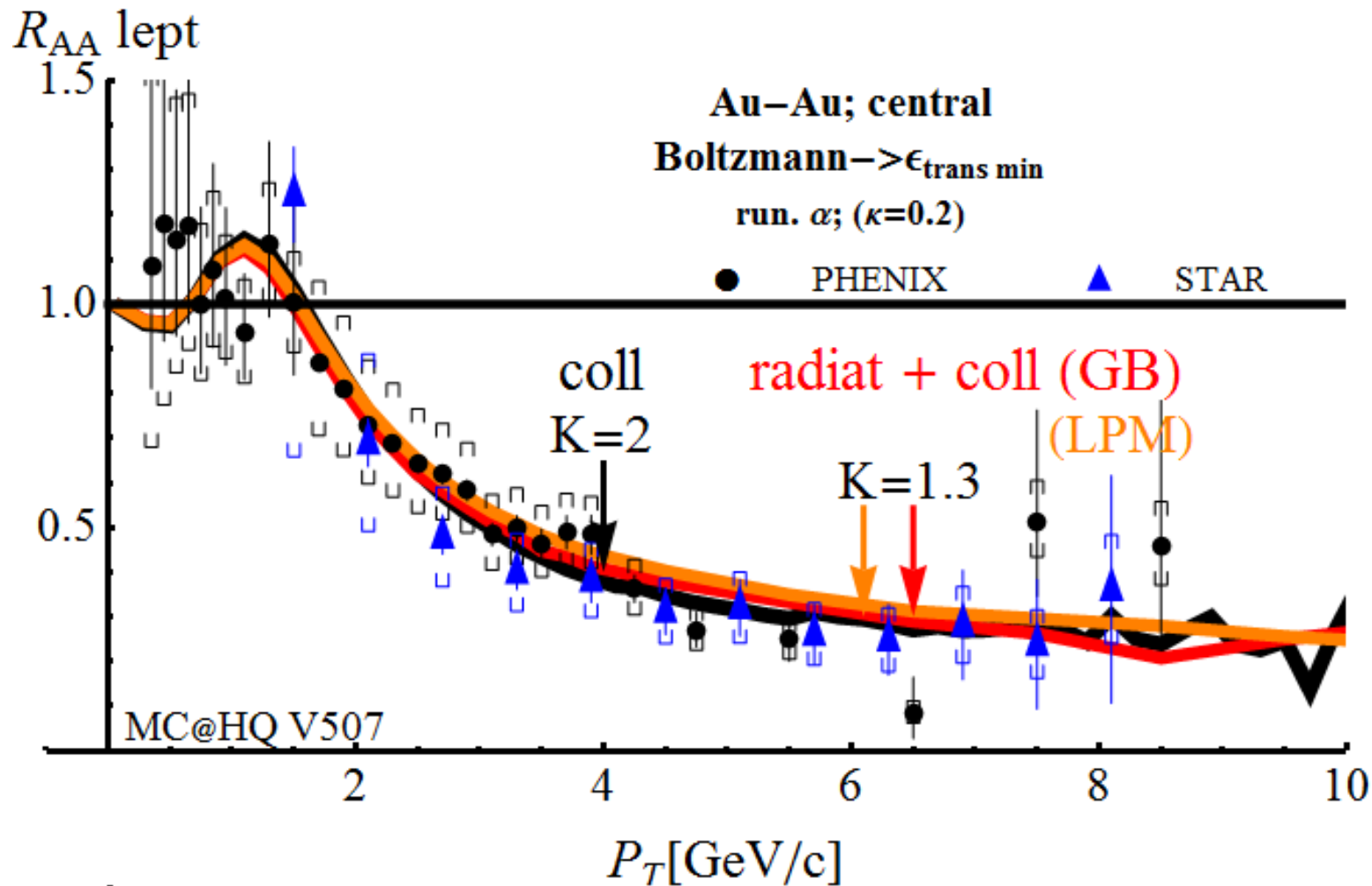
Rather little contribution from the light quark in our treatment... but conclusion may depend on the parameters ( $m_q$ , wave function)

Coalescence according to extended Dover framework

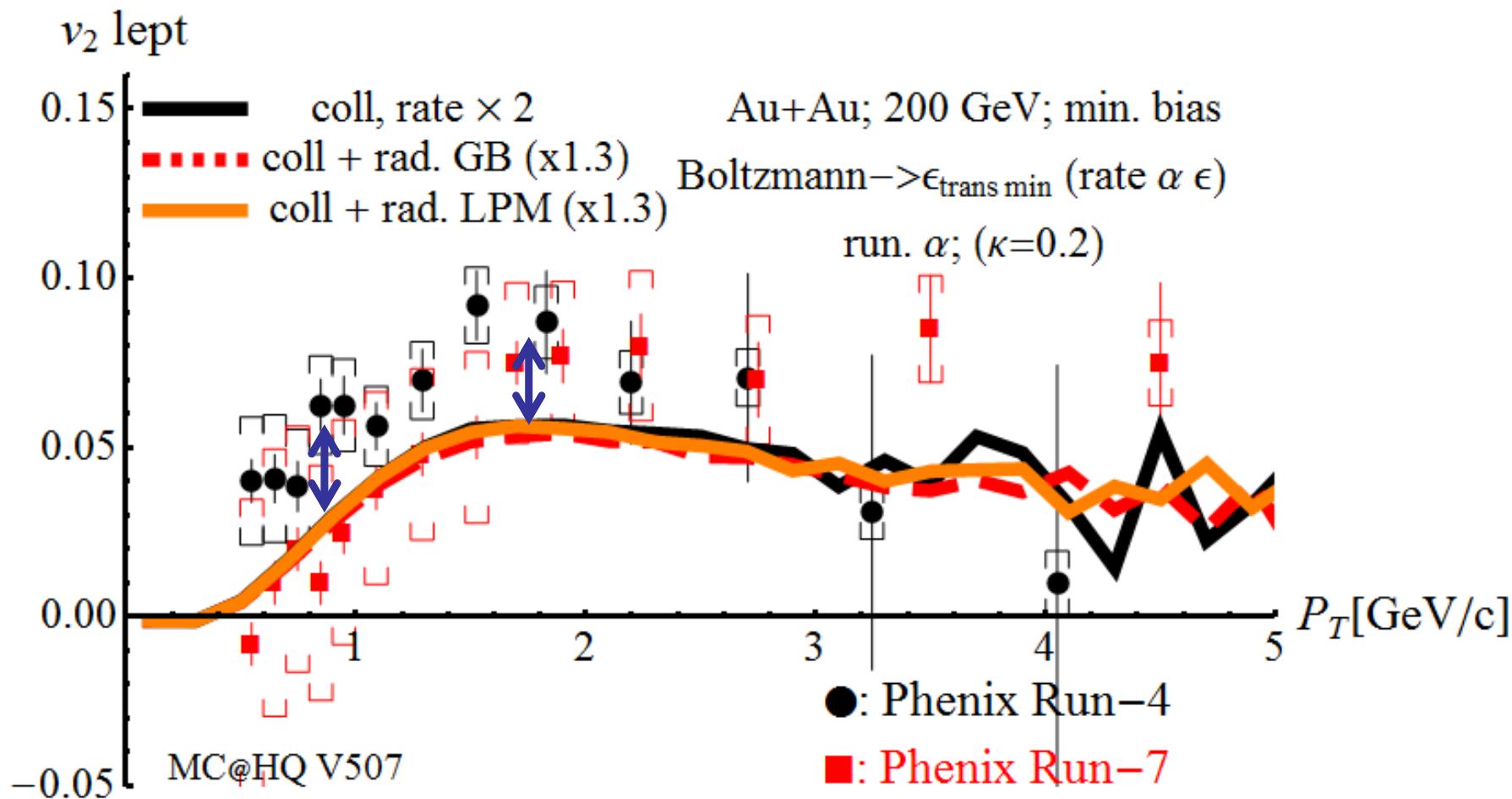
(PRC 79 044906)

$$N_{\Phi} = \int \frac{d^3 p_q}{(2\pi\hbar)^3} \frac{p_q \cdot \hat{d}\sigma}{E_q u_Q \cdot \hat{d}\sigma} f_q(x_Q, p_q) (\sqrt{2\pi} R_c)^3 \times F_{\Phi}(p_Q, p_q),$$

# {Radiative + Elastic} vs Elastic for leptons @ RHIC



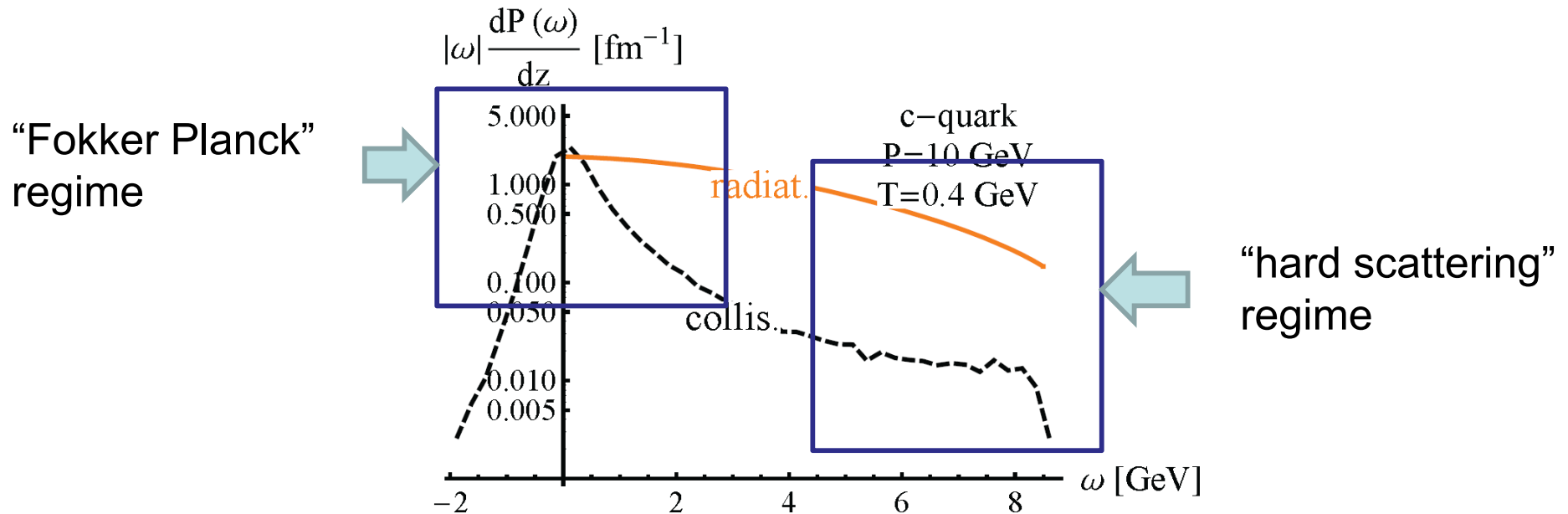
# {Radiative + Elastic} vs Elastic for leptons @ RHIC



**El. + rad: No lack of elliptic flow wrt pure (rescaled) elastic processes (!?)**

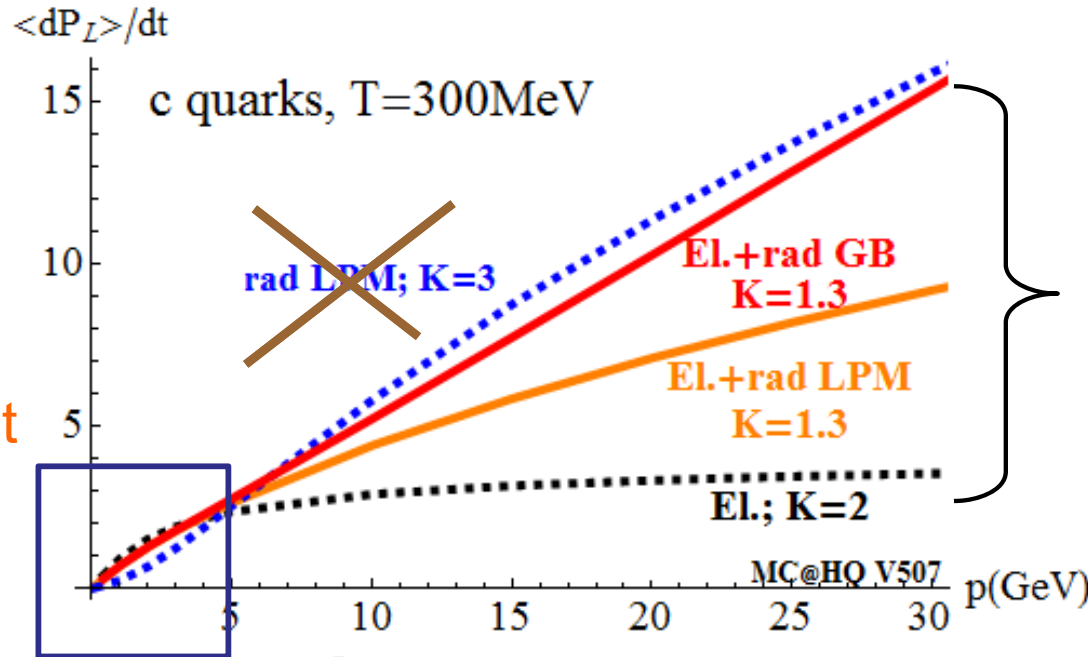
# Conclusions from RHIC

- Good consistency between NPSE and D mesons (10% difference in K values)...
- ... within a model with mass hierarchy
- $\Delta E$  radiative  $<$   $\Delta E$  elastic
- Present data at RHIC cannot decipher between the 2 local microscopic E-loss models (elastic, elastic + radiative GB)  $\Rightarrow$  Not sensitive to the large- $\omega$  tail of the Energy-loss probability (thanks to initial HQ distribution)



# QGP properties from HQ probe at RHIC

Gathering all *rescaled* models (*coll. and radiative*) compatible with RHIC  $R_{AA}$ :



Similar diffusion coefficient at low  $p$

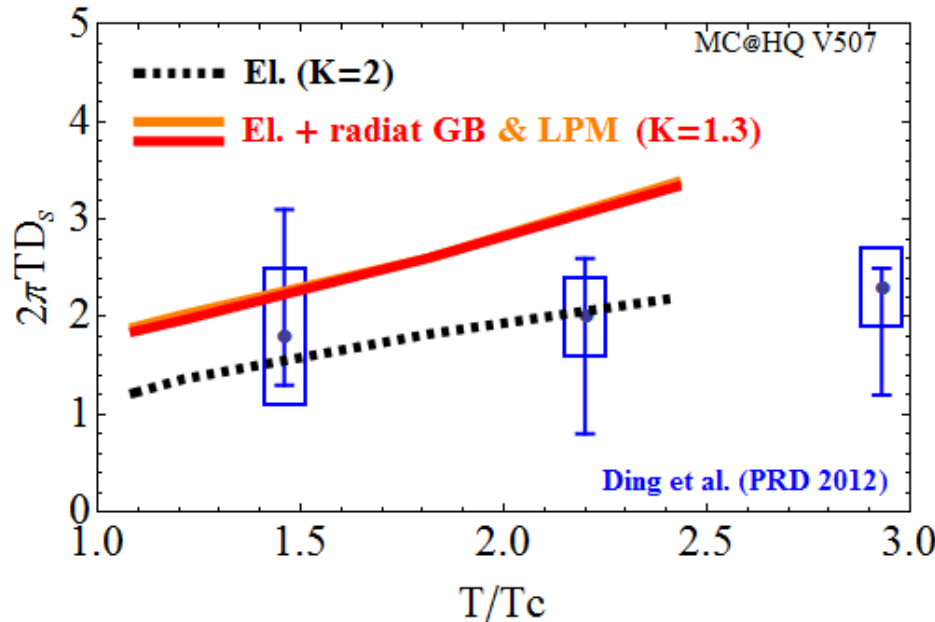
the drag coefficient reflects the average momentum loss (per unit time)  $\Rightarrow$  large weight on  $x \sim 1$

Present RHIC experiments cannot resolve between those various trends

**Hope that LHC can do !!!**

We extract it from data (starting from SQM 2008)

We compare with recent lattice results



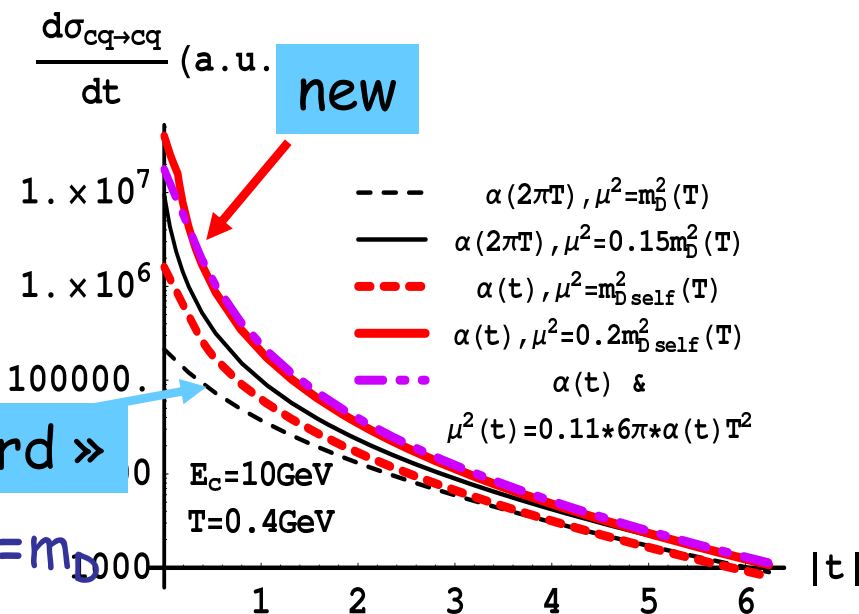
**Main message**

It is possible to reveal some fundamental property of QGP using HQ probes



# Perspectives

**Qq->Qq**



« standard »

