

The Physics of Heavy Quarks in Heavy Ion collisions

How to detect a plasma of quarks and gluons?

Why are heavy quarks interesting ?

Interaction of heavy quarks with the quark gluon plasma

- our model (elastic and inelastic collisions, LPM)
- comparison with data
- how far we are with our understanding

The existence of a quark gluon plasma and the kind of transition towards the hadronic world

has been predicted by lattice gauge calculations
has been claimed to be seen in experiments (Science)

Why this is still a topic ?

- because every result is at most circumstantial evidence of its existence
 - a life time of 10^{-24} of seconds
 - a size of at most 15 fm
 - an expansion velocity of 0.85 c
 - and certainly not in a global thermal equilibrium
- because the multiplicity of almost all observed hadrons can be perfectly described by assuming a gas of $T = 158$ MeV
Hadronic rescattering spoils spectra

Only very special probes are sensitive to the plasma properties

they include:

- jets
- collective features (Elena, Marcus)
azimuthal distribution

$$\frac{dN}{d\Phi} = \frac{1}{2\pi} (1 + 2v_1 \cos \Phi + 2v_2 \cos 2\Phi \dots)$$

- Photons
- Dileptons
- J/psi or psi' or Y (1S)... Y(3S)
- heavy quarks -> heavy mesons

These particles do not come to an equilibrium with the plasma

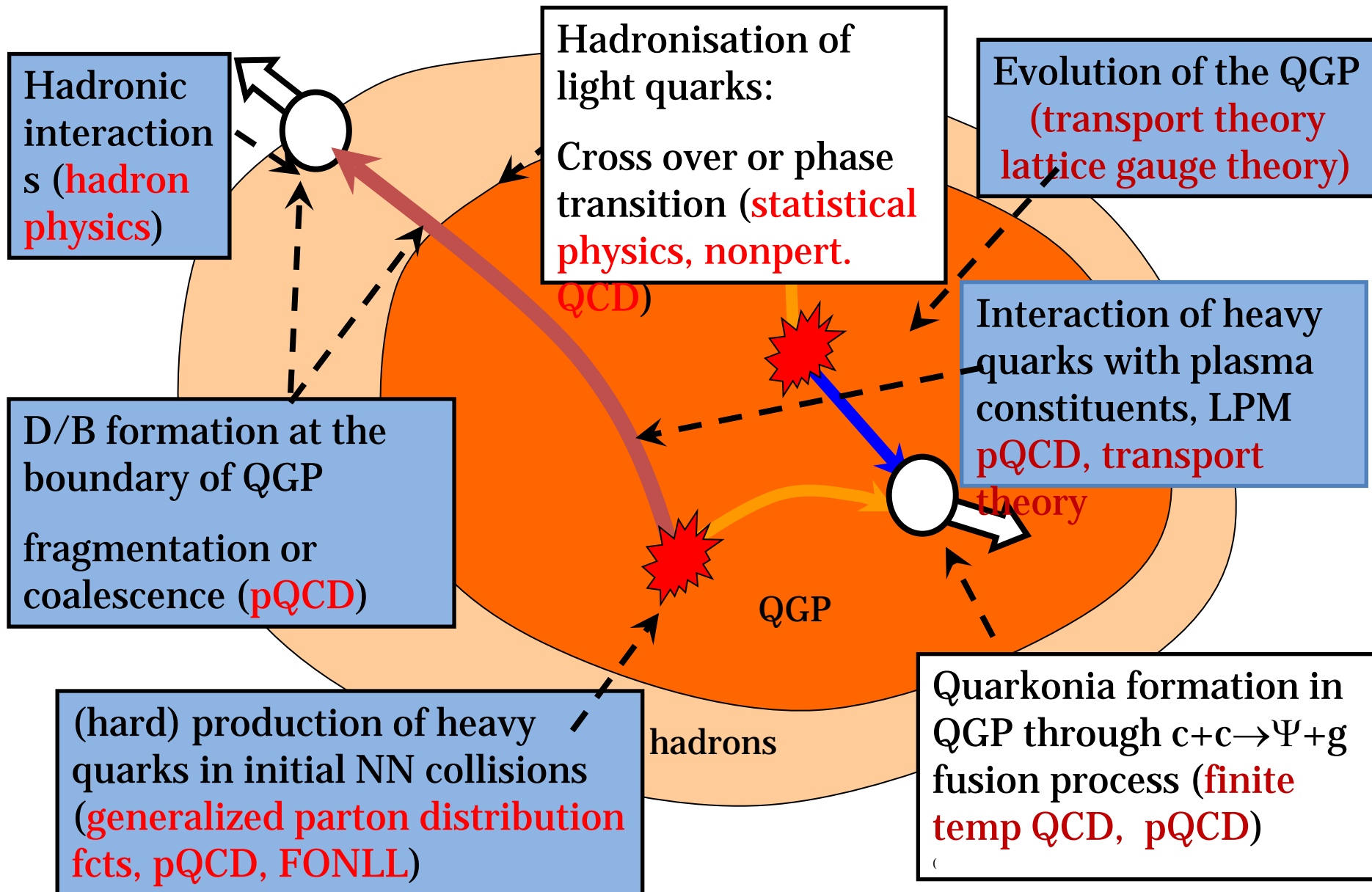
What makes heavy quarks (mesons) so interesting?

- produced in hard collisions (initial distribution: FONLL confirmed by STAR/Phenix)
- high p_T : no equilibrium with plasma particles (information about the early state of the plasma)
- not very sensitive to the hadronisation process

Ideal probe to study
properties of the QGP **during** its expansion

Caveat: two major ingredients: expansion of the plasma and elementary cross section ($c(b)+q(g) \rightarrow c(b)+q(g)$)
difficult to separate (arXiv:1102.1114)

Complexity of heavy quark physics in a nutshell :



Presently the analysis/discussion is centered around **two heavy quark observables**:

$$\text{I) } R_{AA} = \frac{d\sigma_{AA}/dp_t}{N_{bin}d\sigma_{pp}/dp_t}$$

=1 if heavy ion is superposition of pp collisions

Low p_t partial thermalization

High p_t energy loss due to elastic and radiative collisions

Energy loss tests the initial phase of the expansion

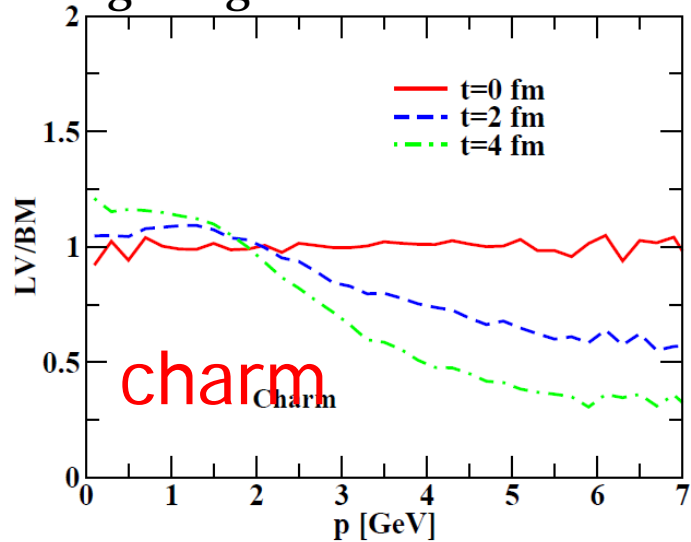
$$\text{II) Elliptic flow } v_2 \quad \frac{dN}{d\Phi} = \frac{1}{2\pi} (1 + 2v_1 \cos \Phi + 2v_2 \cos 2\Phi \dots)$$

tests the late stage of the expansion

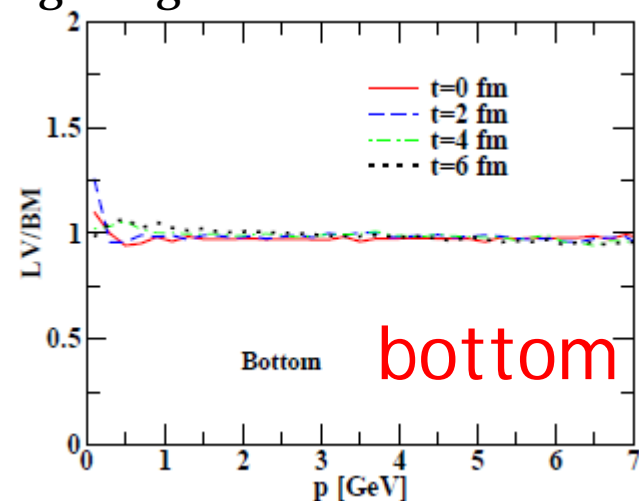
Two caveats one has to realize:

Fokker Planck (Langevin) is not the right tool

Ratio of **charm** quark spectra using Langevin and Boltzmann eq.

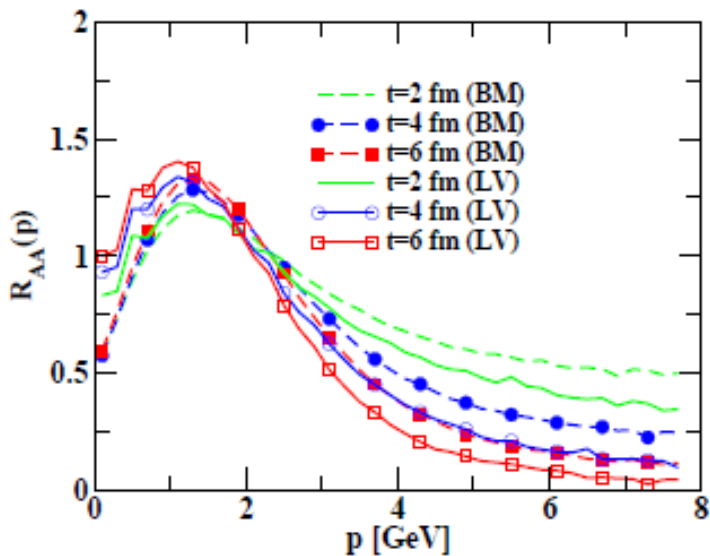


Ratio of **bottom** quark spectra using Langevin and Boltzmann eq.

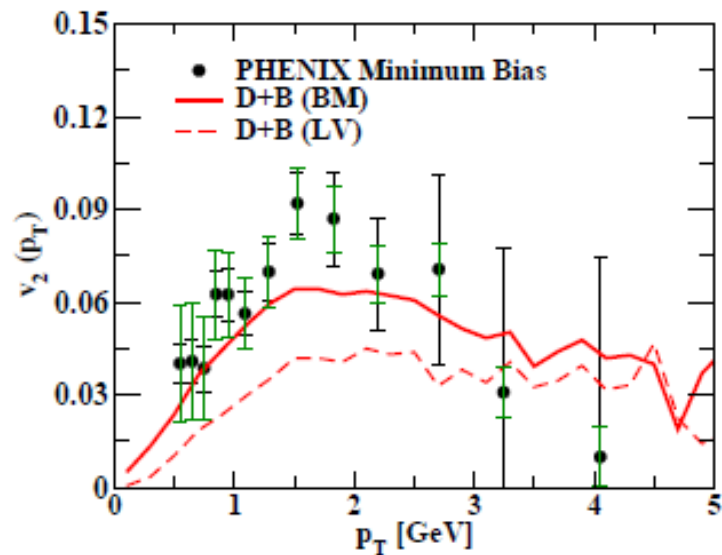


Das et al.
arxiv:

1312.6857

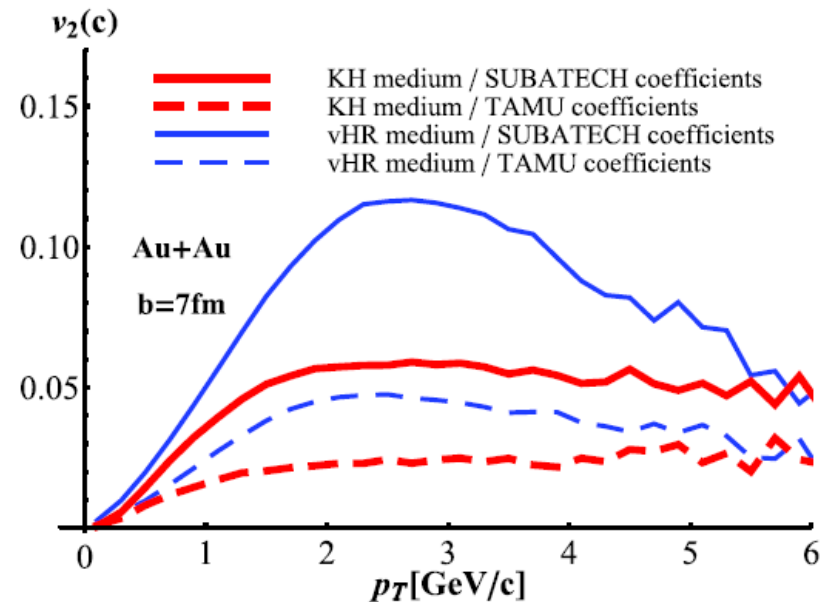
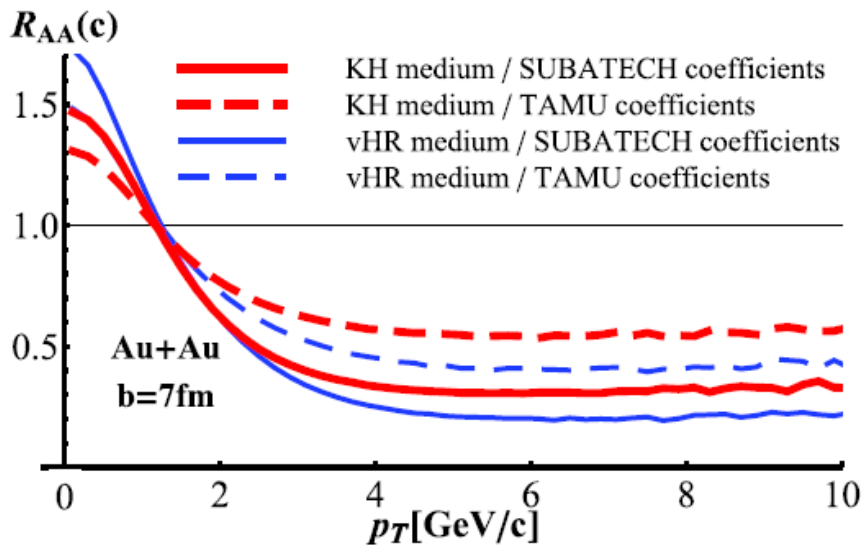


charm



Experimental data are sensitive to
Elementary interactions between heavy quarks and plasma
and
Expansion of the plasma

Arxiv 1102.1114



Difficult to disentangle
Simultaneous comparison of light and heavy mesons
observables is necessary

Our approach :

- We assume that pQCD provides the tools to study the processes

We want to

- model the reaction with a **minimum of approximations:**
exact Boltzmann collisions kernel, no Fokker Planck approx
- take into account **all the known physics with**
- **no approximations of scattering processes (coll+ radiative)**
- make connection to the **light quark sector** (v_2 jets particle spectra)
by embedding the heavy quarks into EPOS (LHC)
(or before Kolb & Heinz (RHIC))
- This serves then as a benchmark
- **deviation from data points towards new physics**

Nantes approach: Elastic heavy quark – q(g) collisions

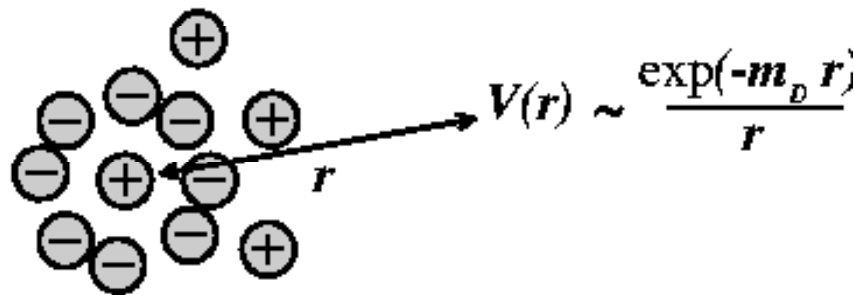
Key ingredients: pQCD cross section like $qQ \rightarrow qQ$

pQCD cross section in a medium has 2 problems:

a) Running coupling constant

$$\frac{d\sigma_F}{dt} = \frac{g^4}{\pi(s - M^2)^2} \left[\frac{(s - M^2)^2}{(t - \kappa m_D^2)^2} + \frac{s}{t - \kappa m_D^2} + \frac{1}{2} \right]$$

b) Infrared regulator



m_D regulates the long range behaviour of the interaction

Neither $g^2 = 4\pi \alpha(t)$ nor κm_D^2 are well determined

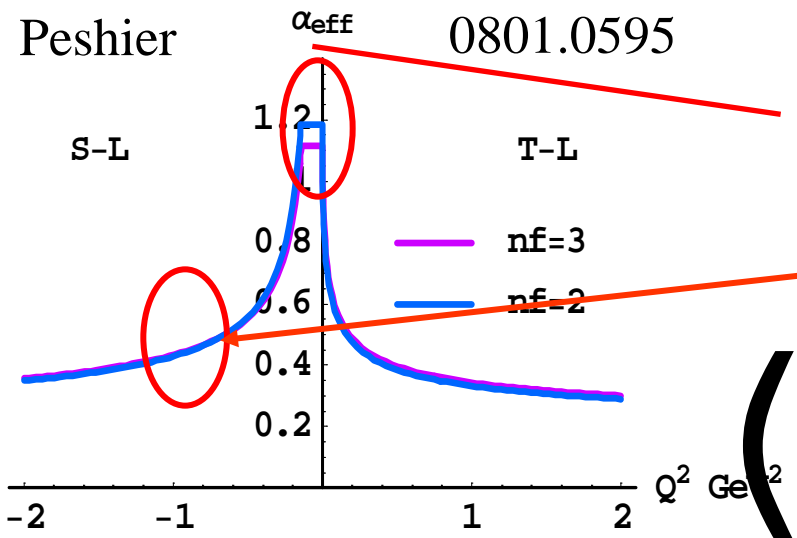
standard: $\alpha(t)$ is taken as constant or as $\alpha(2\pi T)$