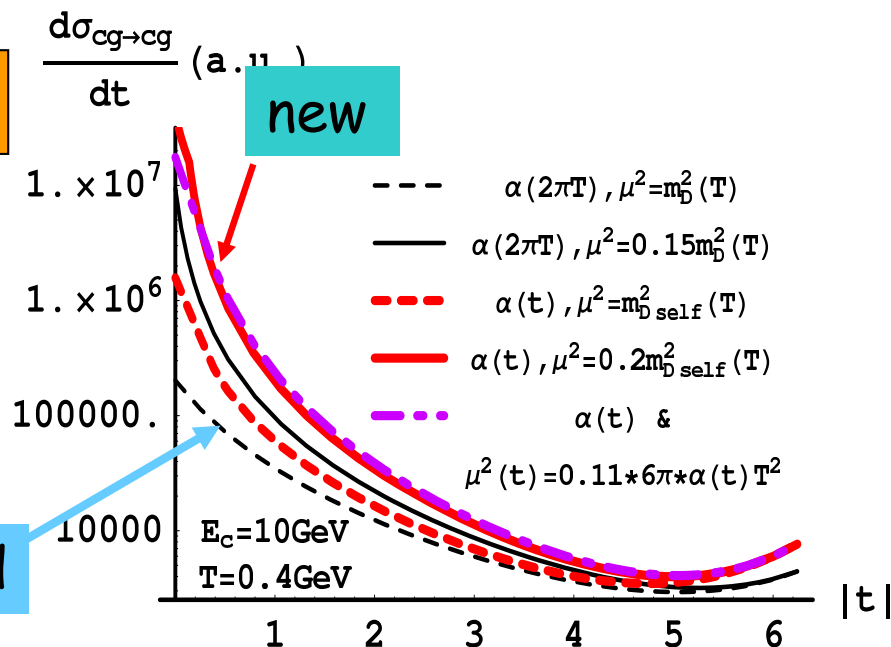
$\alpha(2\pi T), \mu = m_D$

Large enhancement of both cross sections at small and intermediate  $|t|$

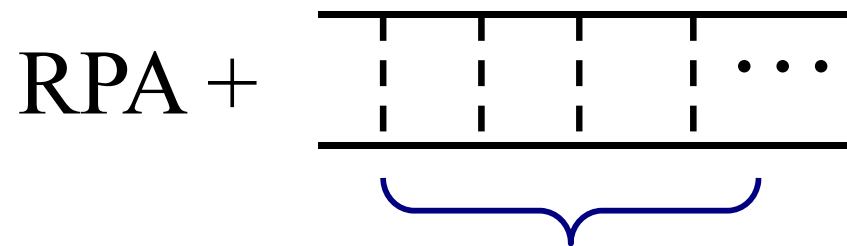
Little change at large  $|t|$

N.B: Non perturbative aspects (beyond Born). Usually in convergent kinetic:

**Qg->Qg**



standard

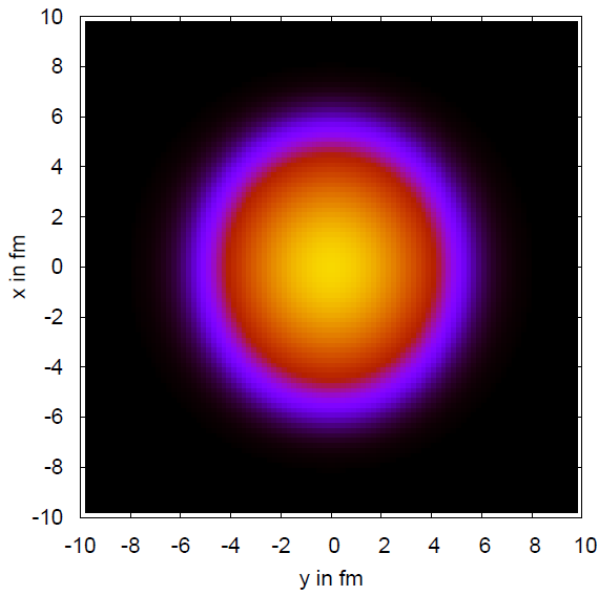


Ladders necessary at short distance (large force)

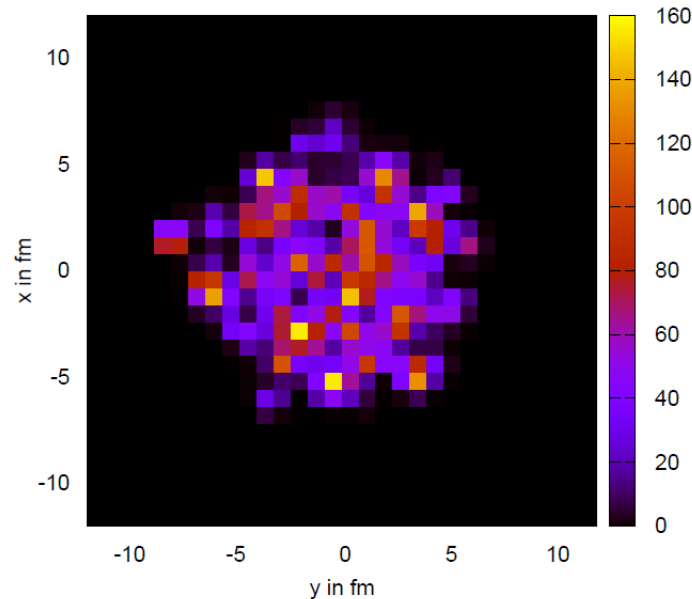
# Nowadays: EPOS as a background for MC@sHQ (K.Werner, M. Nahrgang, B. Guiot, V. Ozvenchuk)

EPOS: state of the art framework that encompass pp, pA and AA collisions

Initial energy density @ RHIC (central Au-Au)



Kolb Heinz (used previously)



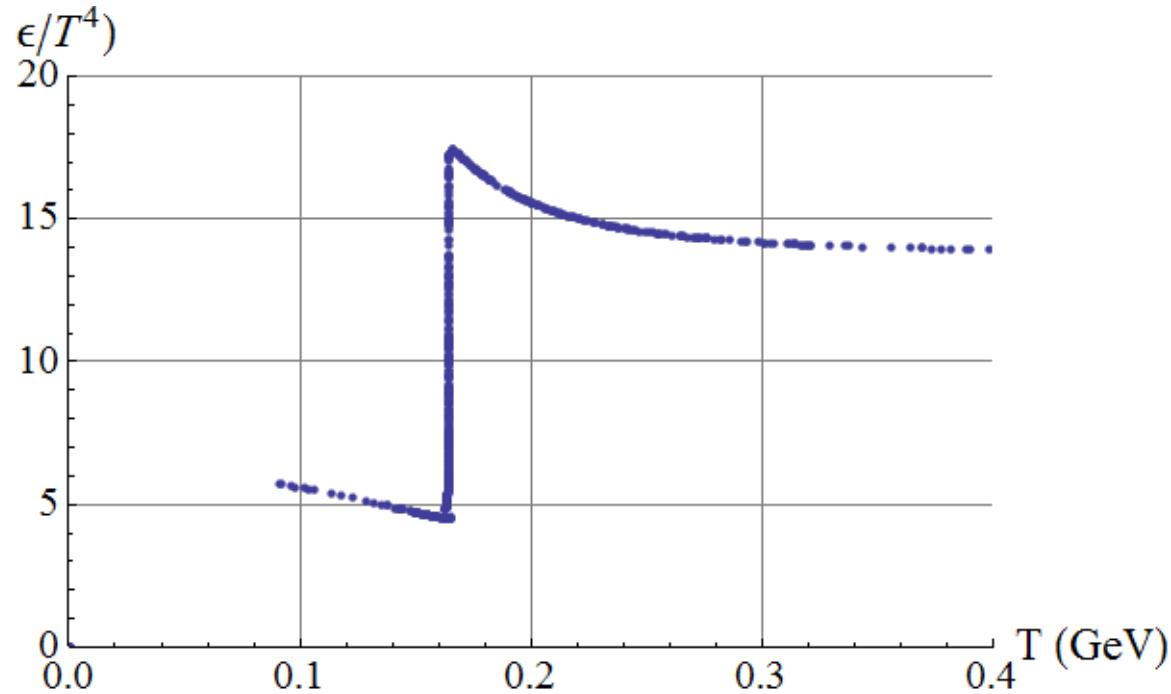
EPOS

Beware:  $\neq$  color scales

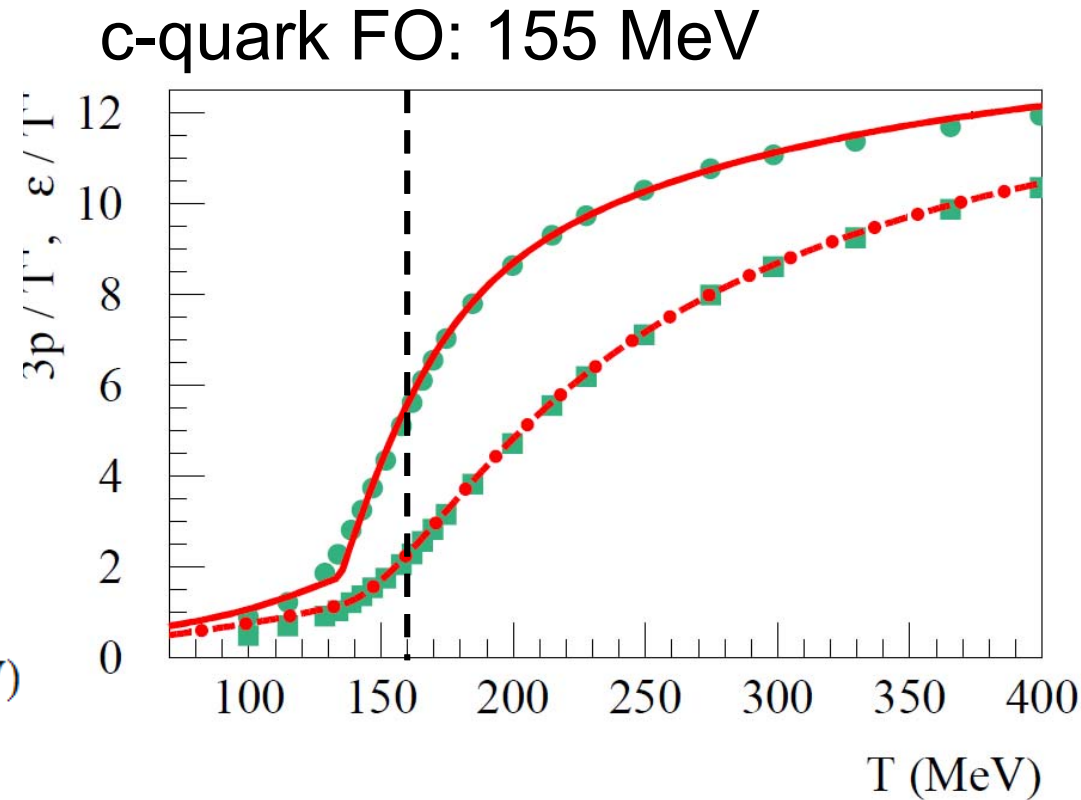
More realistic hydro and initial conditions => original HQ studies such as:

- 1) fluctuations in HQ observables (some HQ might « leak » through the « holes » in the QGP)
- 2) correlations between HF and light hadrons

# Large differences in the EOS !

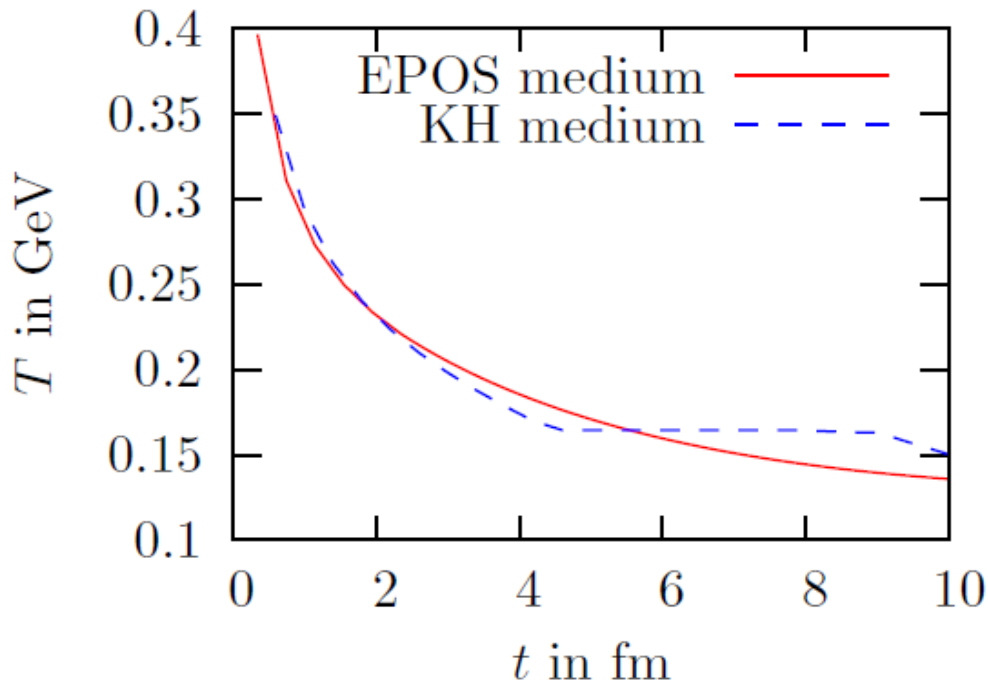


Kolb Heinz: bag model  
(1st order transition  
btwn hadronic phase  
and massless partons)

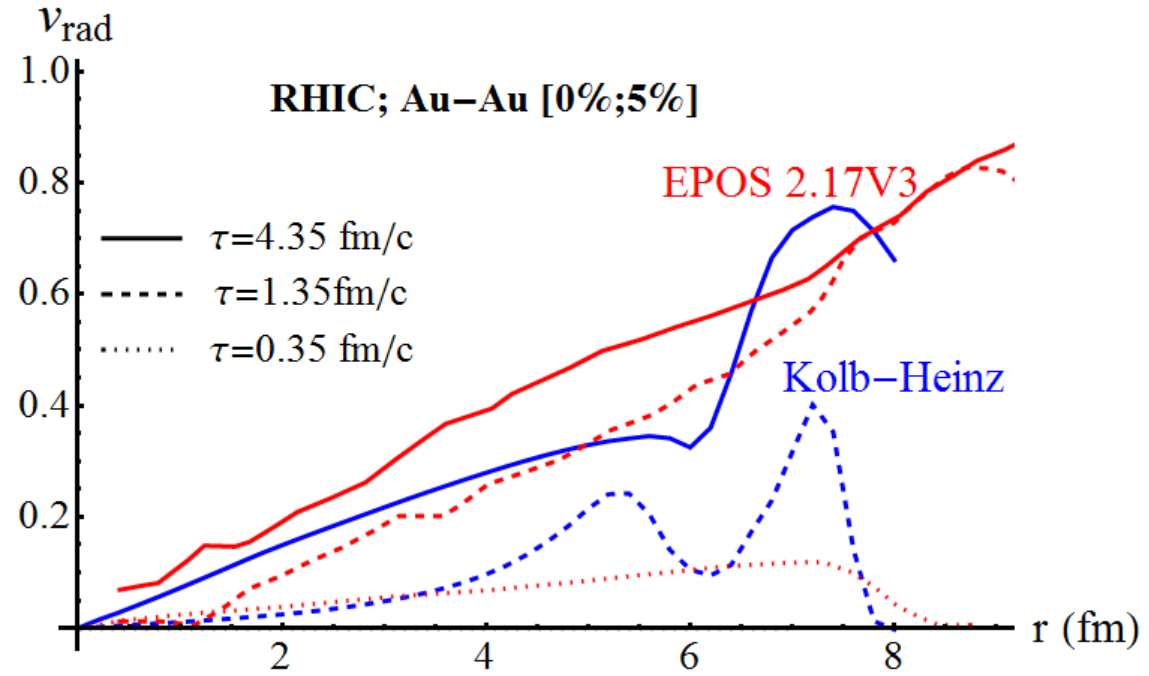


EPOS2: fitted on the  
lattice data from the  
Wuppertal-Budapest  
collaboration

# Medium comparison at RHIC



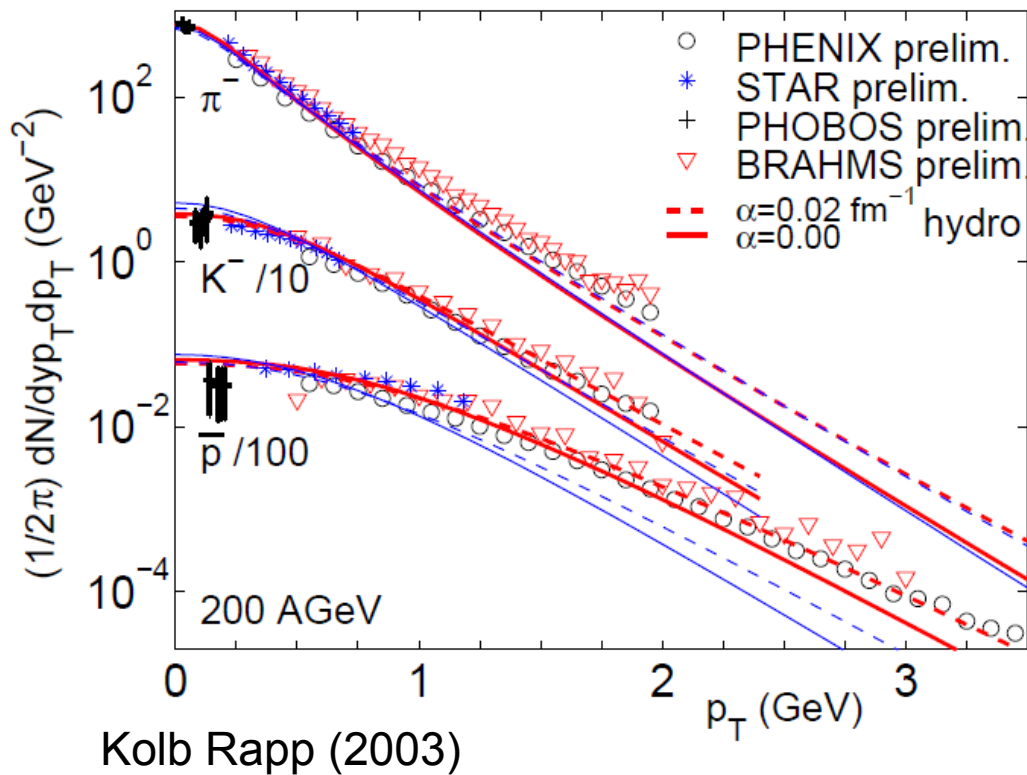
Gross features of  $T$ -evolution  
are identical in the  
« plasma » phase ( $T > 200$   
MeV)