$\kappa = 1$ and $\alpha = .3$: large K-factors (≈ 10) are necessary to describe data

A) Running coupling constant

“Universality constraint” (Dokshitzer 02) helps reducing uncertainties:

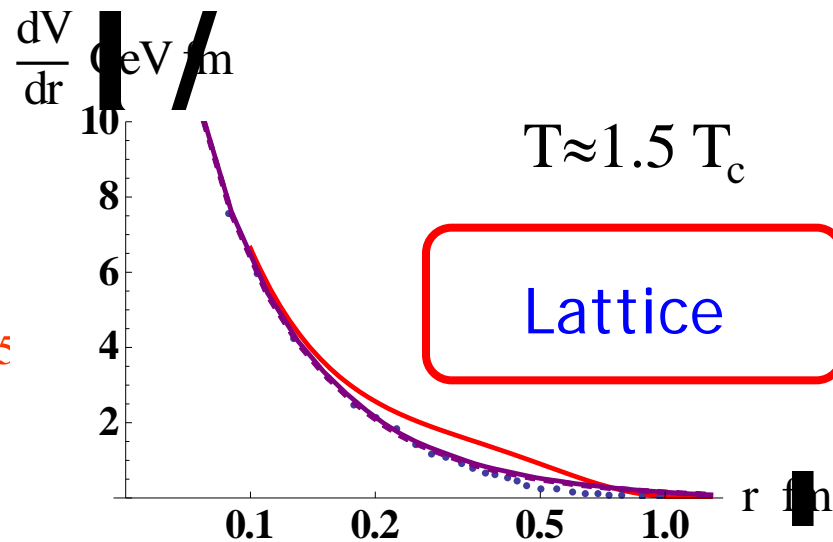
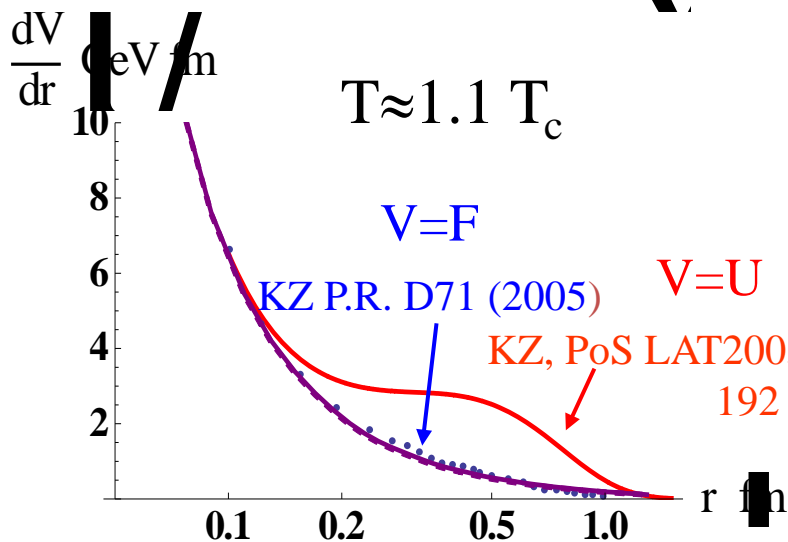
$$\frac{1}{Q_u} \int_{|Q^2| \leq Q_u^2} dQ \alpha_s(Q^2) \approx 0.5$$



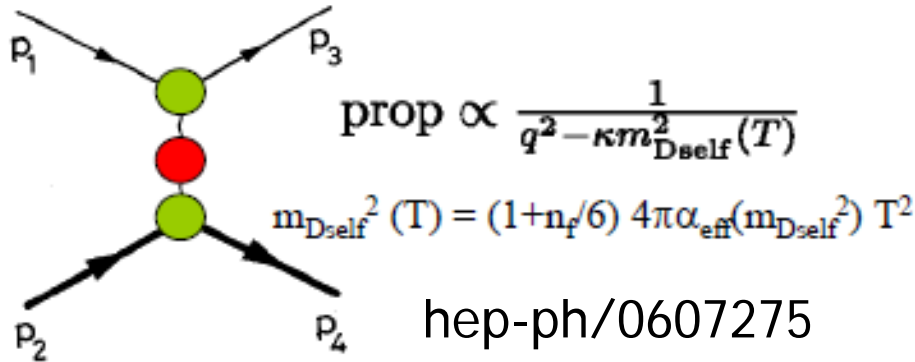
IR safe. The detailed form very close to $Q^2 = 0$ is not important does not contribute to the energy loss

Large values for intermediate momentum-transfer

$$\alpha_{qq}(r) \equiv \frac{3}{4} r^2 \frac{dV(r)}{dr}$$



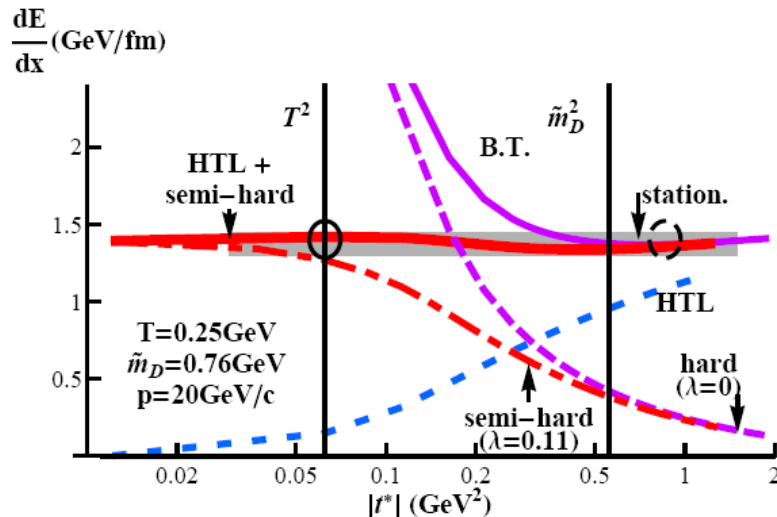
B) Debye mass



If t is small ($\ll T$) : **Born has to be replaced by a hard thermal loop (HTL) approach**

For $t > T$ Born approximation is (almost) ok

(Braaten and Thoma PRD44 (91) 1298,2625) for QED:
Energy loss indep. of the artificial scale t^* which separates the regimes



We do the same for QCD (a bit more complicated)
 Phys.Rev.C78:014904

Result:

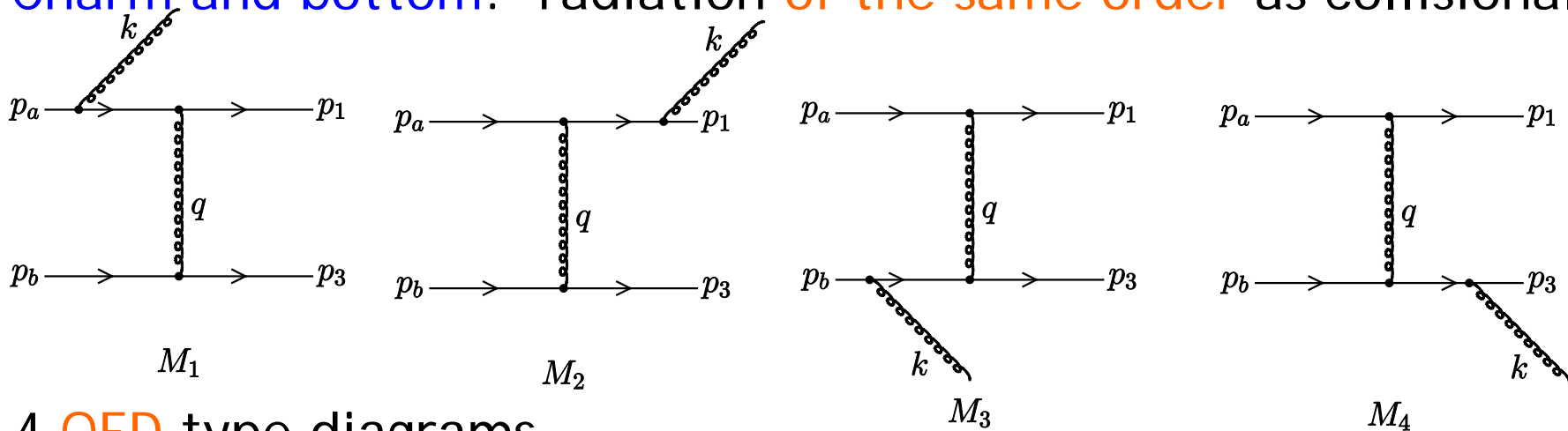
$\kappa \approx 0.2$

much lower than the standard value

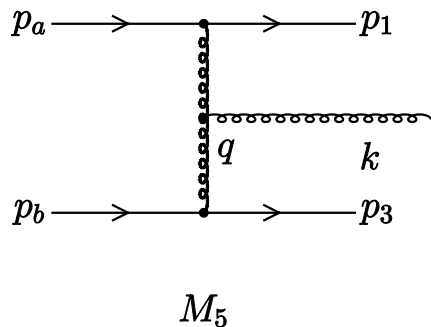
C) Inelastic Collisions

Low mass quarks : radiation dominates energy loss

Charm and bottom: radiation of the same order as collisional



4 QED type diagrams



1 QCD diagram

Commutator of the color SU(3) operators

$$T^b T^a = T^a T^b - i f_{abc} T^c$$

M1-M5 : 3 gauge invariant subgroups

$$M_{QED}^1 = T^a T^b (M_1 + M_2) \quad M_{QED}^2 = T^a T^b (M_3 + M_4)$$

$$M_{QCD} = i f_{abc} T^c (M_1 + M_3 + M_5)$$

M_{QCD} dominates the radiation

M^{SQCD} in light cone gauge

In the limit $\sqrt{s} \rightarrow \infty$ the radiation matrix elements **factorize** in

$$M_{tot}^2 = M_{elast}^2 \cdot P_{rad}$$

k_t, ω = transv mom/ energy of gluon E = energy of the heavy quark

$$P_{rad} = C_A \left(\frac{\vec{k}_t}{k_t^2 + (\omega/E)^2 m^2} - \frac{\vec{k}_t - \vec{q}_t}{(\vec{q}_t - \vec{k}_t)^2 + (\omega/E)^2 m^2} \right)^2$$