Radial velocities differ  
significantly, starting from the  
earliest times in the evolution

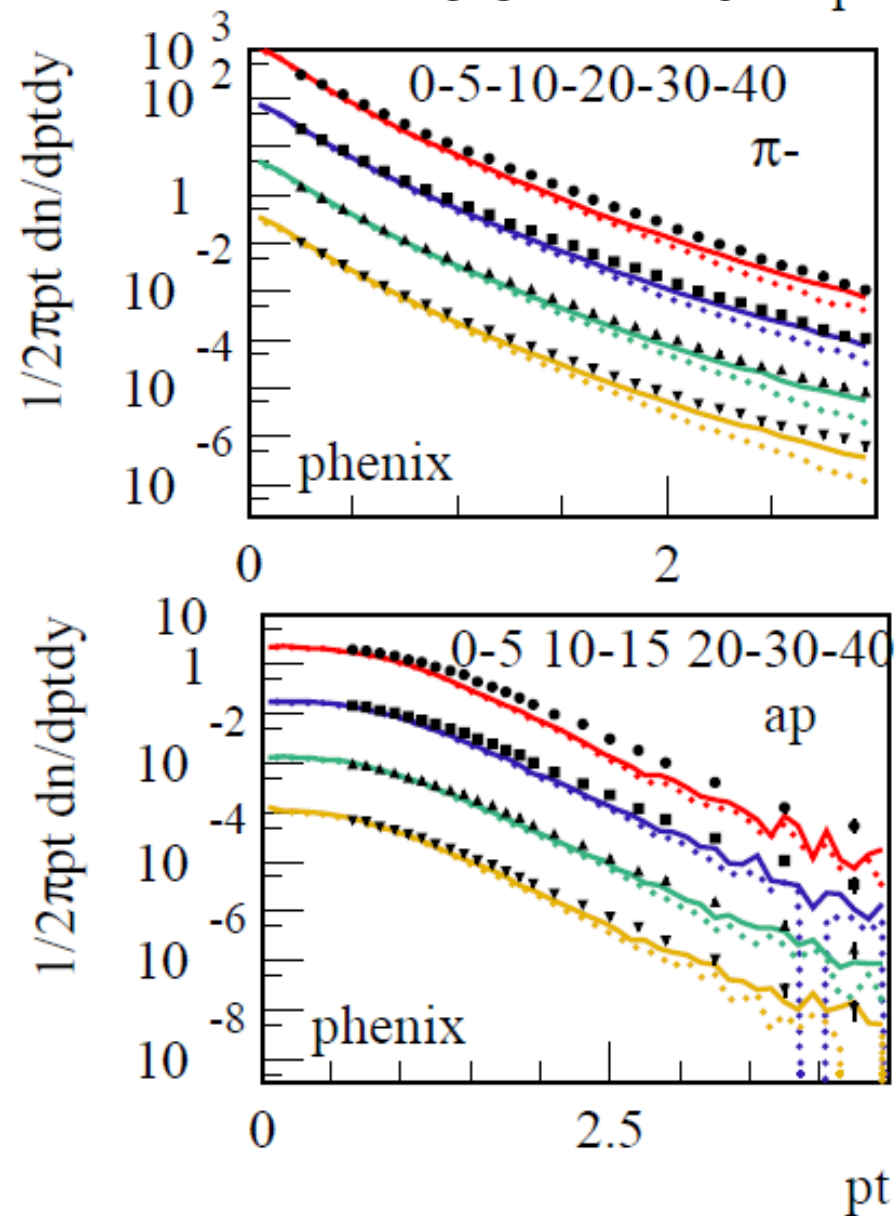
# Identified particles spectra at RHIC

## Kolb-Heinz



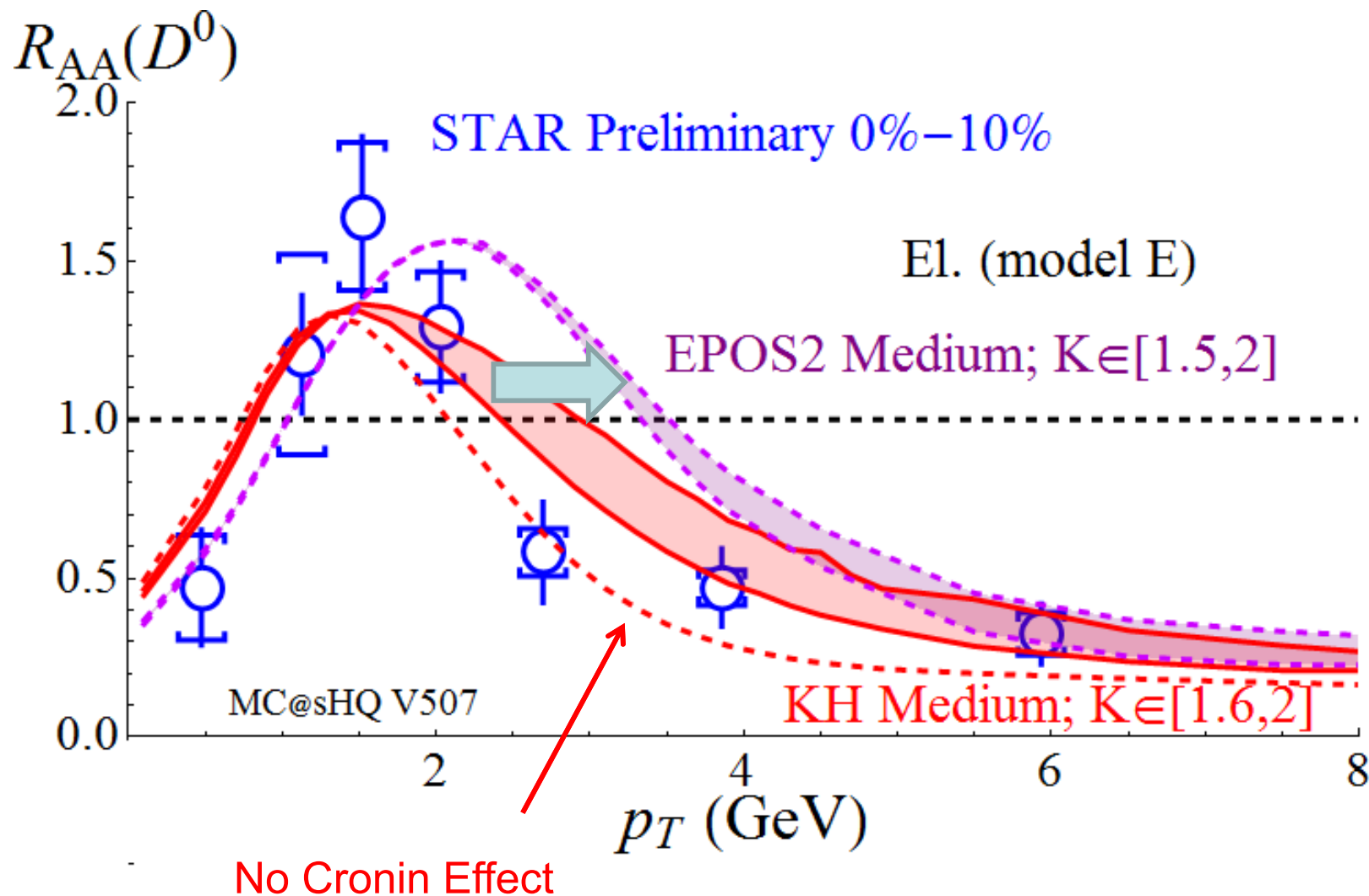
better agreement if  
 initial flow ( $v_r = \tanh(0.02 r)$ )

## EPOS2.17V3

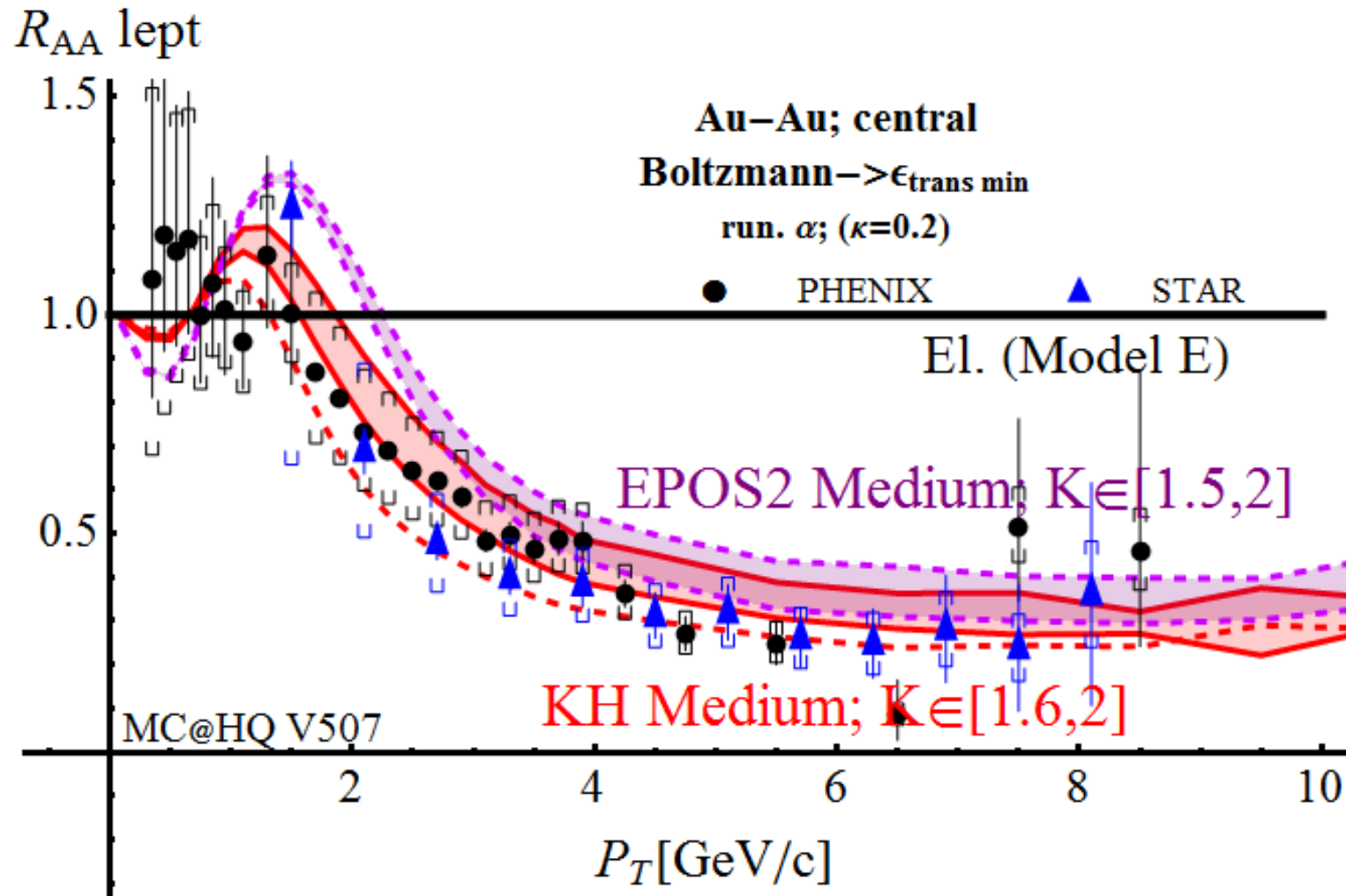


# Elastic D mesons @ RHIC

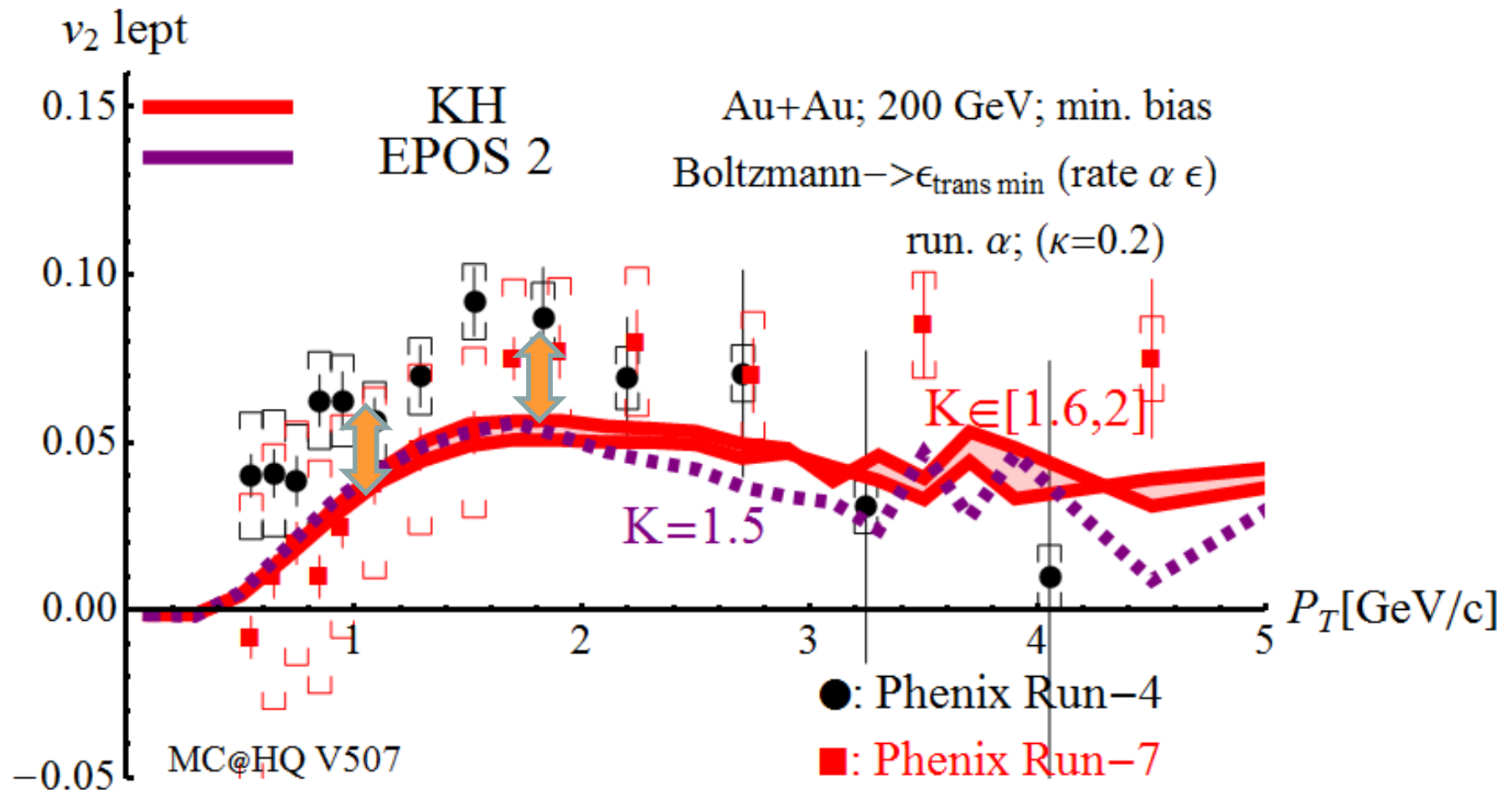
=> Allow for some global rescaling of the rates: “K” fixed on experiment



# Elastic for leptons @ RHIC



# {Radiative + Elastic} vs Elastic for leptons @ RHIC



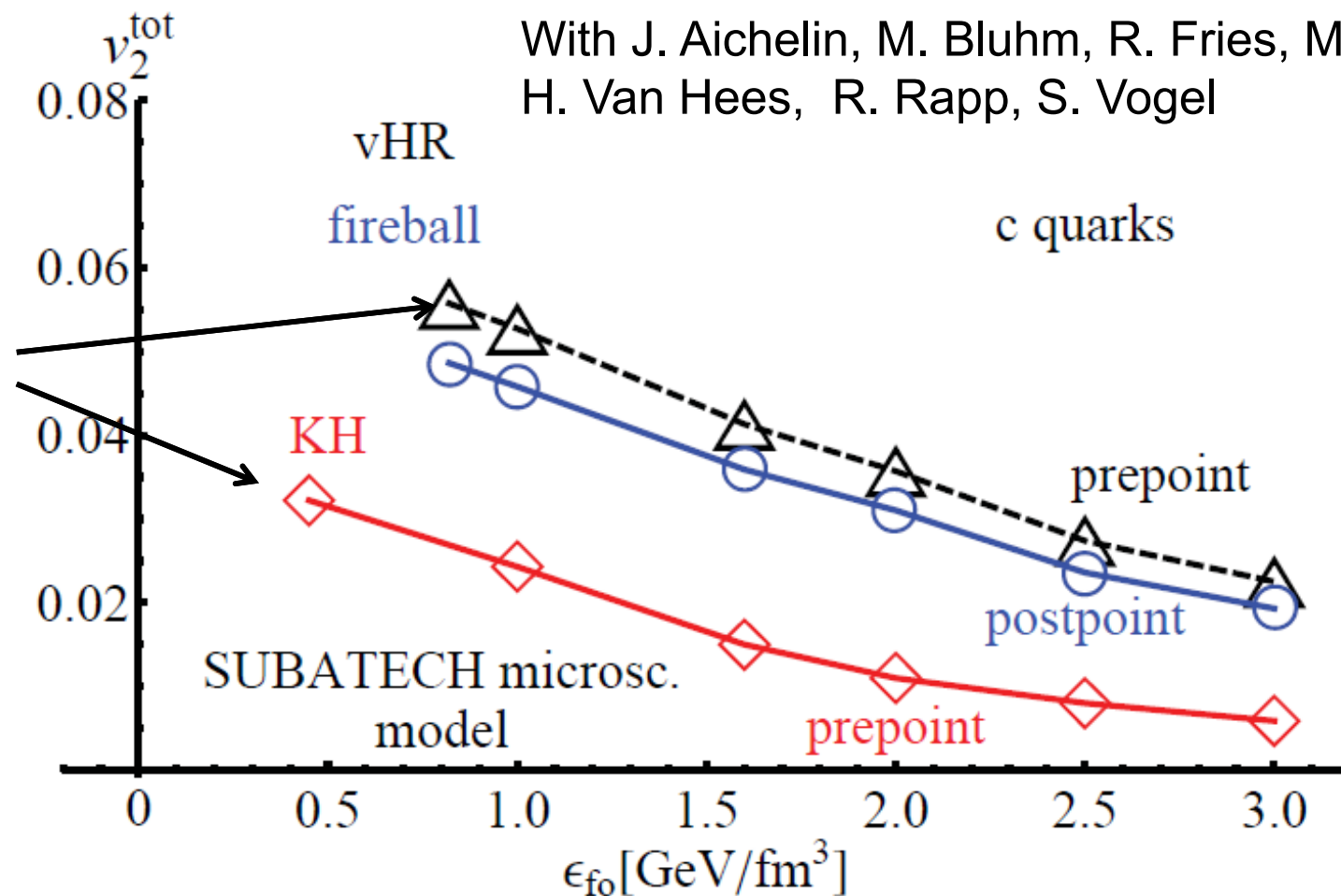
Rather systematic underestimation of the  $v_2$ ... sign for a significant D mesons rescattering in hadronic matter ?