Emission from heavy q

Emission from g

leading order: no emission from light q

heals collinear divergences

$m=0$ -> Gunion Bertsch
Energy loss:

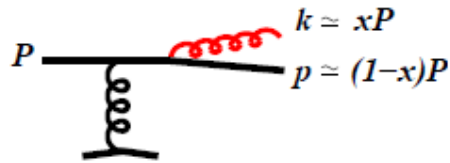
$$\frac{\omega d^4 \sigma^{rad}}{dx d^2 k_t dq_t^2} = \frac{N_c \alpha_s}{\pi^2} (1-x) \cdot \frac{d\sigma^{el}}{dq_t^2} \cdot P_{rad}$$

$$x = \omega/E$$

$$M_{QCD} = M_{SQCD} \left(1 - \frac{(\omega/E)^2}{(1-\omega/E)^2} \right)$$

Landau Pomeranshuk Migdal Effekt (LPM)

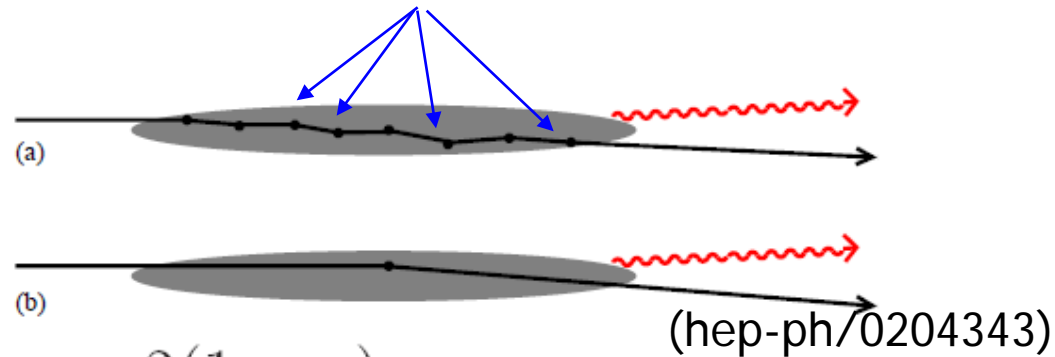
reduces energy loss by gluon radiation



Heavy quark radiates gluons
gluon needs time to be formed

Collisions during the formation time
do not lead to emission of a second gluon

emission of **one** gluon
(not N as Bethe Heitler)



$$t_f \approx \frac{2(1-x)\omega}{(\vec{k}_\perp - \vec{q}_\perp)^2 + x^2 M^2 + (1-x)m_g^2}$$

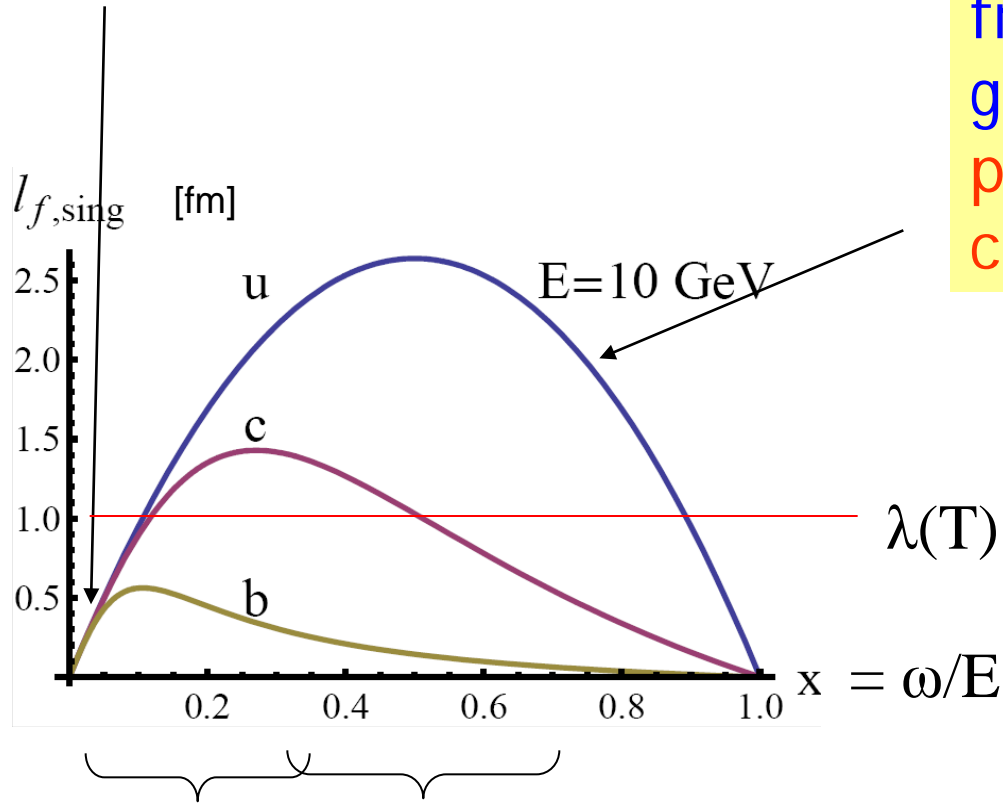
Multiple scatt .QCD:

$\approx N_{\text{coll}} \langle k_t^2 \rangle = t_f \hat{q}$ (red box) single scatt. (green box)

dominates $x < 1$ dominates $x \approx 1$ dominates $x \ll 1$

For $x < x_{cr} = m_g/M$, basically no mass effect in gluon radiation

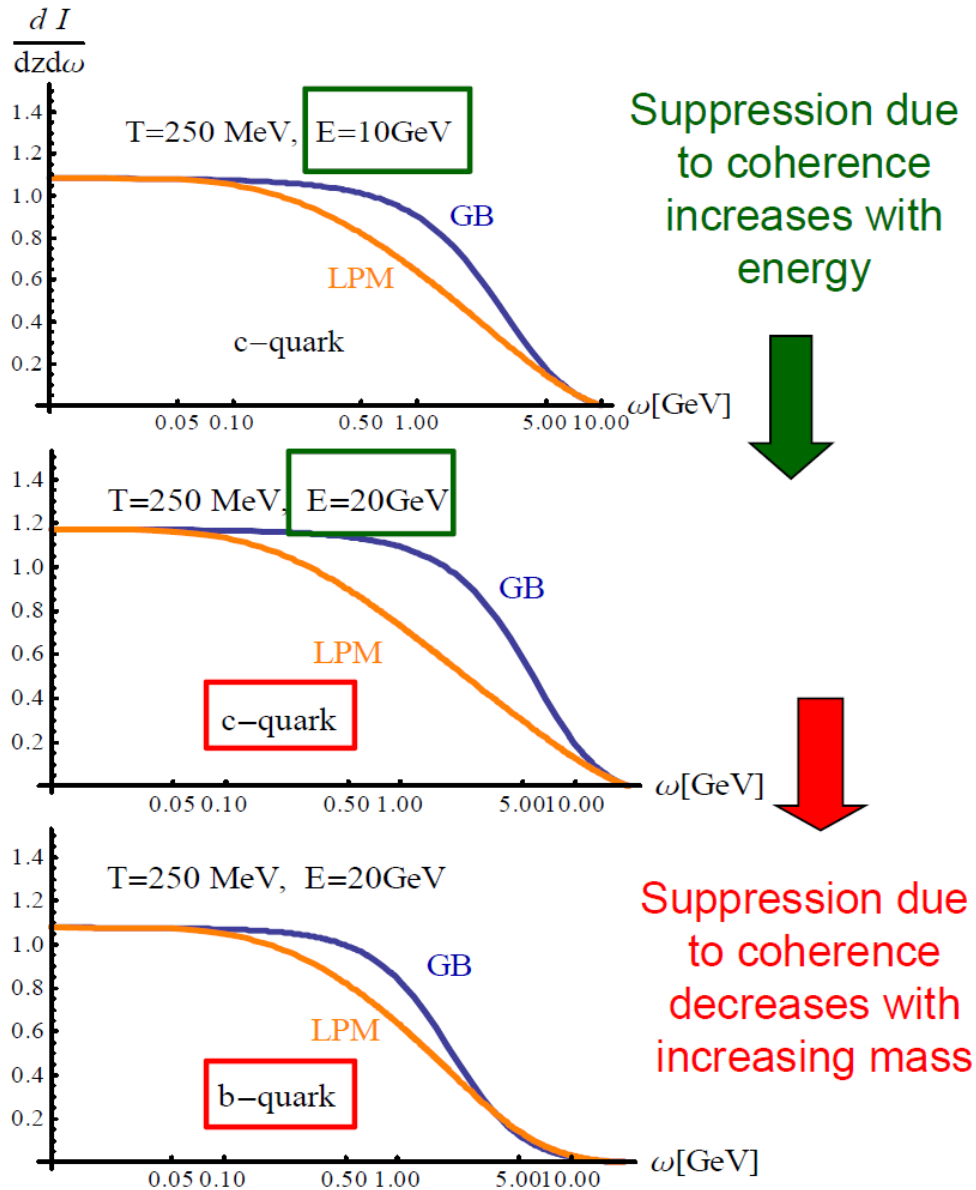
For $x > x_{cr} = m_g/M$, gluons radiated from heavy quarks are resolved in less time than those from light quarks and gluons => radiation process less affected by coherence effects.