# {Radiative + Elastic} vs Elastic for leptons @ RHIC

With J. Aichelin, M. Bluhm, R. Fries, M. He,  
H. Van Hees, R. Rapp, S. Vogel

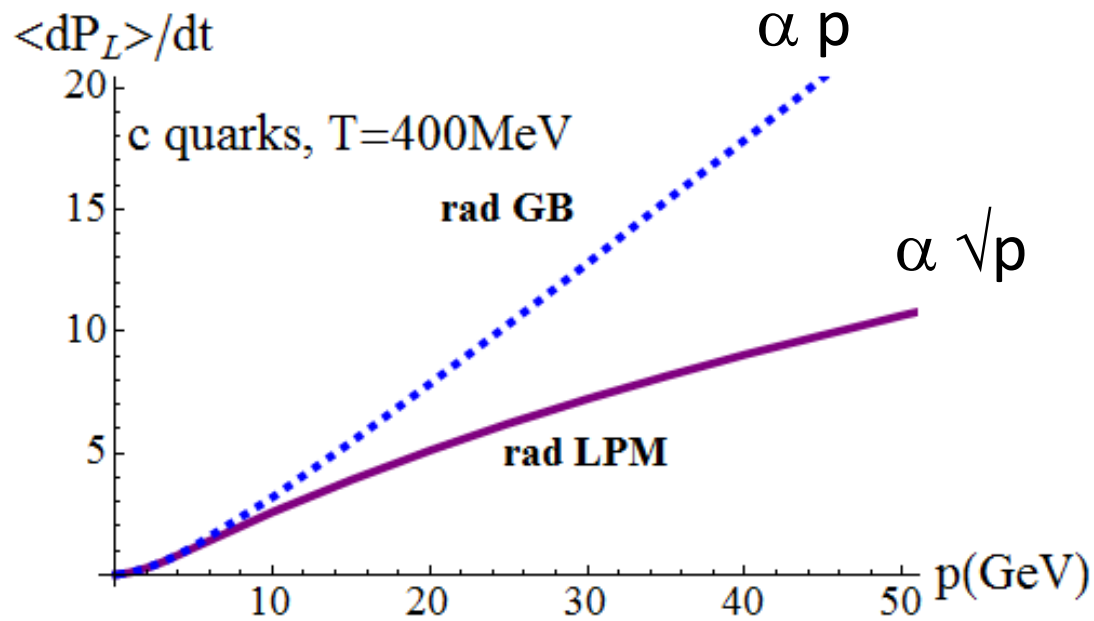
**V2 builds continuously with time (large inertia) => support the need for studying the D-mesons interactions in hadronic matter**



**Alternative “exotic” explanation: early v2 => fundamental issue of initial state conditions in AA collisions**

**Having the hadronic sector under control (FAIR) will help constraining the “exotic” explanation => important cross-talk between FAIR & RHIC-LHC**

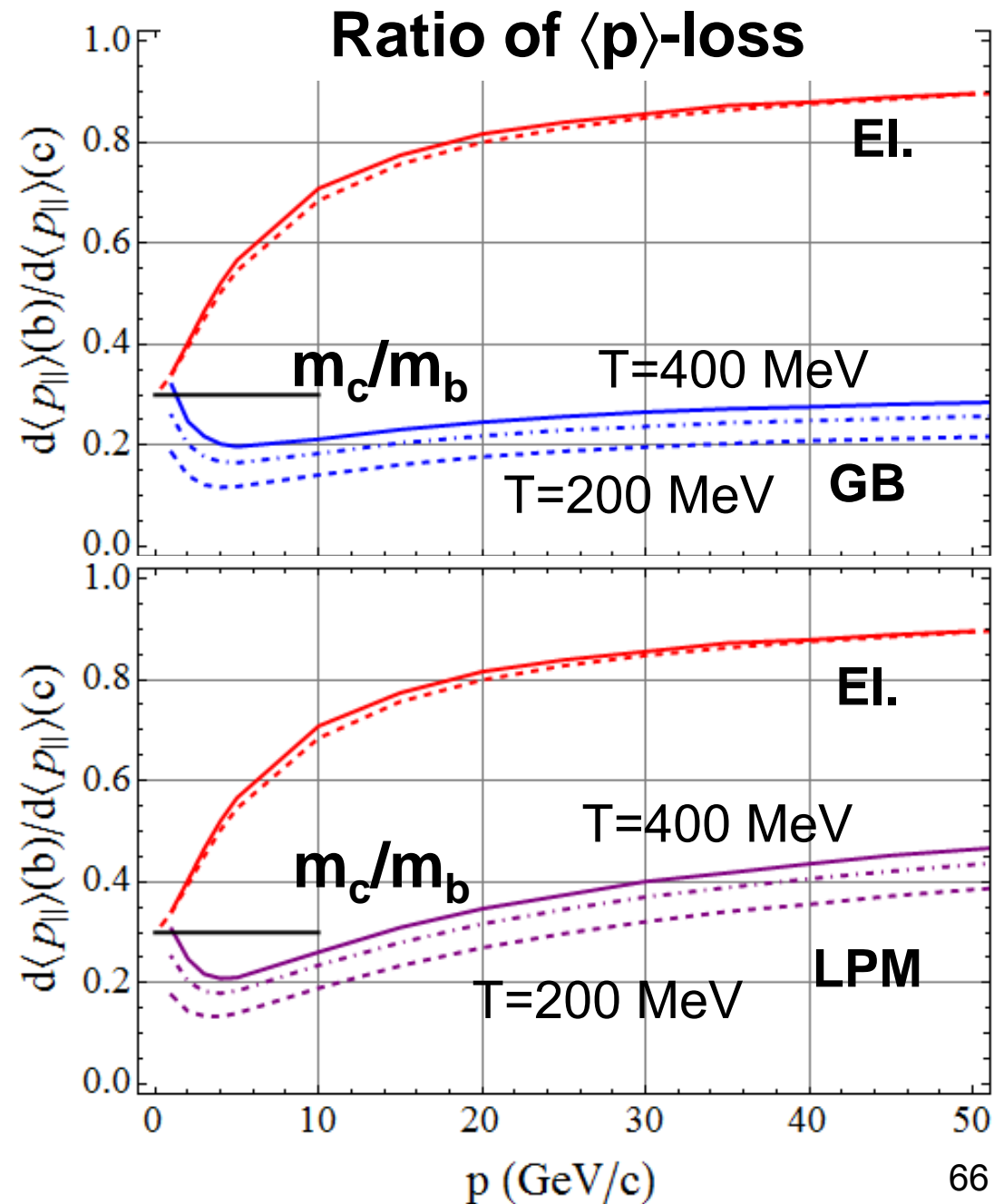
# Radiative Momentum Loss with Running $\alpha_s$ $d\sigma_{el}$



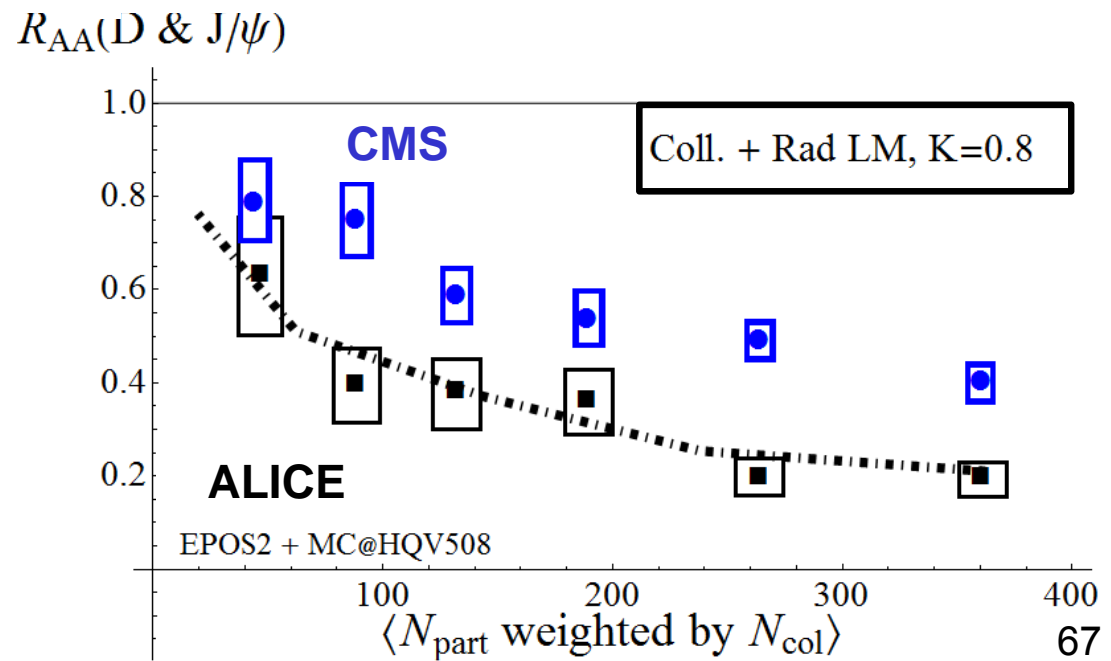
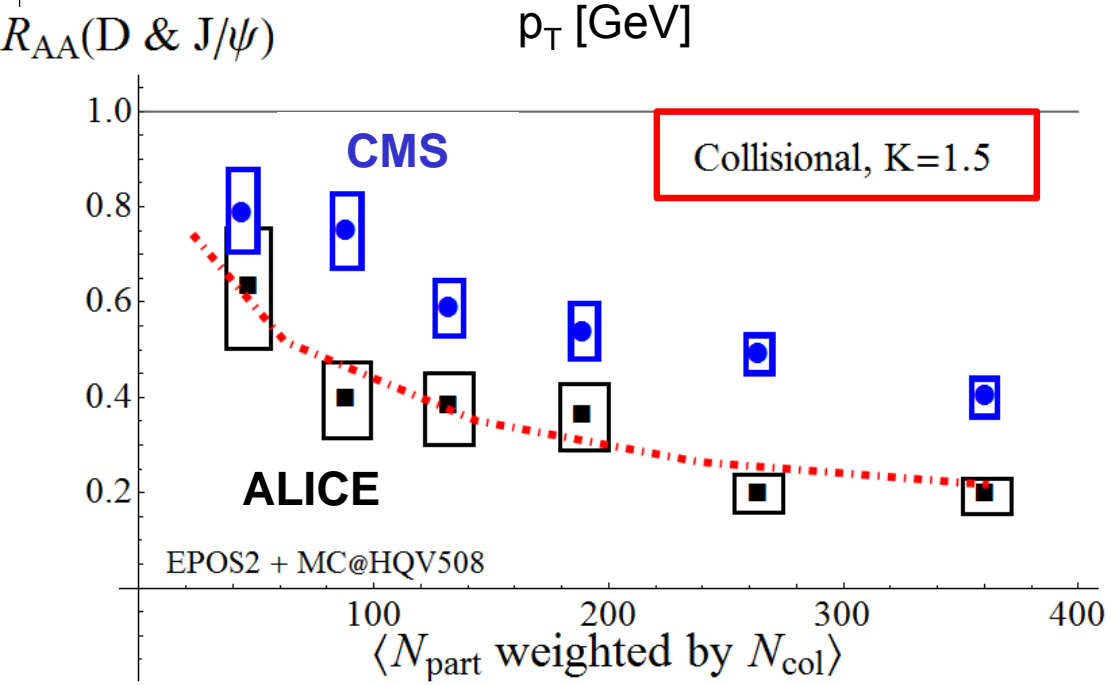
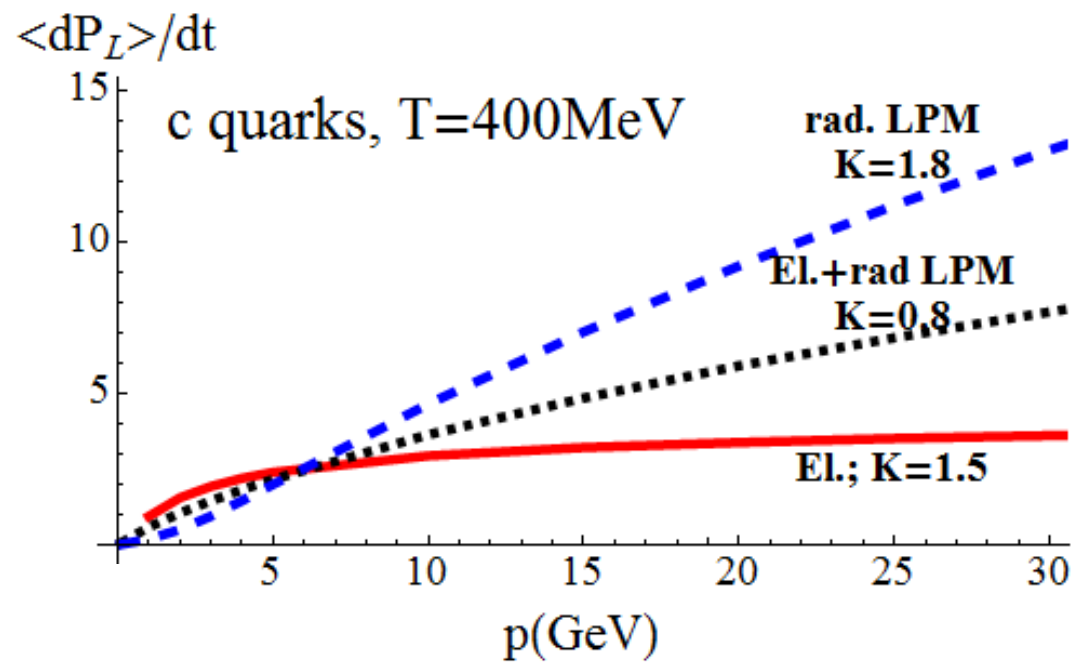
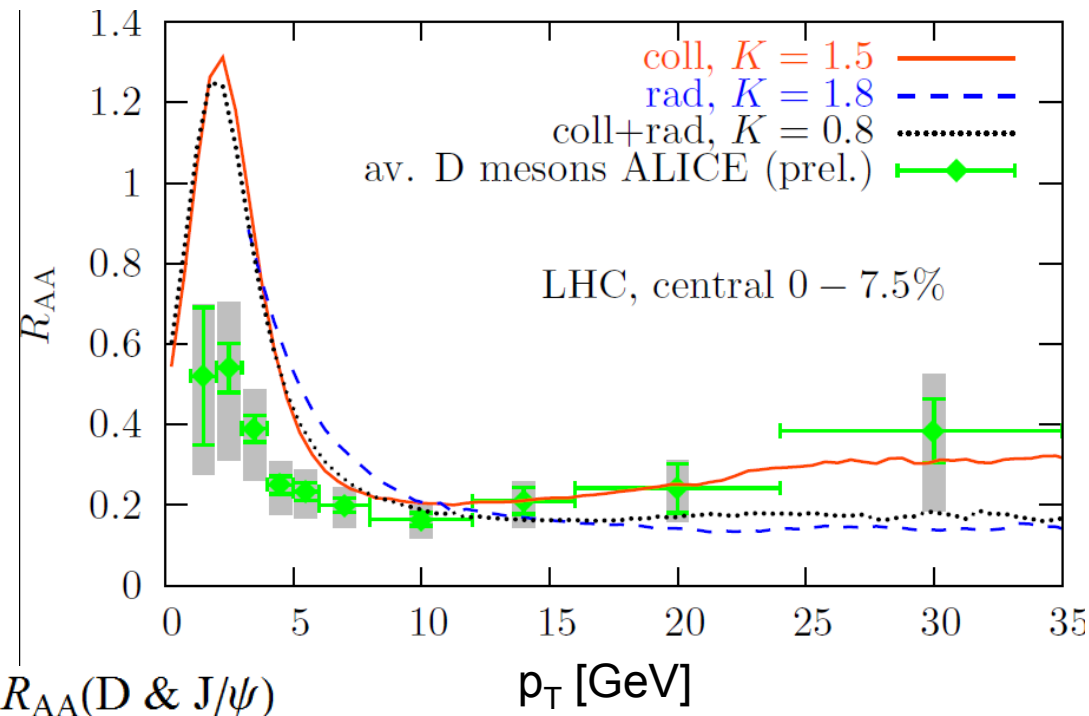
**Mass hierarchy:**

**Elastic < rad LPM < rad GB**

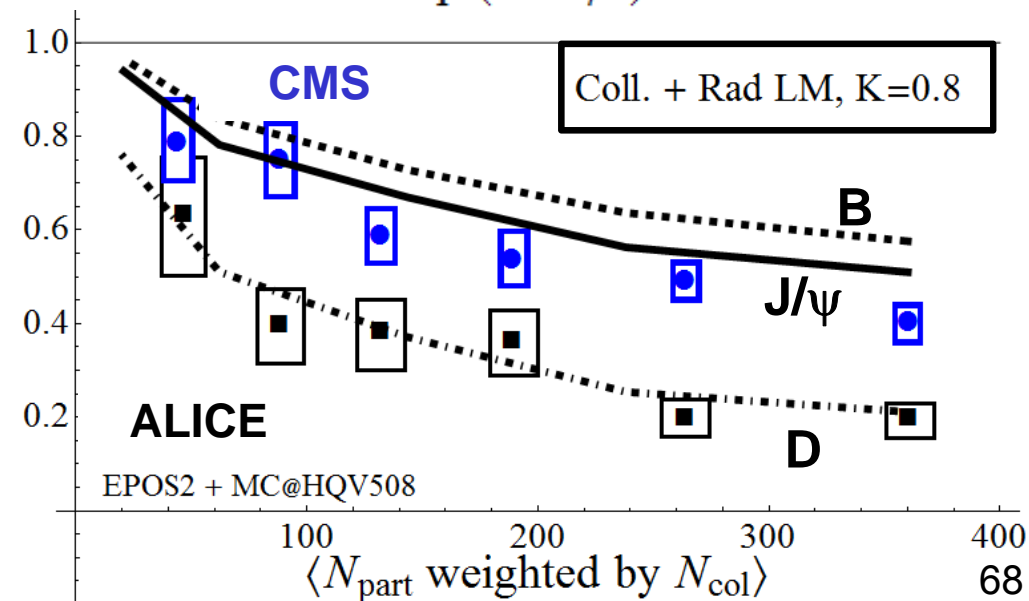
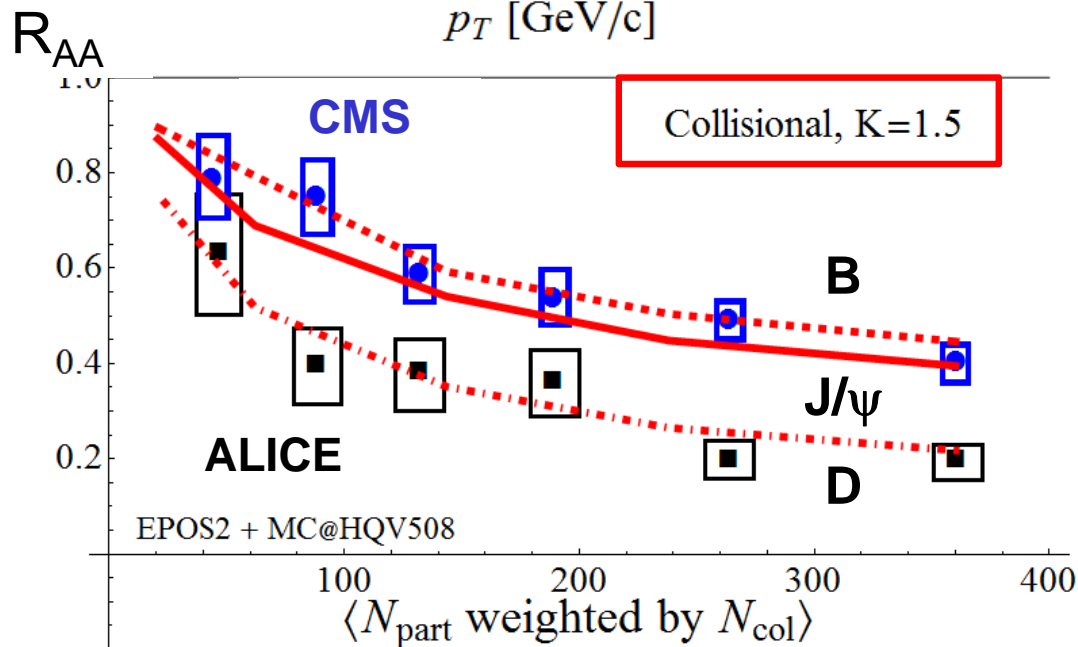
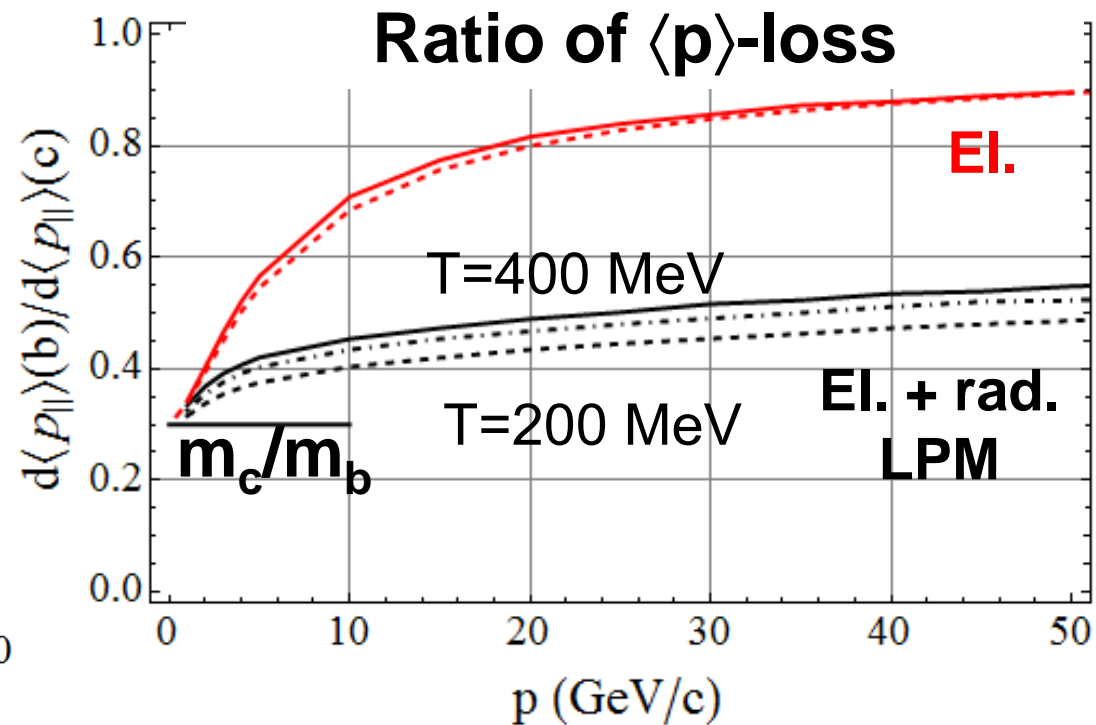
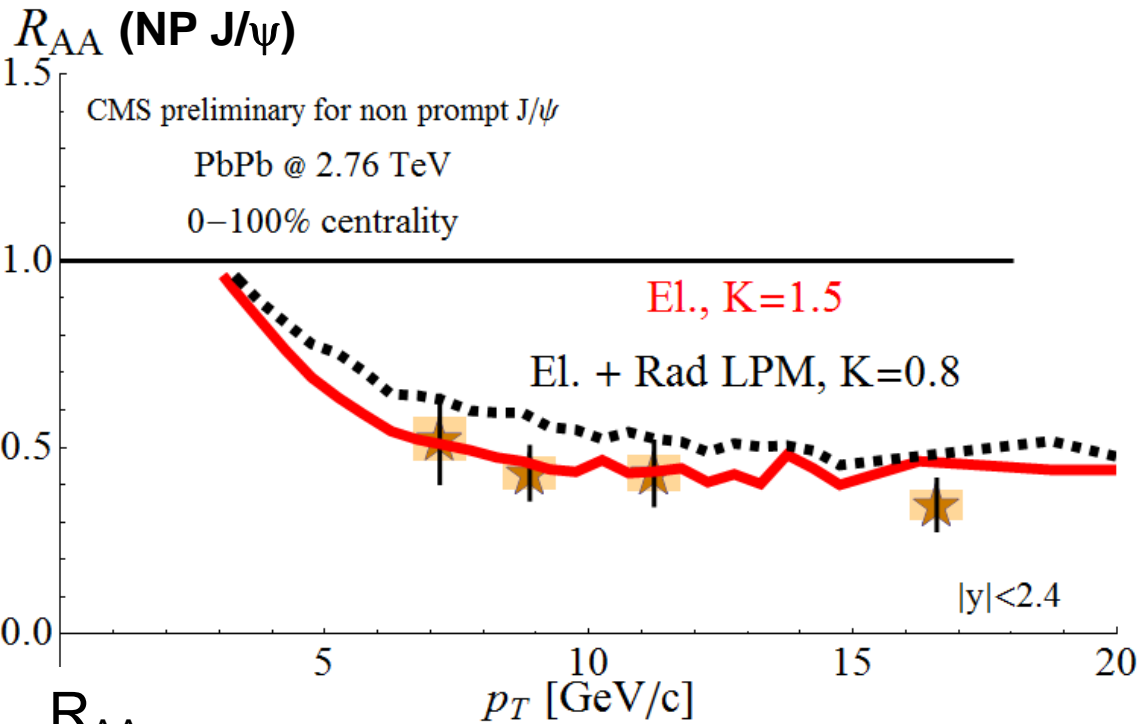
**Best seen at the LHC**



# Contact with LHC Data: a) for c-Quarks...



# ... b) for b-Quarks (& Non-Prompt J/ψ)

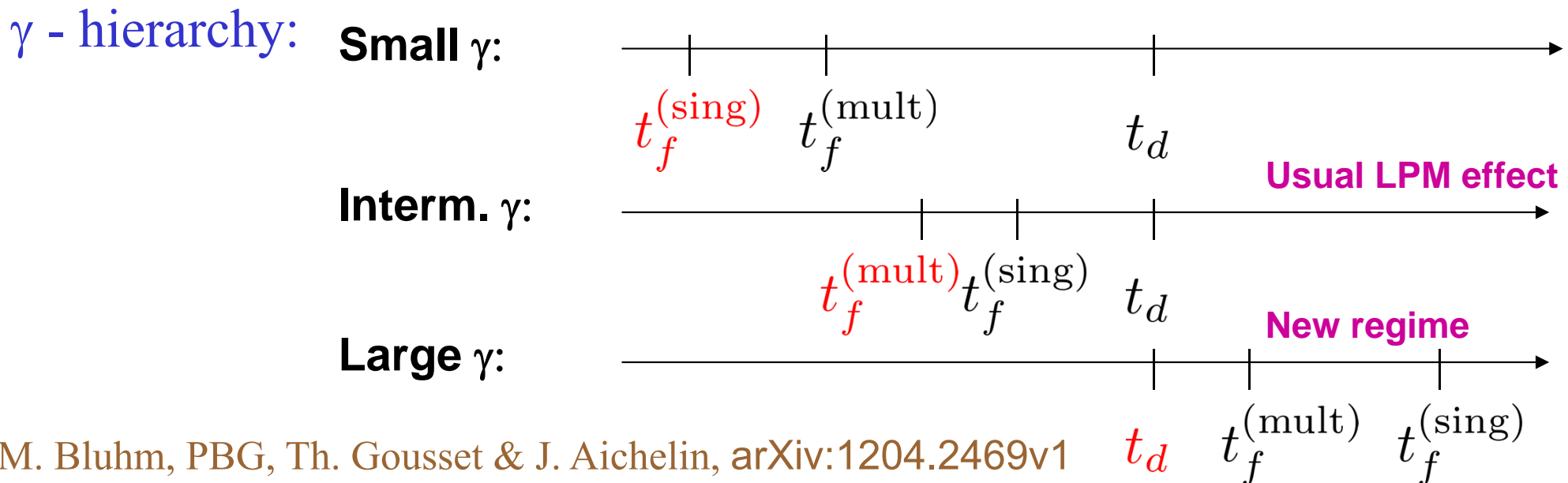


# Consequences of radiation damping on energy loss; with J. Aichelin, Th. Gousset and M. Bluhm

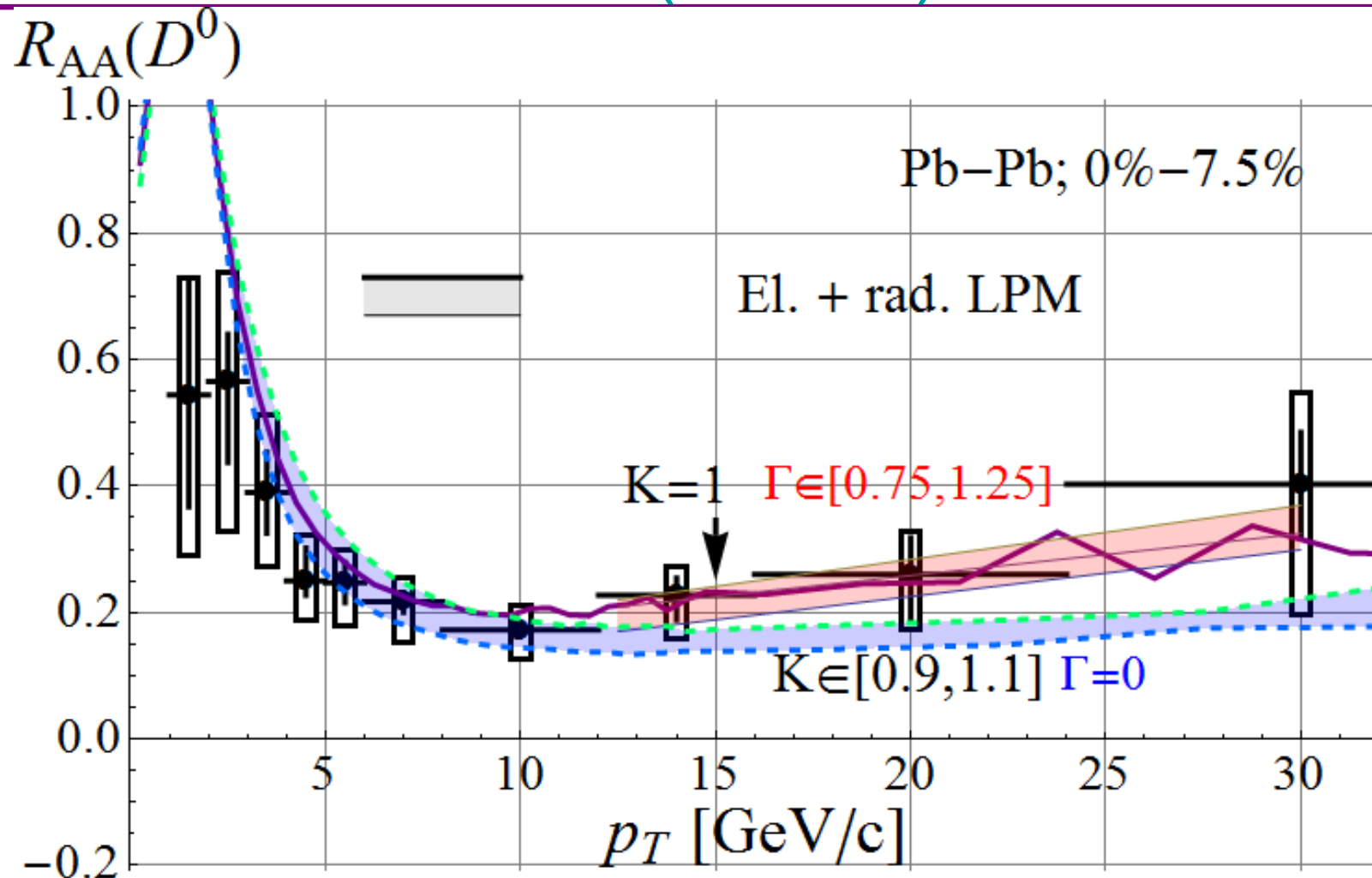
Basic question: Implications of a finite lifetime of the radiated gluon ?