LPM important for intermediate x where formation time is long

Most of the collisions $\frac{d\sigma}{dx}$ Dominant region for average E loss $x \frac{d\sigma}{dx}$

Consequences of LPM on the energy loss



Calculations for RHIC and LHC

Initialization: FONLL distribution of c and b

QGP : Hydro Kolb-Heinz for RHIC
EPOS for LHC

Interaction QGP-heavy quarks:

elastic collisions (collisional energy loss) ($K \approx 2$)

elastic collisions + and gluon emission (radiative energy loss)
+LPM

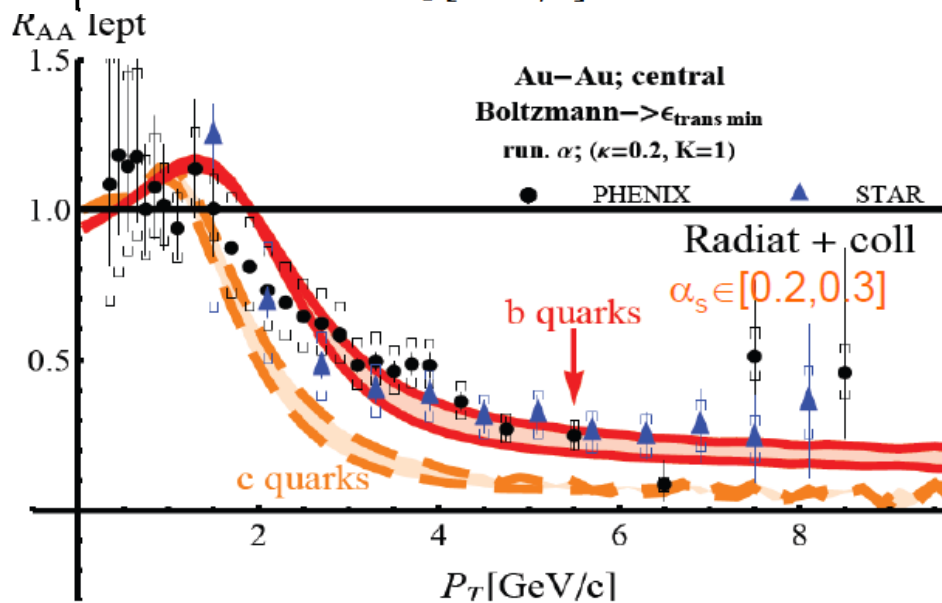
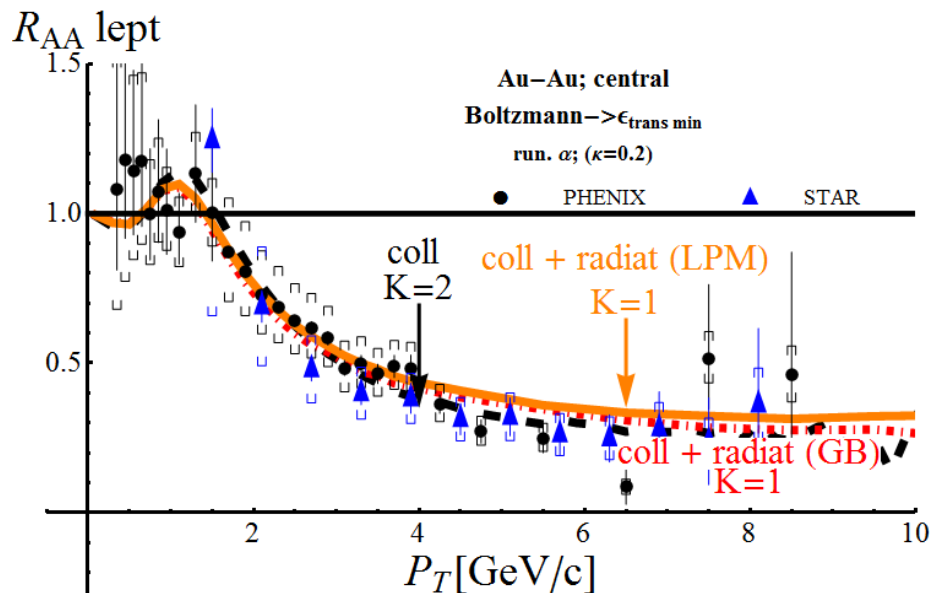
Hadronisation:

Coalescence for low pt heavy quarks

Fragmentation for high pt heavy quarks

Hadronic rescattering is small

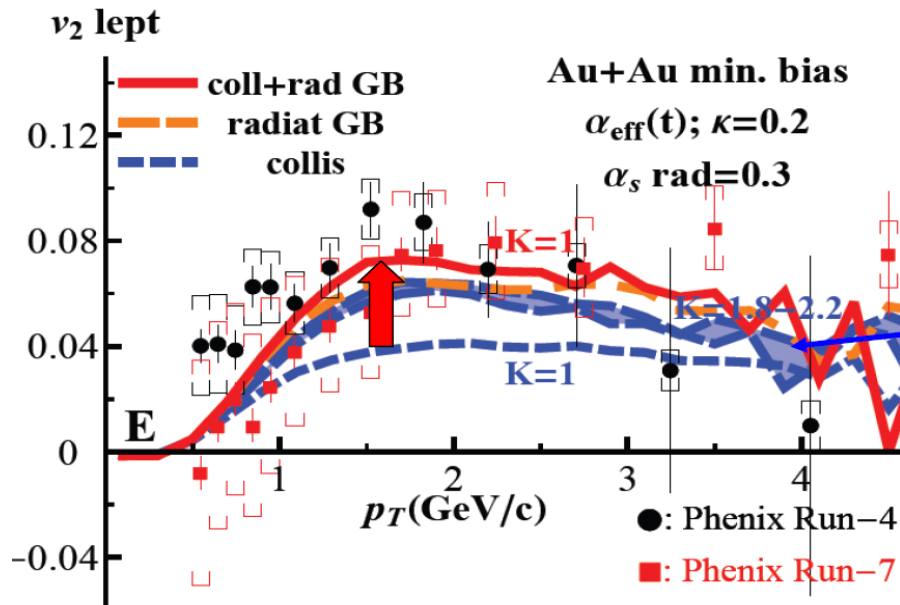
RHIC Hydro: Kolb Heinz



1. Coll: too little quenching (but very sensitive to freeze out) $\rightarrow K=2$
2. Radiative Eloss indeed as important as the collisional one
3. Flat experimental shape is well reproduced
4. $R_{AA}(p_T)$ has the same form for radial and collisional energy loss (at RHIC)

separated contributions e from D and e from B.