## Concepts

- In QED or pQCD, damping is a NLO process (damping time  $t_d \gg \lambda$ ); neglected up to now.
- However: formation time of radiation  $t_f$  increases with boost factor  $\gamma$  of the charge
- Expected effects when  $t_f \approx t_d$  or  $t_f > t_d$  : in this regime,  $t_d$  should become the relevant scale (gluons absorbed being formed)



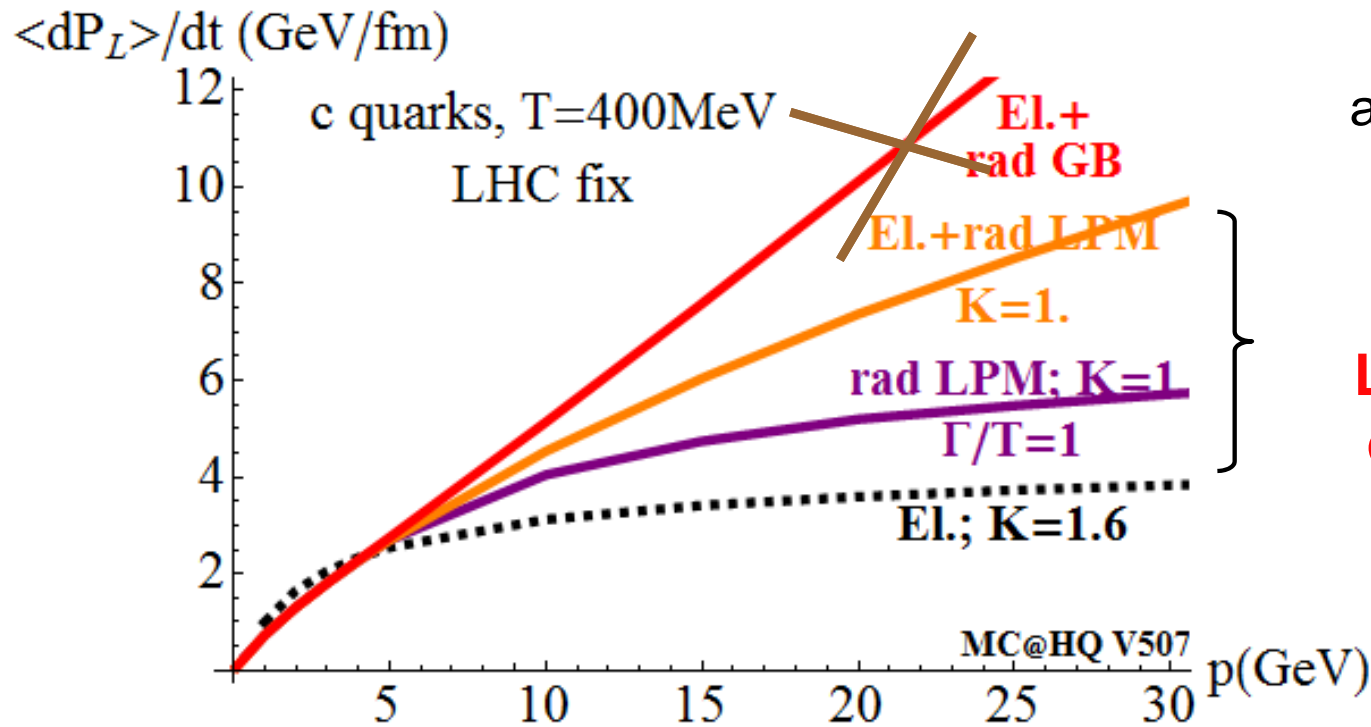
# Consequences of radiation damping for mesons at LHC (central);



Damping of radiated gluons reduces the quenching of D mesons

# QGP properties from HQ probe at LHC

Gathering all *rescaled* models (*coll. and radiative*) compatible with RHIC  $R_{AA}$ :



the drag coefficient reflects the average momentum loss (per unit time) => large weight on  $x \sim 1$

**LHC has the potentiality to constrain further the drag coefficient!!!**

We extract it from data

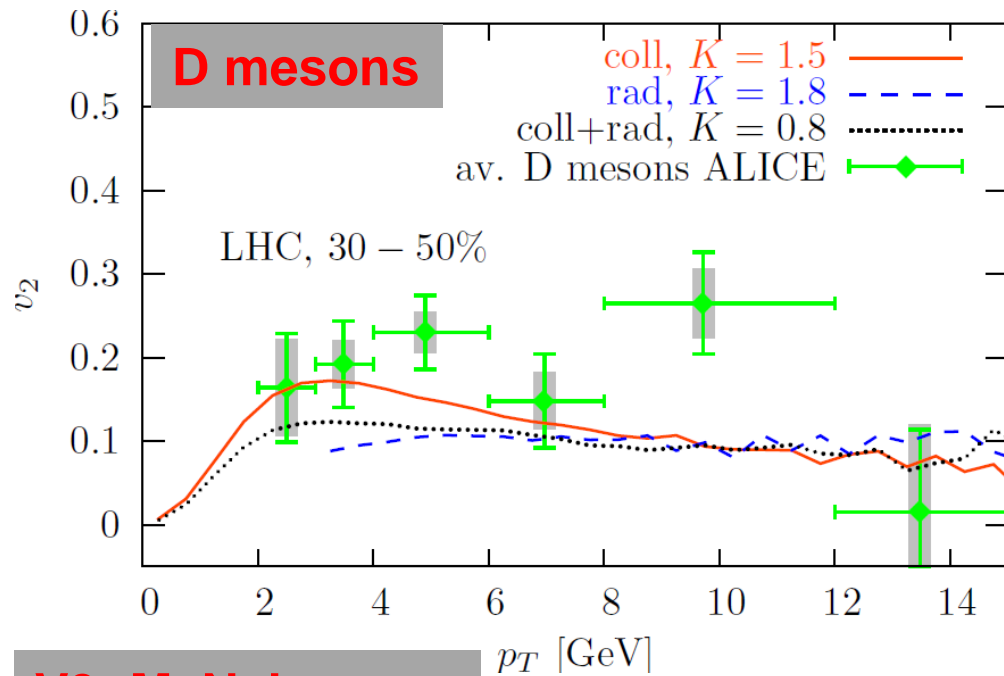


We are eager to compare with future lattice results

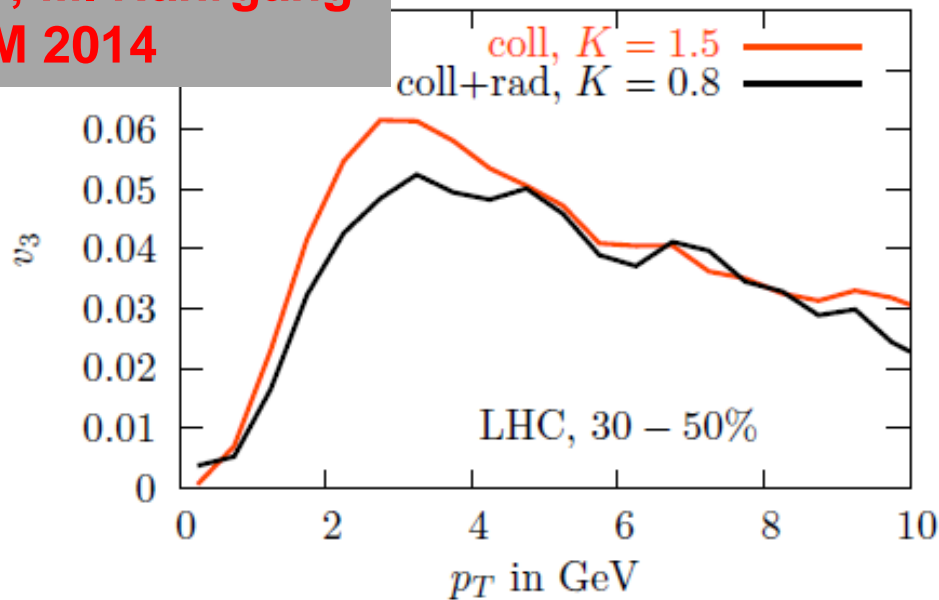
**Main message**

It is possible to reveal some fundamental property of QGP using HQ probes

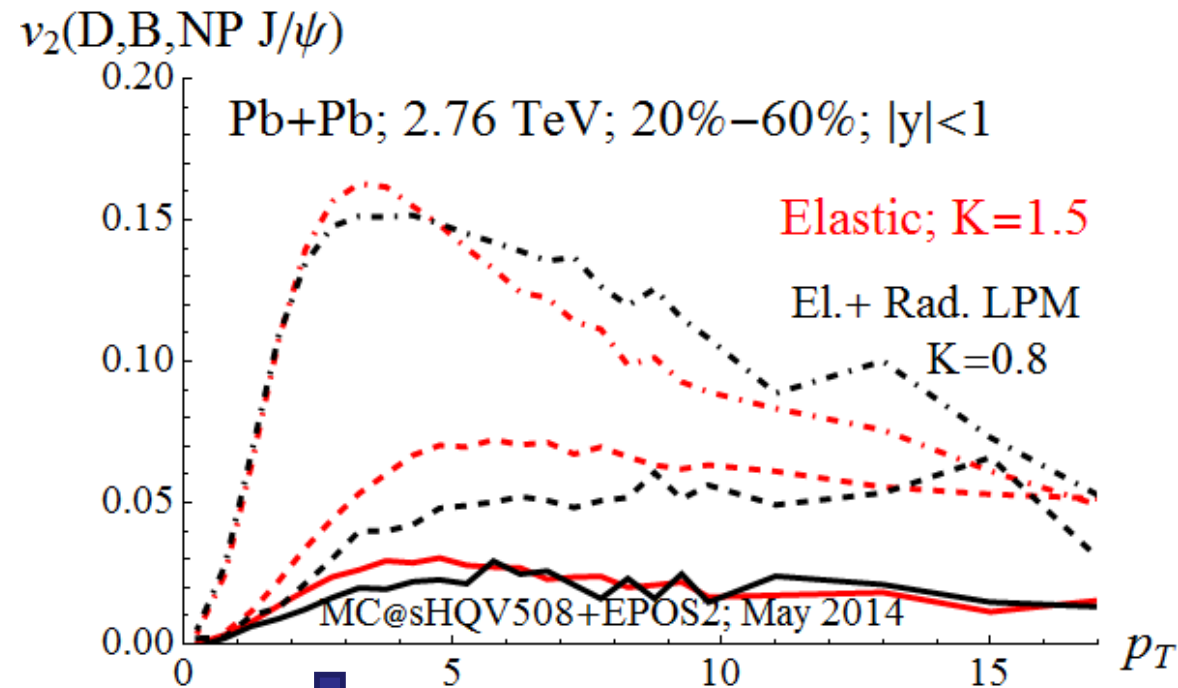
# Elliptic flow(s) @ LHC



**V3; M. Nahrgang  
 QM 2014**



**B mesons and NP J/psi**



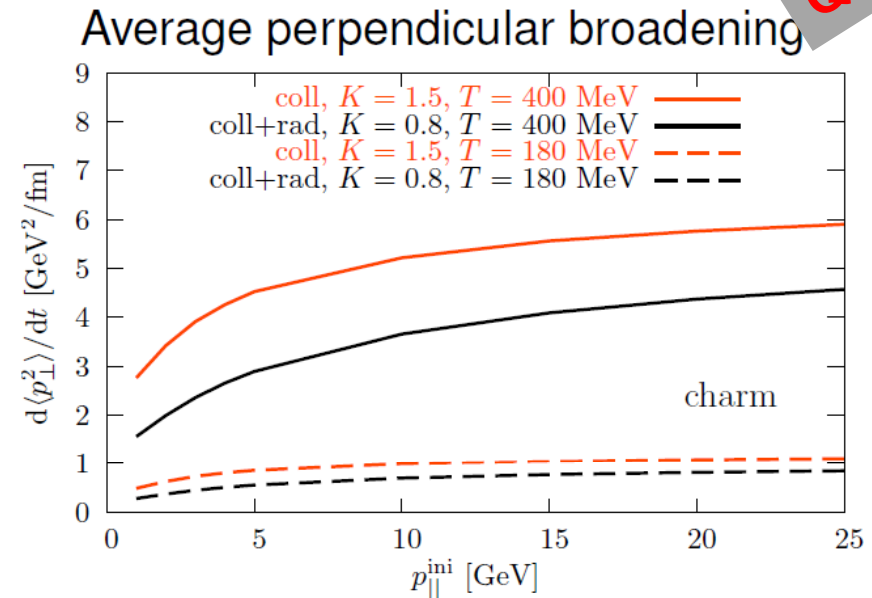
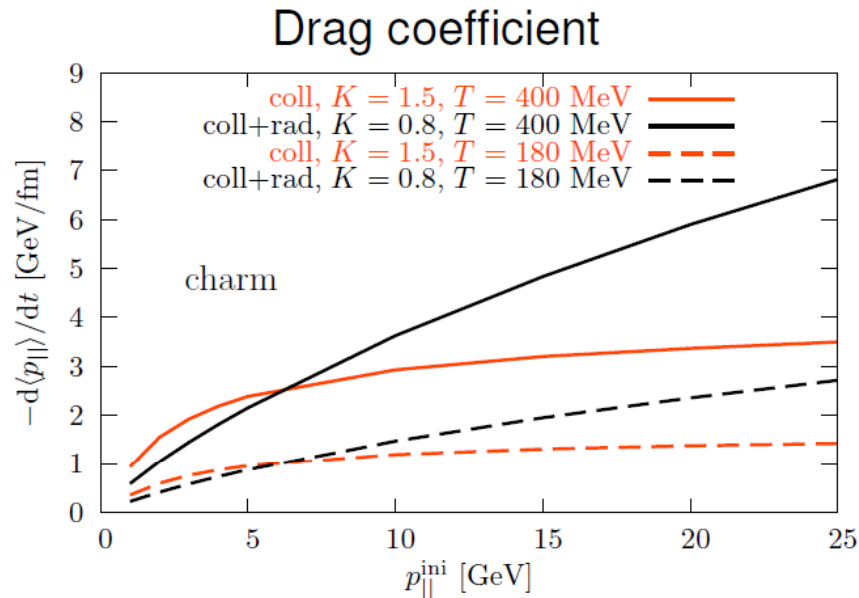
↓  
**To be compared with future  
 CMS results (in a few weeks  
 from now)**



# New probe: HQ correlations ([arxiv 1305.3823](https://arxiv.org/abs/1305.3823))

## Properties of the interaction

M. Nahrgang  
QM 2014



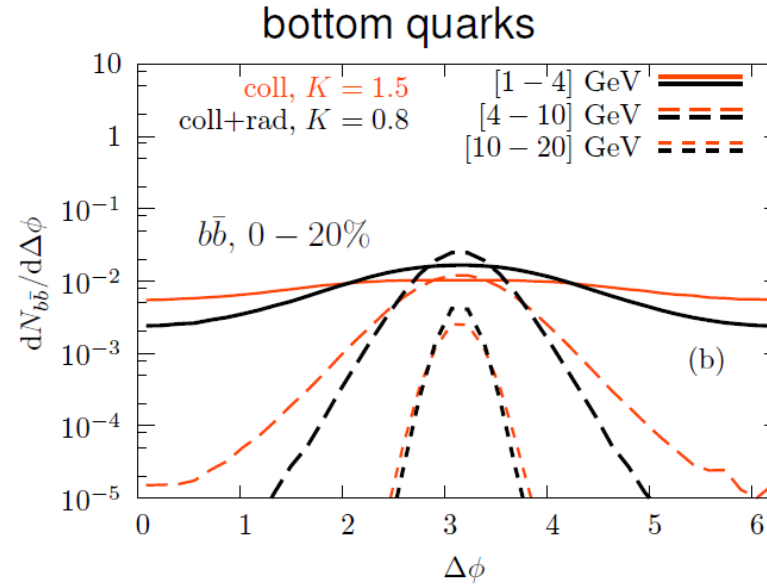
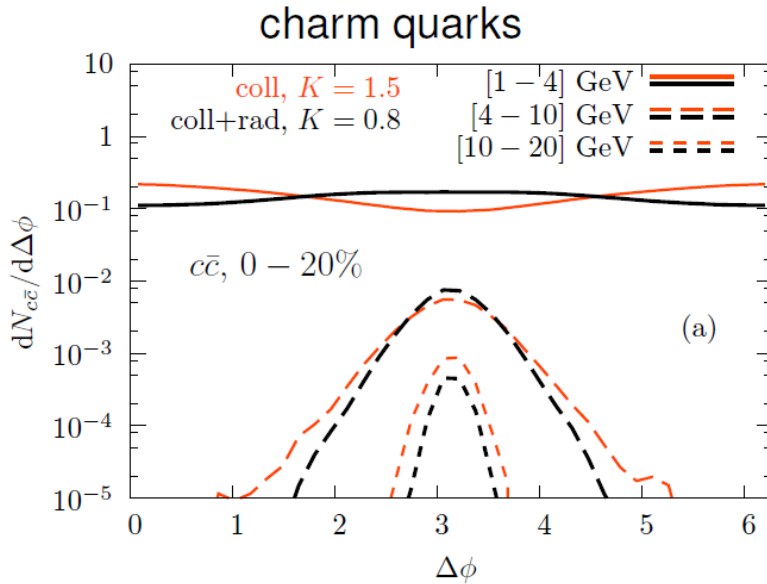
- Clearly different  $p_T$  dependence of the drag coefficient, stronger increase for **collisional+radiative(+LPM)** energy loss.
- At low  $p_T$  the drag coefficient is larger for **collisional** energy loss.
- Purely **collisional** scatterings lead to a larger average  $\langle p_{\perp}^2 \rangle$  than **collisional+radiative(+LPM)**.
- Expectation: initial correlations are broadened more effectively by a purely **collisional** interaction mechanism.

# New probe: HQ correlations

## Heavy-quark azimuthal correlations at LHC energies

M. Nahrgang  
QM 2014

(central collisions, back-to-back initialization, no background from uncorrelated pairs)



- Stronger broadening in a purely **collisional** than in a **collisional+radiative(+LPM)** interaction mechanism
- Variances in the intermediate  $p_T$ -range:  
**0.22** vs. **0.13** (charm) and **0.3** vs. **0.14** (bottom)
- Initial correlations survive the propagation in the medium at higher  $p_T$ .
- At low  $p_T$  initial correlations are almost washed out: small residual correlations remain for the **collisional+radiative(+LPM)** mechanism, “partonic wind” effect for a purely **collisional** scenario.

# New signature: HQ correlations

## Realistic initial $b\bar{b}$ distributions - MC@NLO

M. Nahrgang  
QM 2014

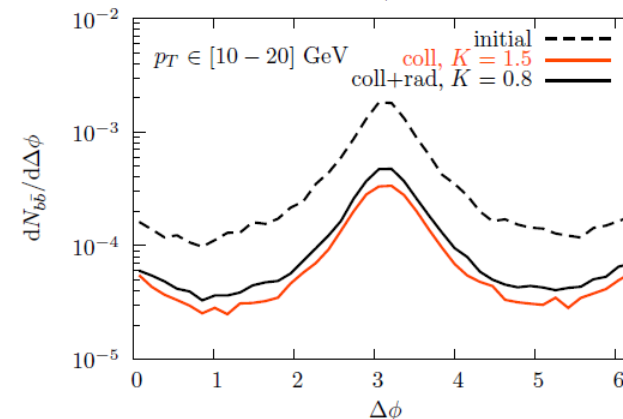
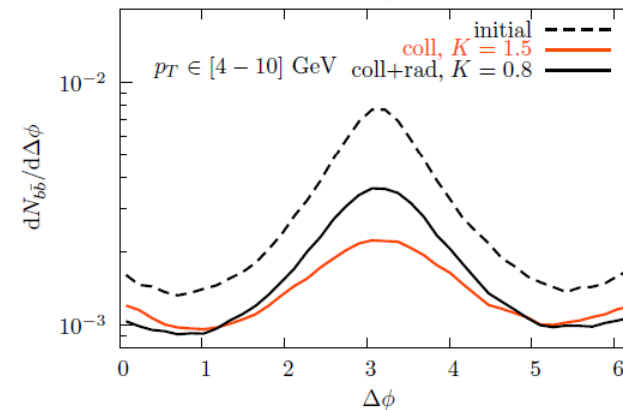
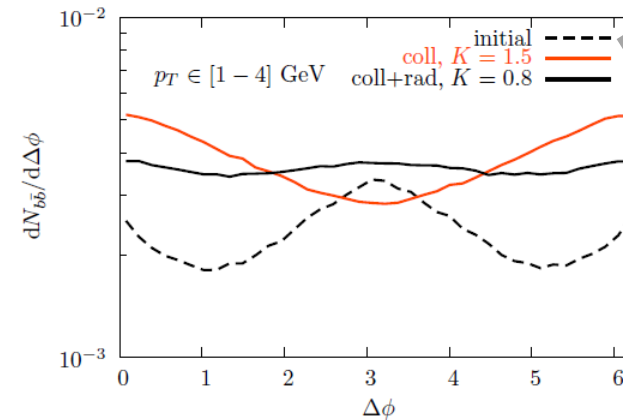
NLO QCD matrix elements coupled to parton shower evolution: MC@NLO+Herwig.

S. Frixione and B. R. Webber, JHEP **0206** (2002)

S. Frixione, P. Nason and B. R. Webber, JHEP **0308** (2003)

- Higher-order processes lead to an initial broadening around  $\Delta\phi \approx \pi$  and an enhancement of the correlations at  $\Delta\phi \approx 0$ .
- For intermediate  $p_T$ : increase of the variances from initial to final by  $\sim 20\%$  for the purely **collisional** mechanism and  $\sim 10\%$  for **collisional+radiative(+LPM)**.
- Correlations at large  $p_T$  seem to be dominated by the initial correlations.
- Large differences between NLO+parton shower approaches on charm quark production!
- Very important: need a reliable pp reference for  $\Delta\phi$  distributions!

LHC, central  $\rightarrow$



## Conclusions & further studies

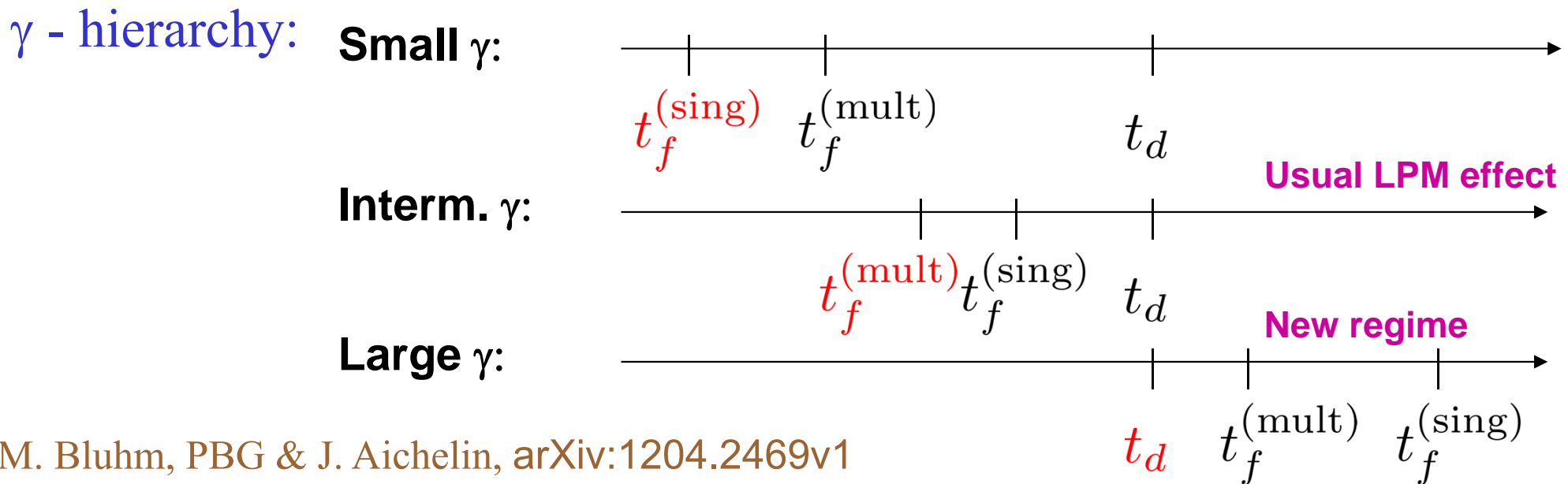
- Inspired pQCD model, in reasonable agreement with RHIC (and LHC) open heavy quark physics (**some resummation mandatory**).
- Hadronization plays an important role (not shown here)
- There seems to be a systematic underestimation of the elliptical flows ( $v_2$ )
- Need for a better understanding of the effective degrees of freedom in the QGP (cross over vs phase transition): recent common work with FIAS and Giessen (see H. Berrehrah's talk)... to be continued
- ... and many more things that could be achieved thanks to networking.

# Consequences of radiation damping on energy loss

Basic question: Implications of a finite lifetime of the radiated gluon ?

## Concepts

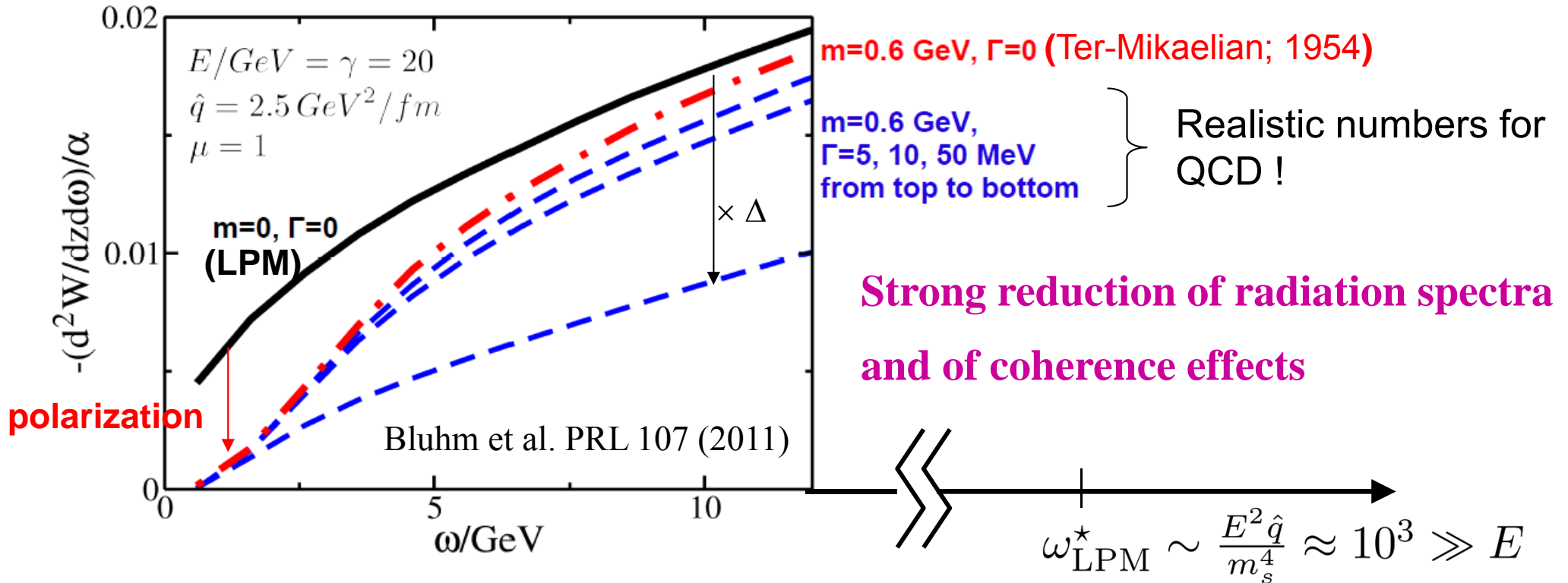
- In QED or pQCD, damping is a NLO process (damping time  $t_d \gg \lambda$ ); neglected up to now.
- However: formation time of radiation  $t_f$  increases with boost factor  $\gamma$  of the charge
- Expected effects when  $t_f \approx t_d$  or  $t_f > t_d$  : in this regime,  $t_d$  should become the relevant scale (gluons absorbed being formed)



# Consequences of radiation damping on energy loss

PRL 107 (2011): Revisiting LPM effect in ED using complex index of refraction, focussing on the radiation at time of formation

$$n^2(\omega) = 1 - m^2/\omega^2 + 2i\Gamma/\omega$$



Scaling law:

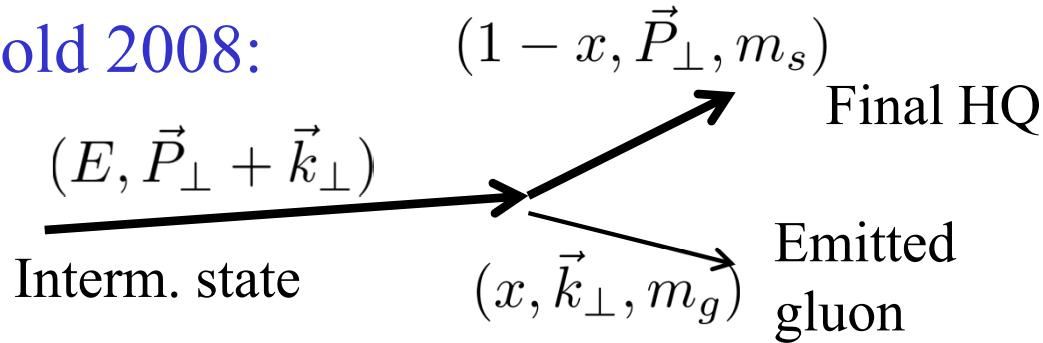
$$\frac{\frac{dN}{d\omega}}{\frac{dN_{sing}}{d\omega}} \approx \frac{\min(t_d, t_f^{(sing)}, t_f^{(mult)})}{t_f^{sing}}$$

**Allows for first phenomenological study in QCD case**

No "BH" limit

# Formation time of radiated gluon

Arnold 2008:



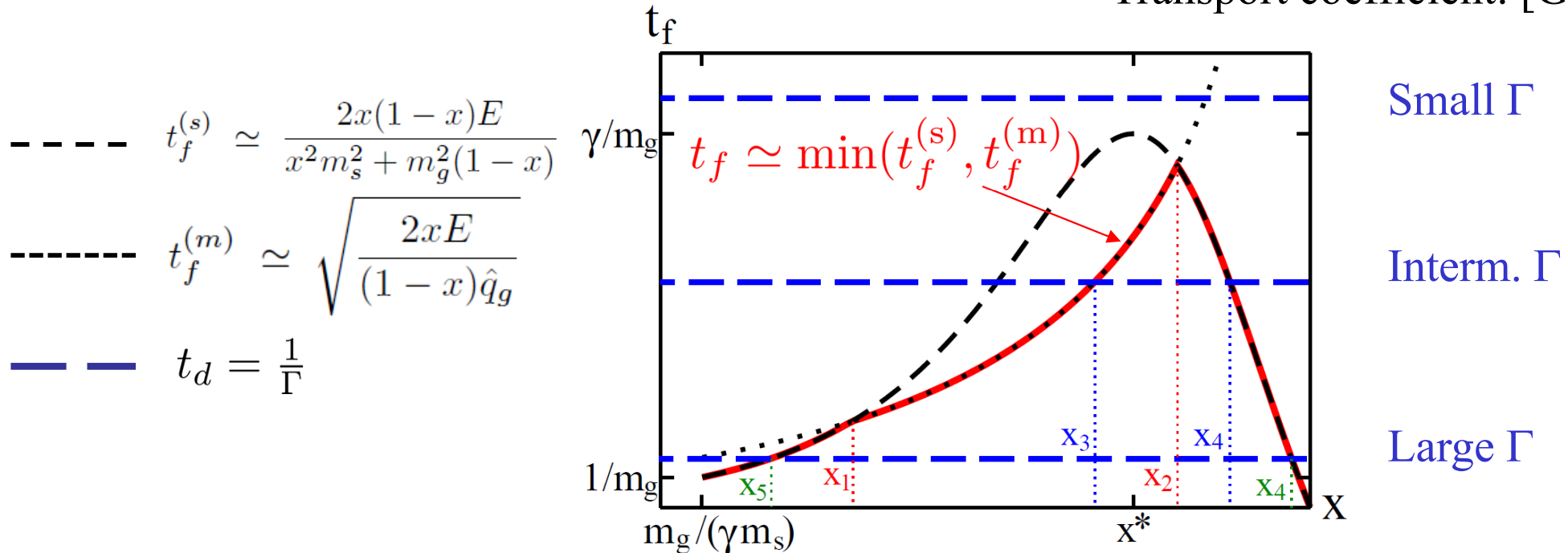
$$t_f \left[ \frac{\langle p_B^2 \rangle + x^2 m_s^2 + (1-x)m_g^2}{2x(1-x)E} \right] \simeq 1$$

$$p_B^2 := \left( (1-x)\vec{k}_\perp + x\vec{P}_\perp \right)^2 \Rightarrow \langle p_B^2 \rangle \approx (1-x)^2 \hat{q}_g t_f$$

In QCD: mostly gluon rescattering

**=> Self consistent expression for  $t_f$**

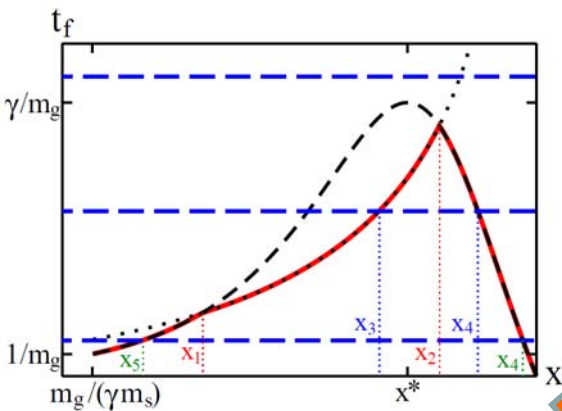
Transport coefficient: [GeV<sup>2</sup>/fm]





# New regimes when including gluon damping

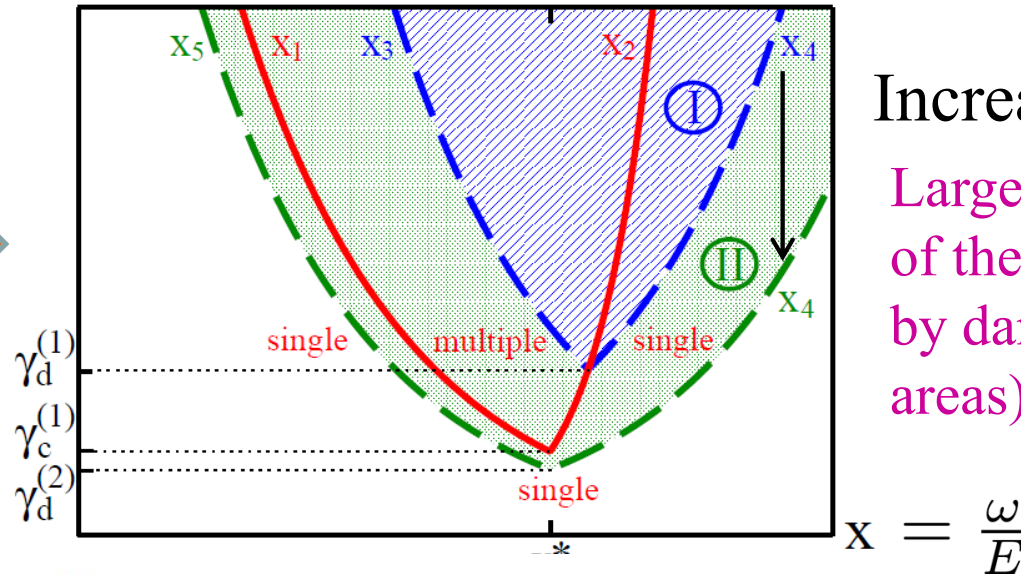
$x$ - $\gamma$  space for  $\hat{q} < m_g^3$