RHIC



1. Collisional + radiative energy loss + dynamical medium : *compatible* with data
2. To our knowledge, one of the first model using radiative Eloss that reproduces v_2

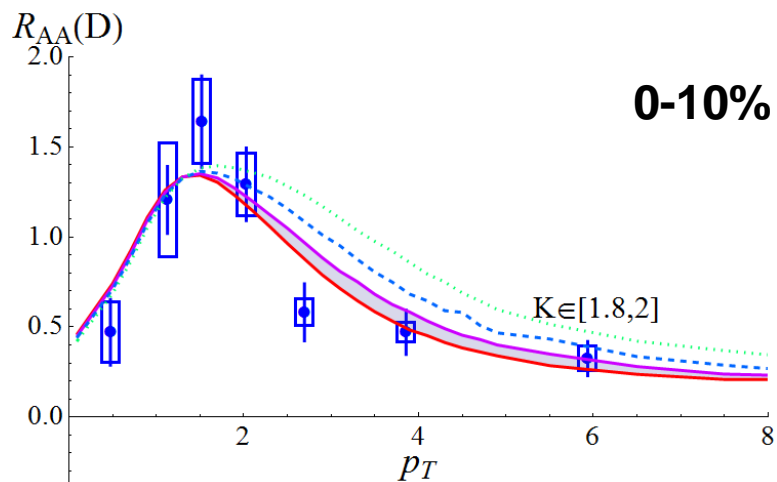
For the hydro code of Kolb and Heinz:

$K = 1$ compatible with data

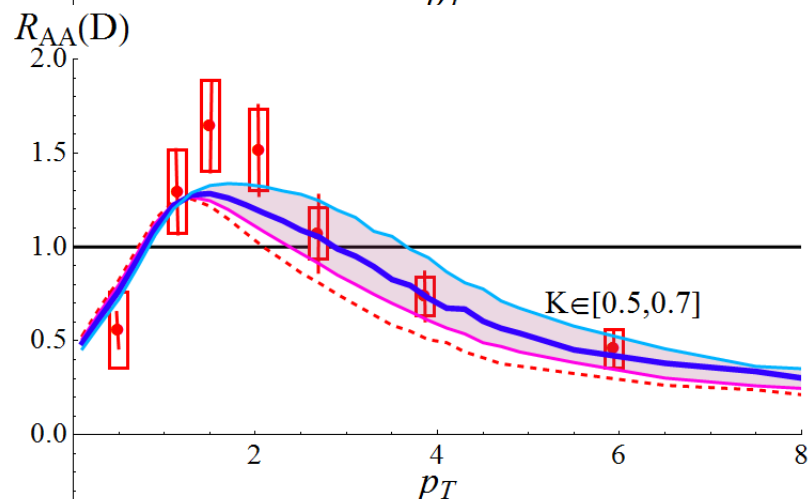
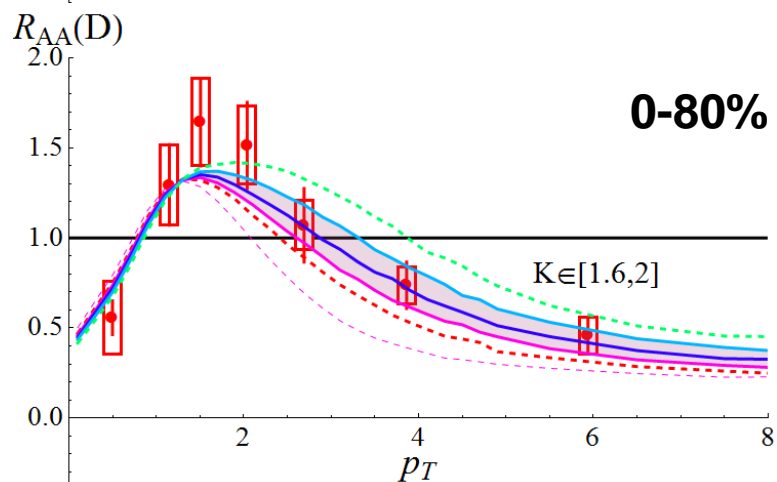
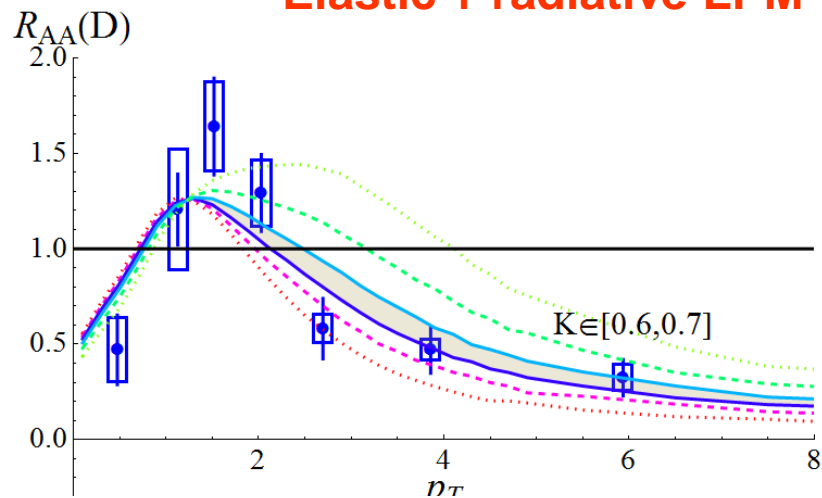
$K = 0.7$ best description – remember influence of expansion

RHIC: D mesons

Elastic

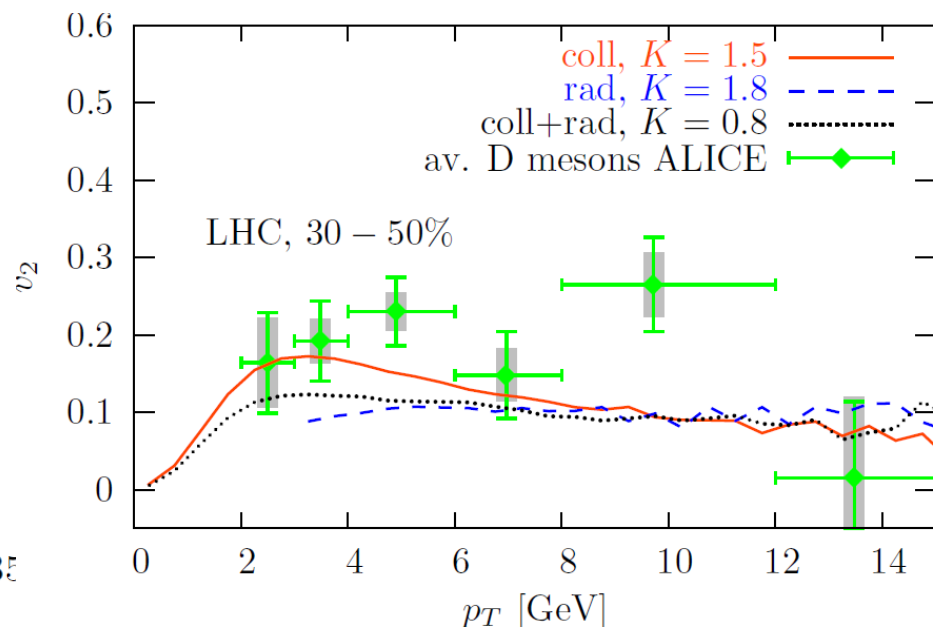
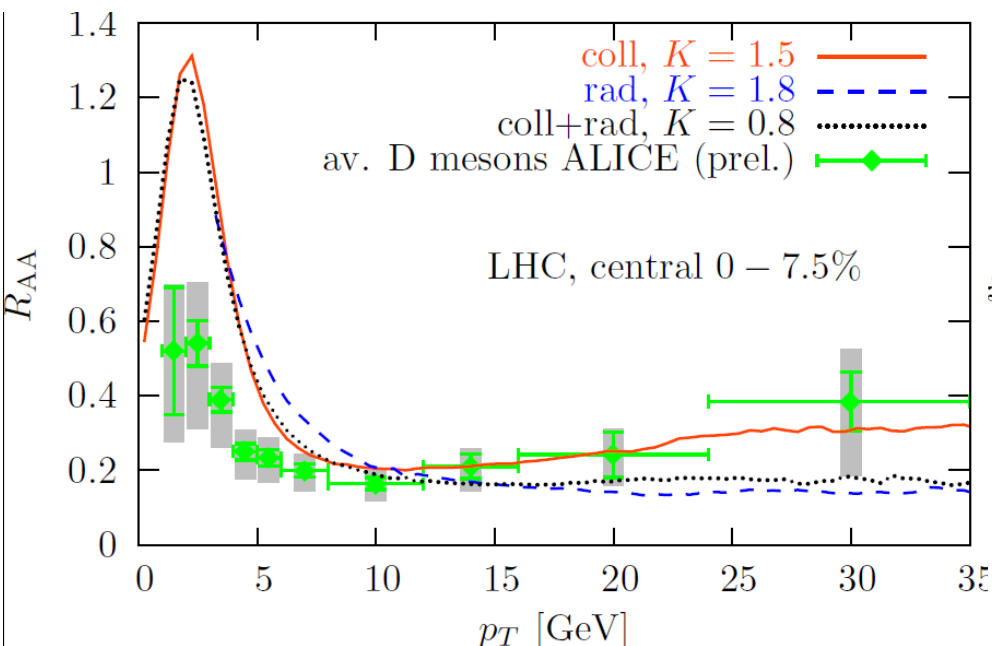