$\Gamma$ - $\gamma$  space

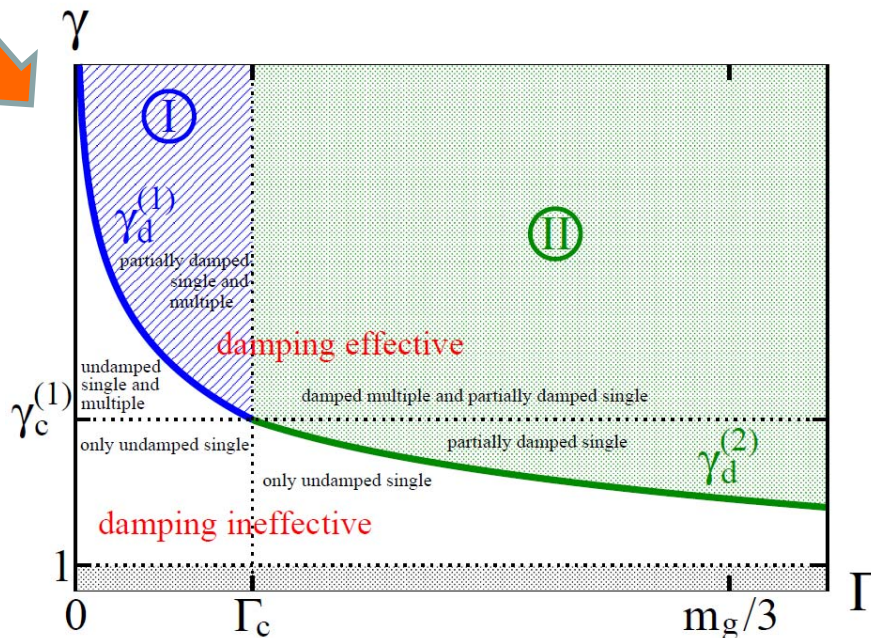
$\gamma$ -scales	
$\gamma_c^{(1)}$	$\sim m_g^3 / \hat{q}_g$
$\gamma_d^{(1)}$	$\sim \sqrt{\hat{q}_g / \Gamma^3}$
$\gamma_d^{(2)}$	$\sim m_g / \Gamma$

Larger damping effect at large  $\gamma$



Increasing  $\Gamma$

Larger and larger part of the spectrum affected by damping (shaded areas)



For  $\Gamma > \Gamma_c \approx \frac{\hat{q}_g}{m_g^2}$

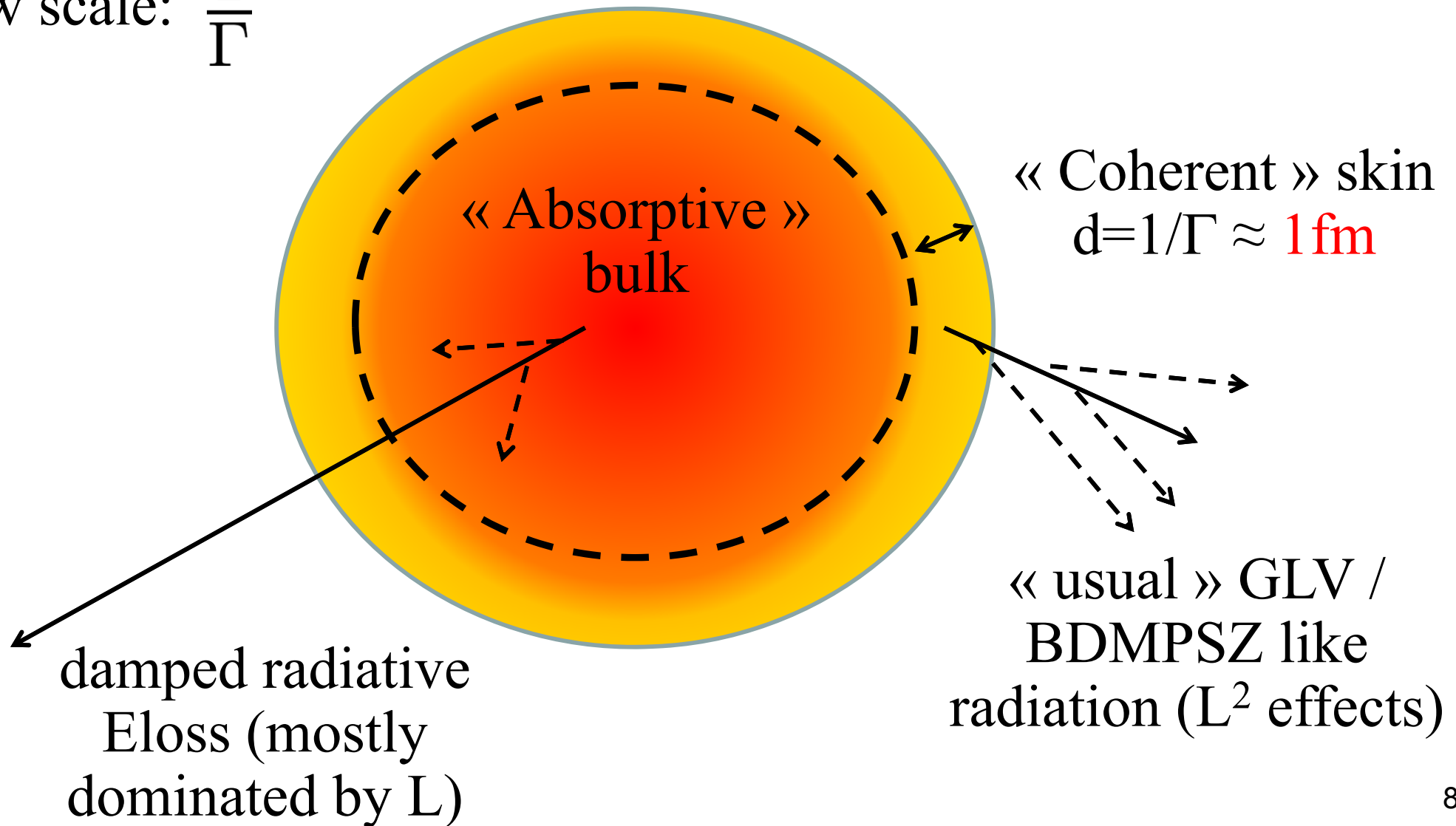
coherent radiation is totally superseded by damping



# Conclusion: Global picture for finite path length $L$ Eloss

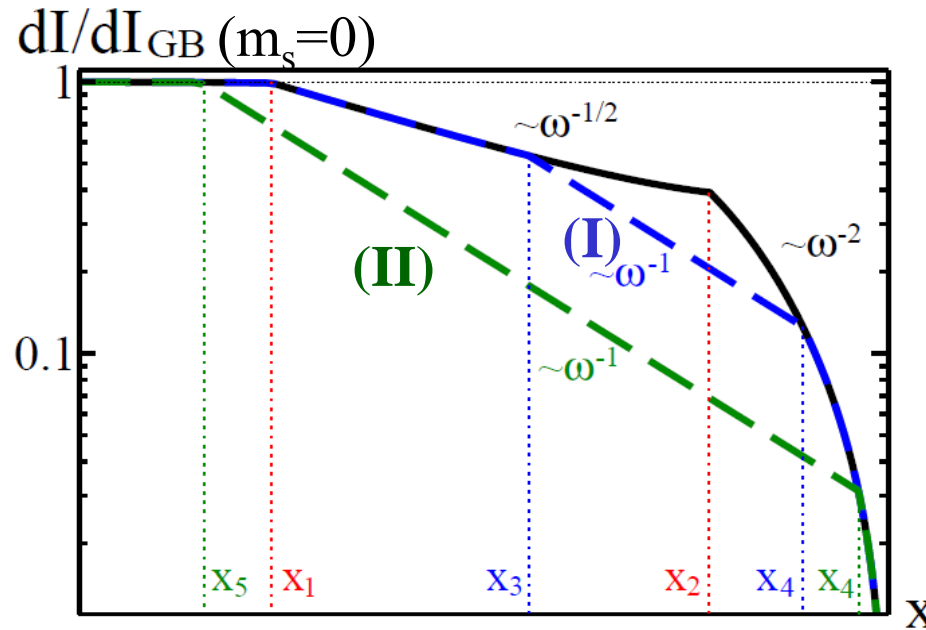
Usually: competition btwn  $L$  vs  $L_\infty = \sqrt{\frac{E}{\hat{q}}}$

New scale:  $\frac{1}{\Gamma}$



# Consequences on the power spectra

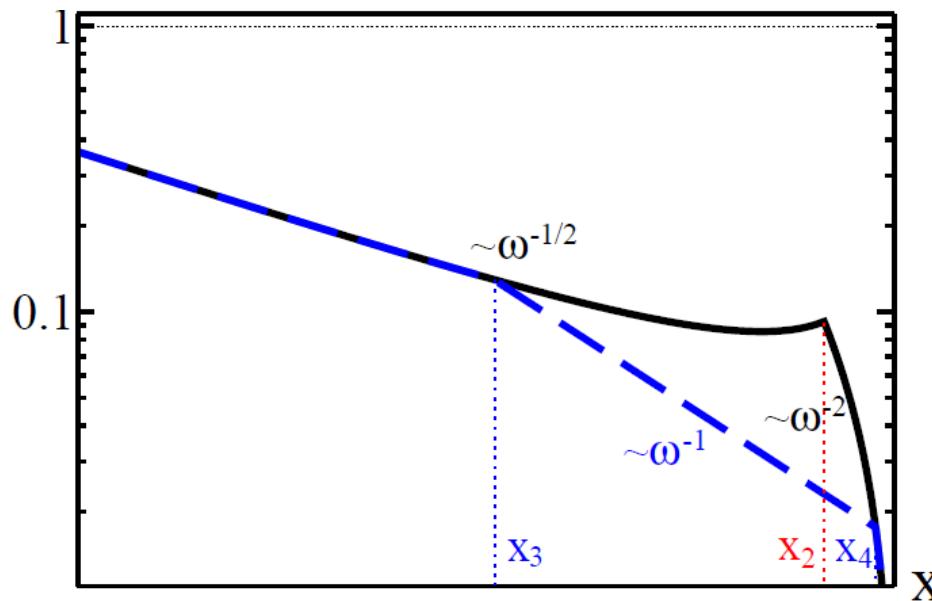
$$\hat{q} < m_g^3$$



(I) and (II): moderate and large damping (see previous slide)

$E = 45 \text{ GeV}$ ,  $m_s = 1.5 \text{ GeV}$   
 $m_g = 0.6 \text{ GeV}$ ,  $\hat{q} = 0.1 \text{ GeV}^2/\text{fm}$   
 $\Gamma = 0.05 \text{ GeV}$  (I) &  $0.15 \text{ GeV}$  (II)

$$\hat{q} > m_g^3$$



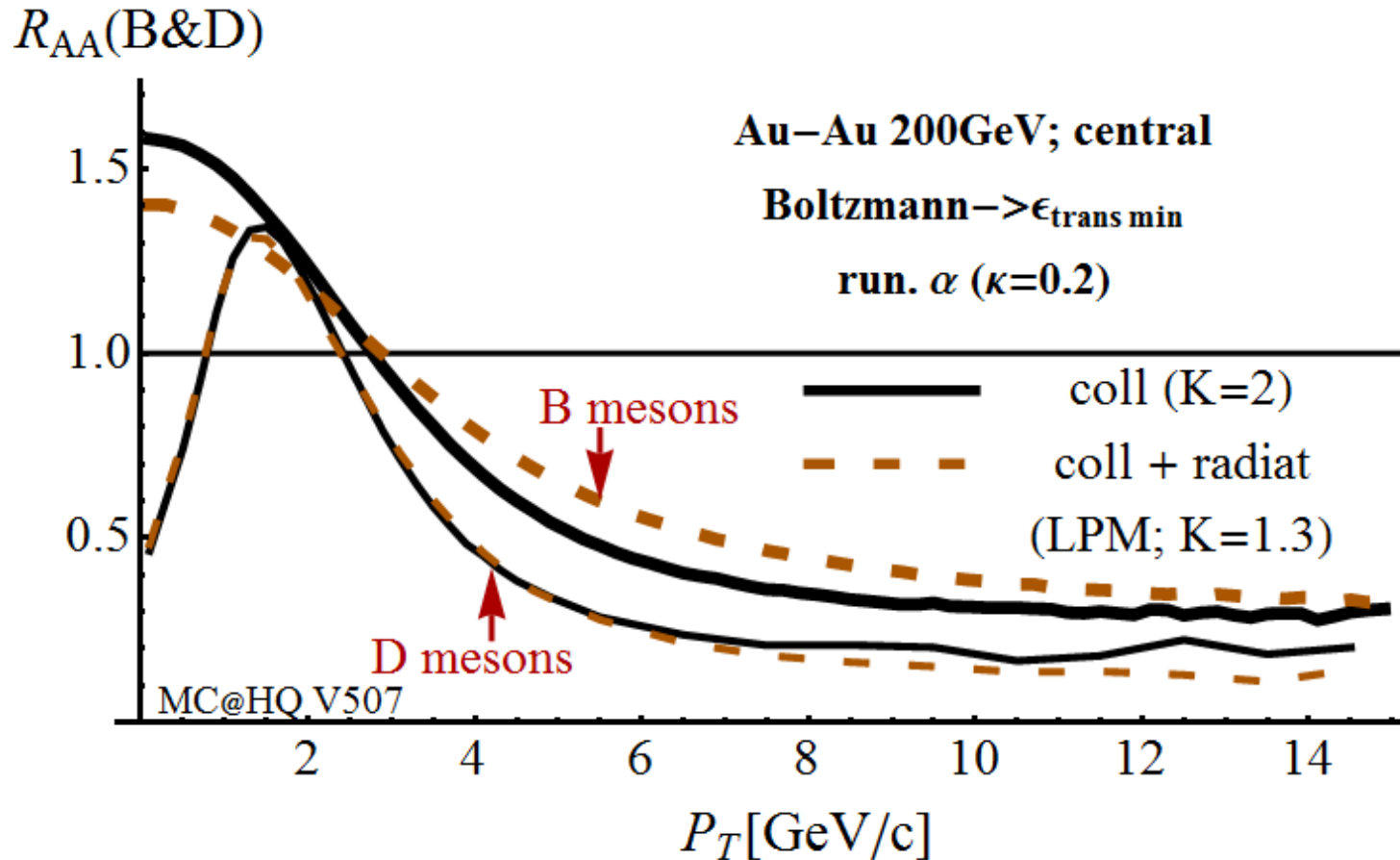
Same but

$$\hat{q} = 2 \text{ GeV}^2/\text{fm}$$

$$\Gamma = 0.25 \text{ GeV}$$

# Bright future of RHIC

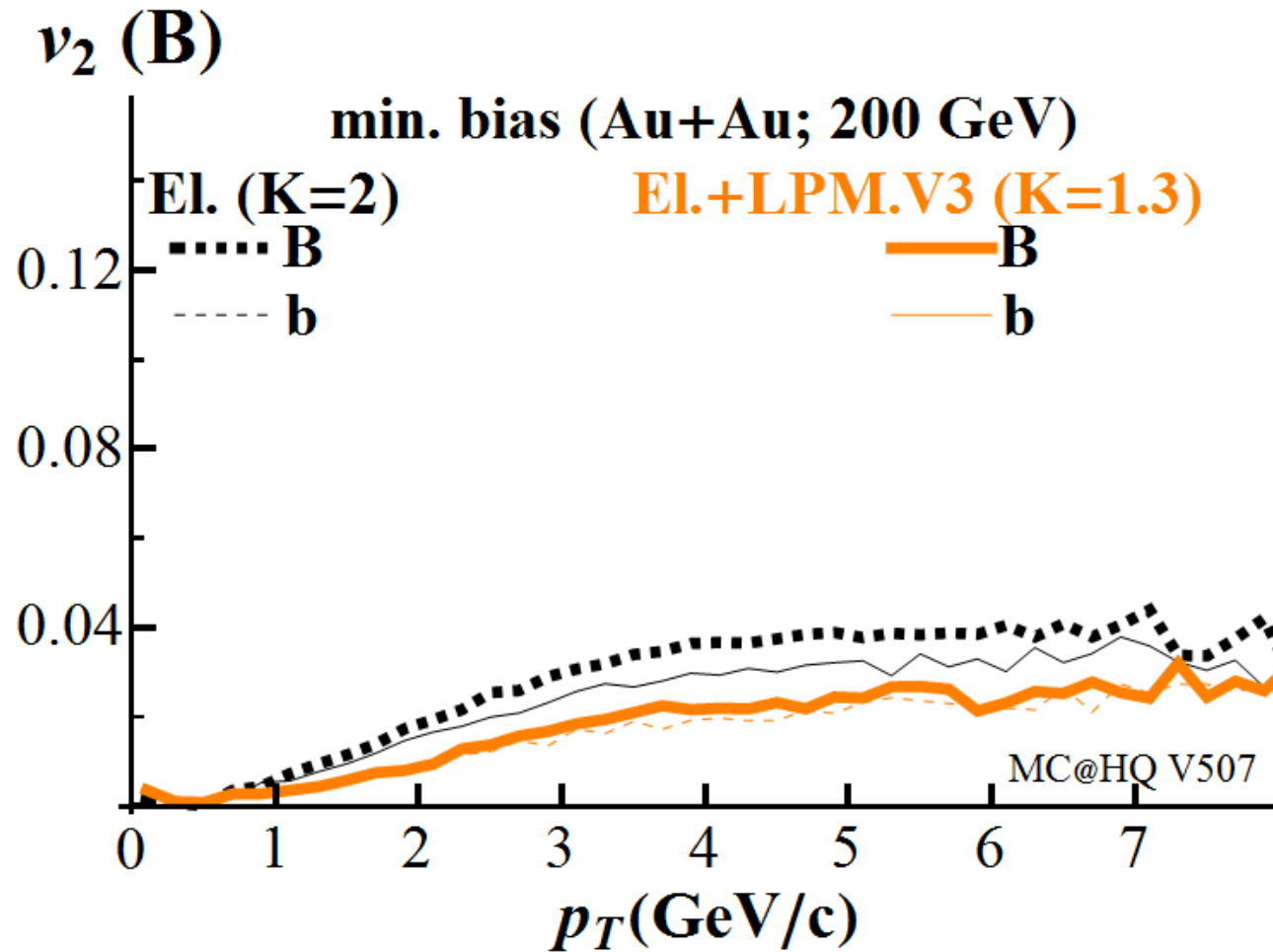
=> Discriminating power of B mesons



Larger mass hierarchy for radiative Eloss

# Bright future of RHIC

=> Discriminating power of B mesons



Larger mass hierarchy for radiative Eloss