Elastic + radiative LPM



No form difference between coll and coll + rad

LHC : EPOS event generator

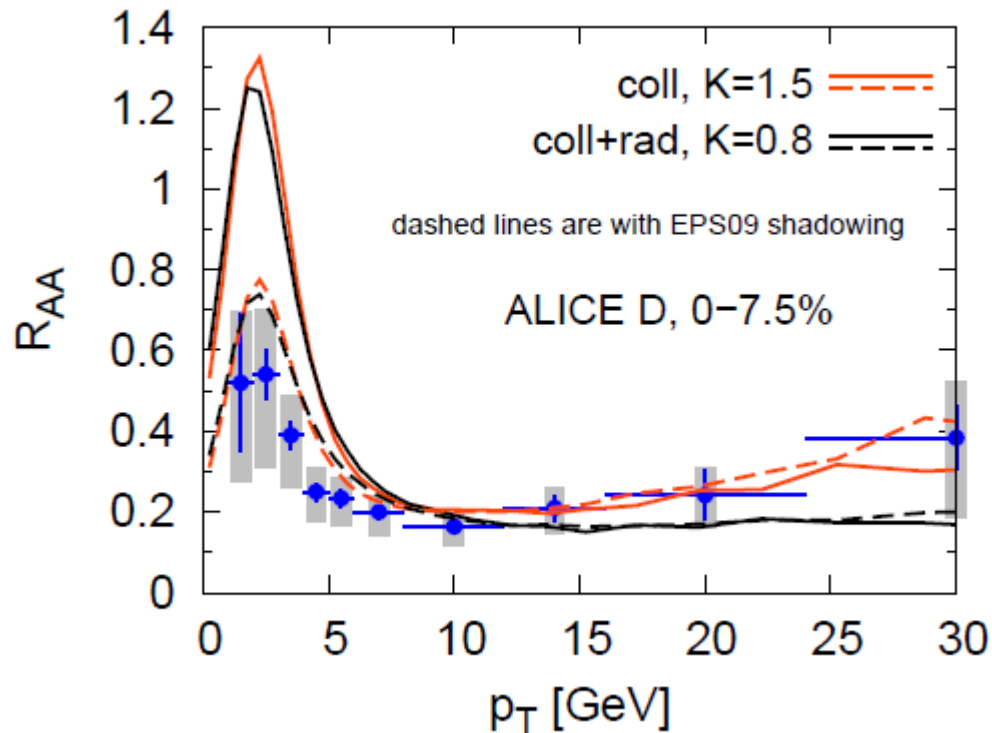


Three options :
 Collisions only K factor = 1.5
 Collision and radiation K = 0.8
 Radiation only K= 1.8

R_{AA} and v_2 for coll and coll + radiative about the same

Discussion of our results

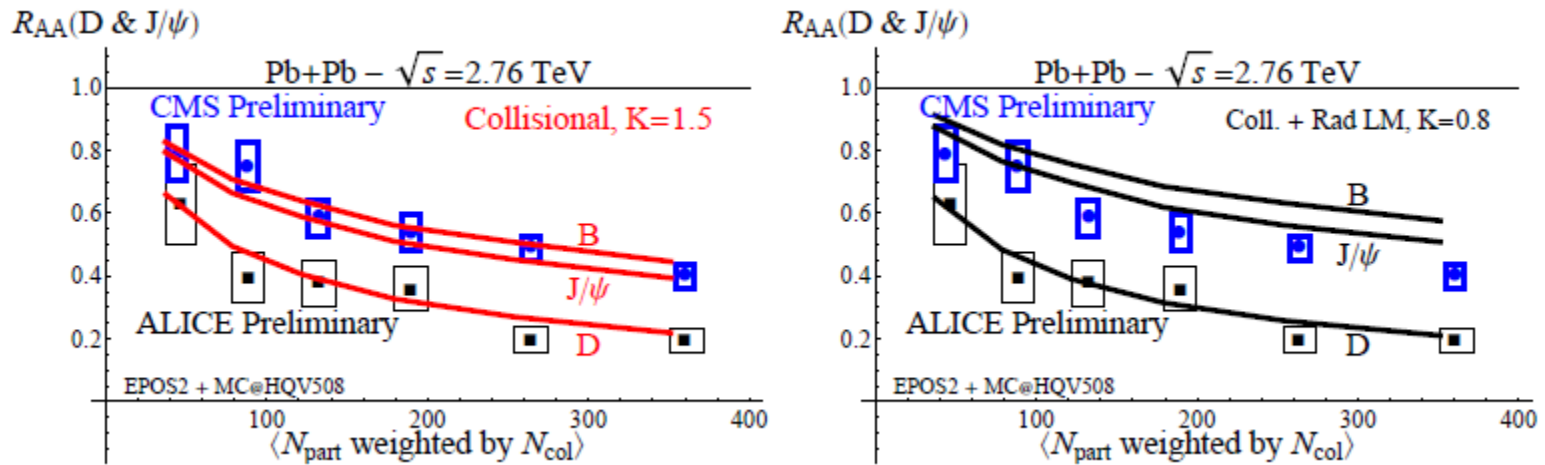
I) R_{AA}



Shadowing effects may **suppress strongly** the R_{AA} at small p_t
Anti-shadowing visible but not strong at large p_t

Shadowing has little influence on v_i

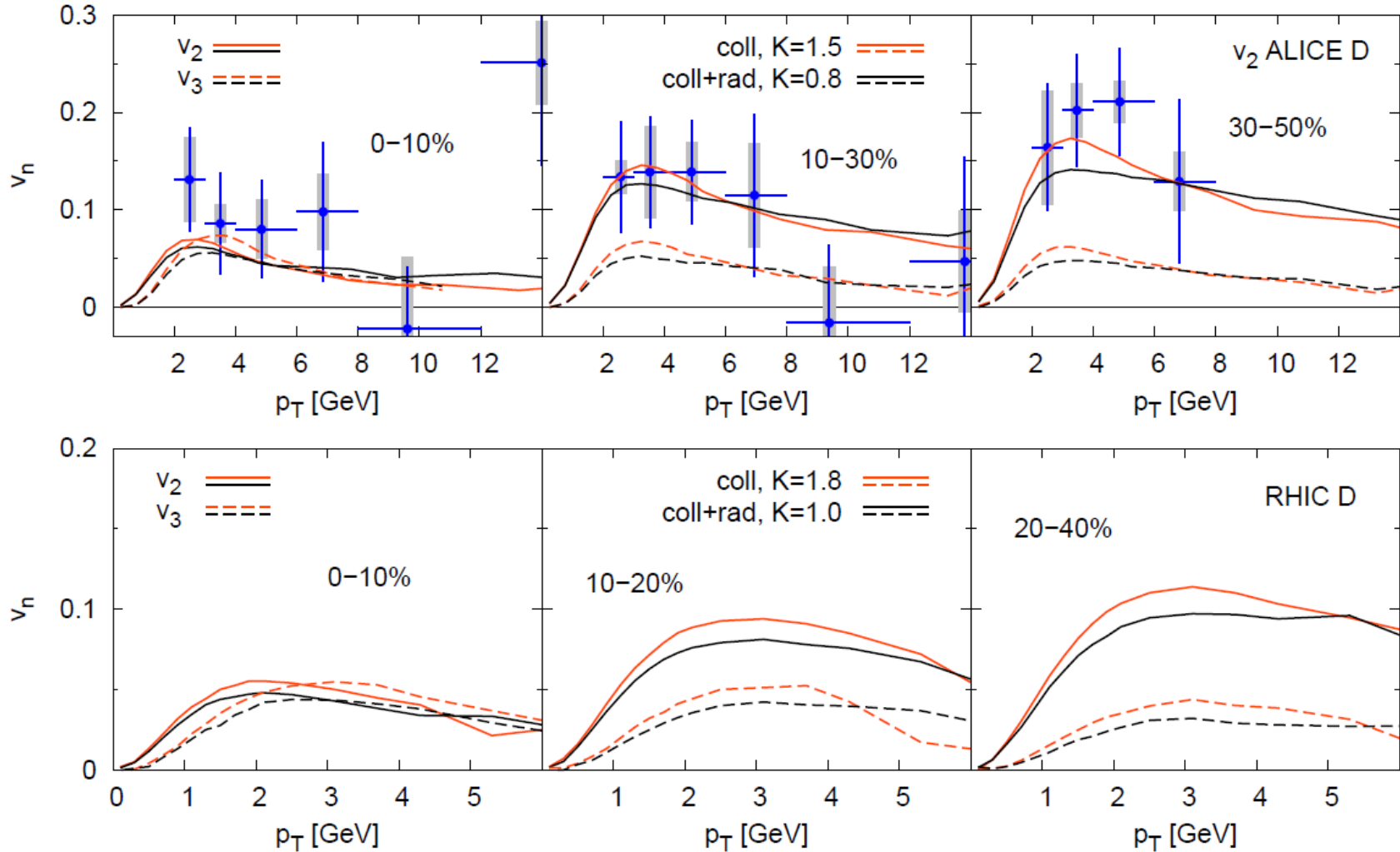
The different R_{AA} of D and B mesons seem to be verified experimentally (by comparing two different experiments)



ALICE D meson R_{AA} , $6 < p_T < 12$ GeV/c, $|y| < 0.5$

CMS Preliminary Non-prompt J/ ψ R_{AA} , $6.5 < p_T < 30$ GeV/c $|y| < 1.2$

Heavy quarks show also a finite v_3 and finite higher moments

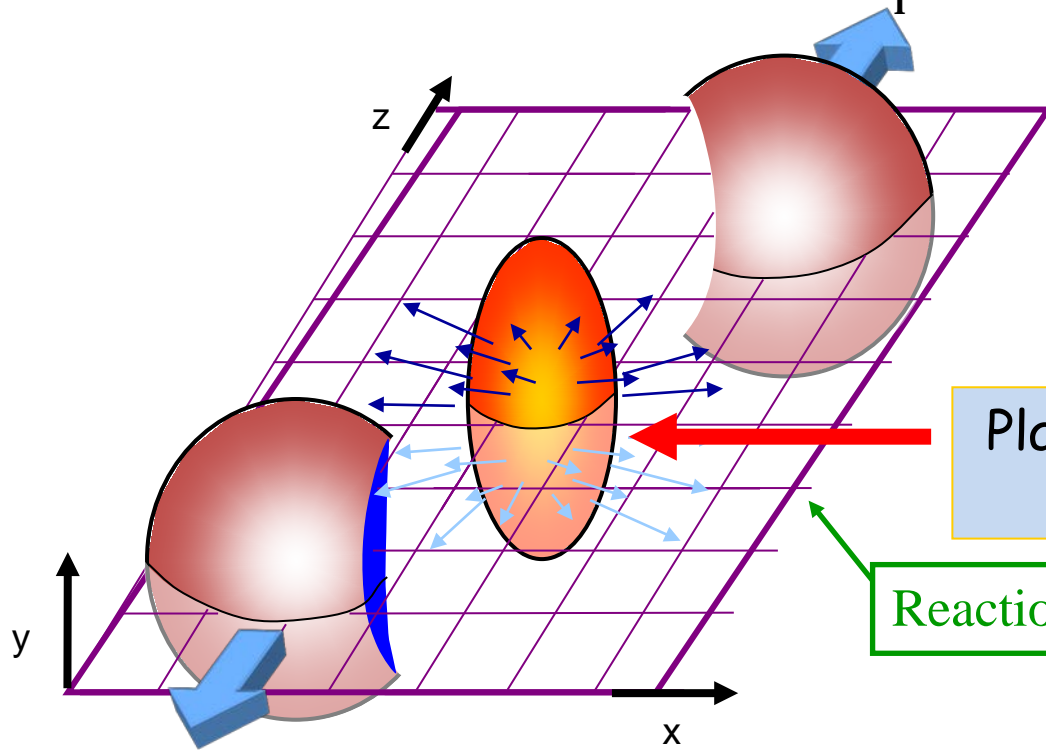


What can one learn from these results?

v_2 decreases with centrality -> understandable with the decrease of ϵ_2

v_3 independent of centrality -> fluctuations

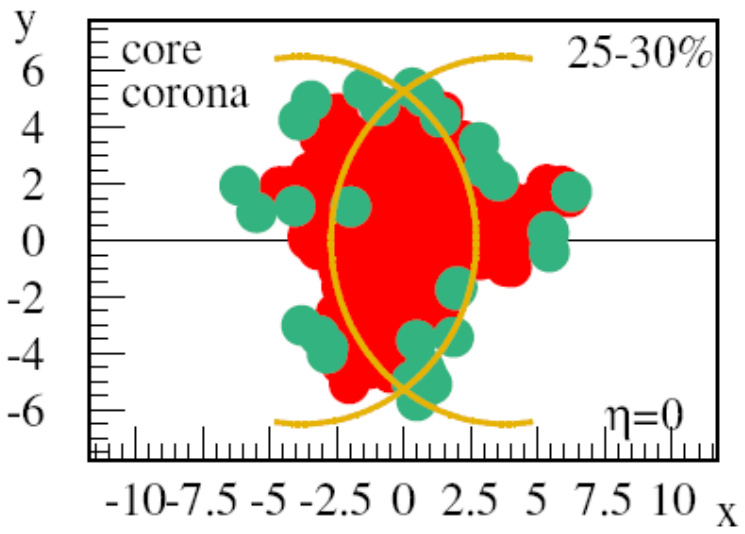
Where do the finite v_i come from?



In the ideal world the plasma should have only v_2

Plasma to be studied

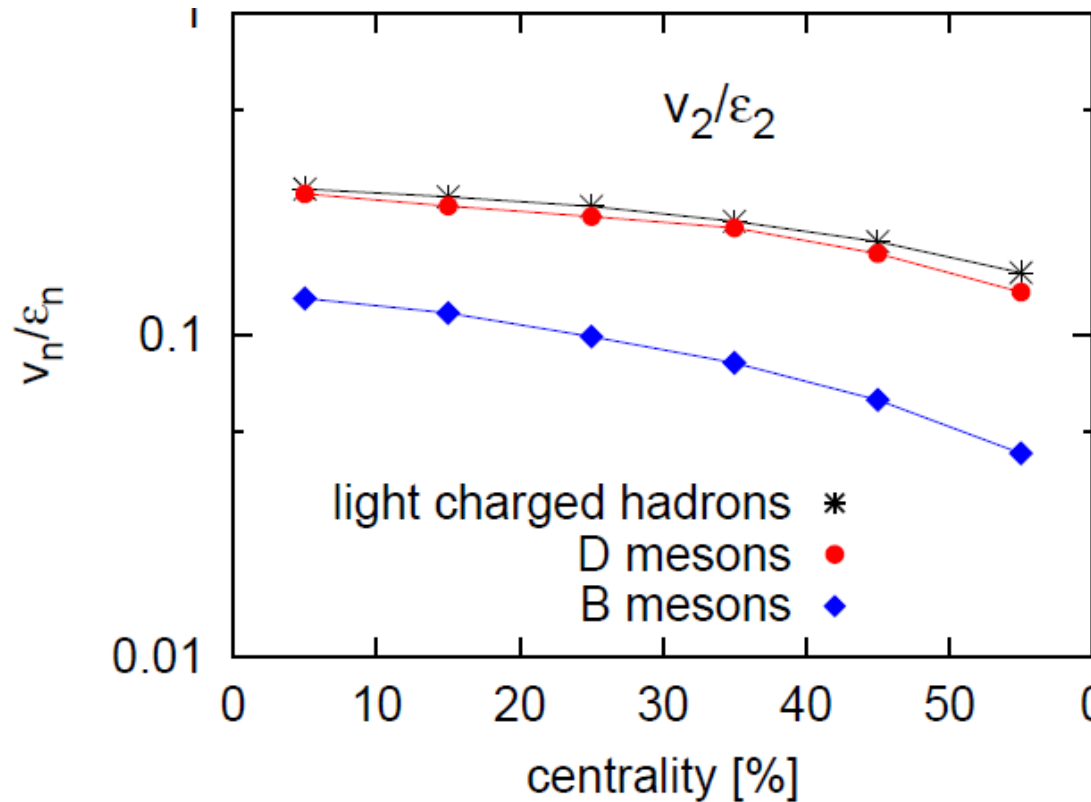
Reaction plane



In the real world (EPOS) the plasma has all kinds of moments v_i the v_i impair are fluctuations

v_3 corresponds to a Mercedes Star

Very surprising : v_2/ϵ_2 : same for light hadrons and D mesons



Light quarks: **hydro-dynamical pressure** caused by **spatial eccentricity**
 v_2/ϵ_2 const for ideal hydro, centrality dependent for viscous hydro

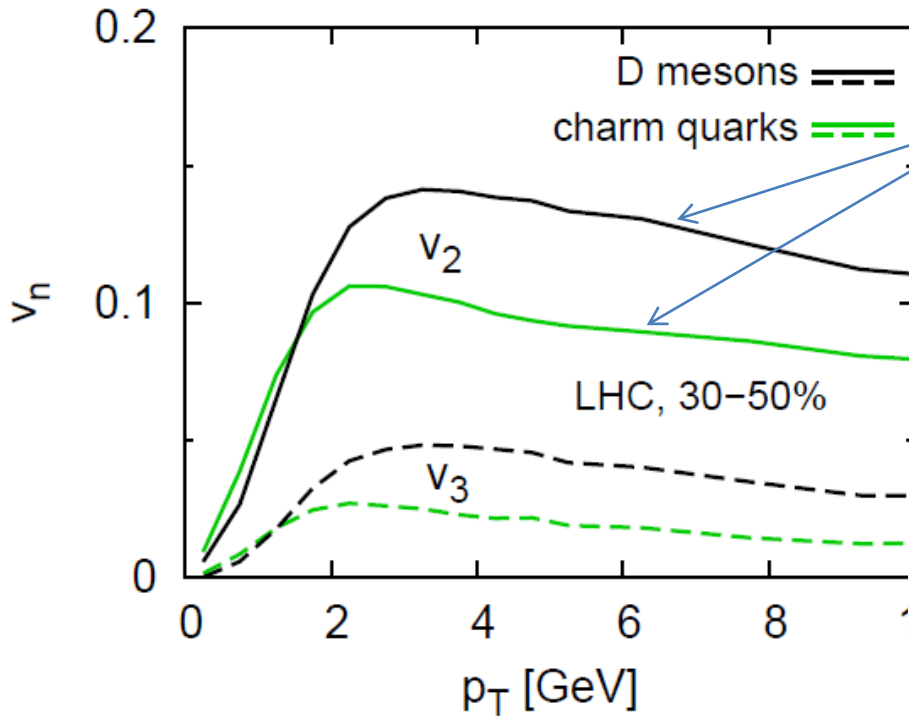
Heavy quarks: **No initial v_2** (hard process)

v_2 only due to interaction with q and g

v_2 of heavy quarks is created later measures the interaction time

Bottom quarks are too heavy to follow

More detailed analysis of the flow

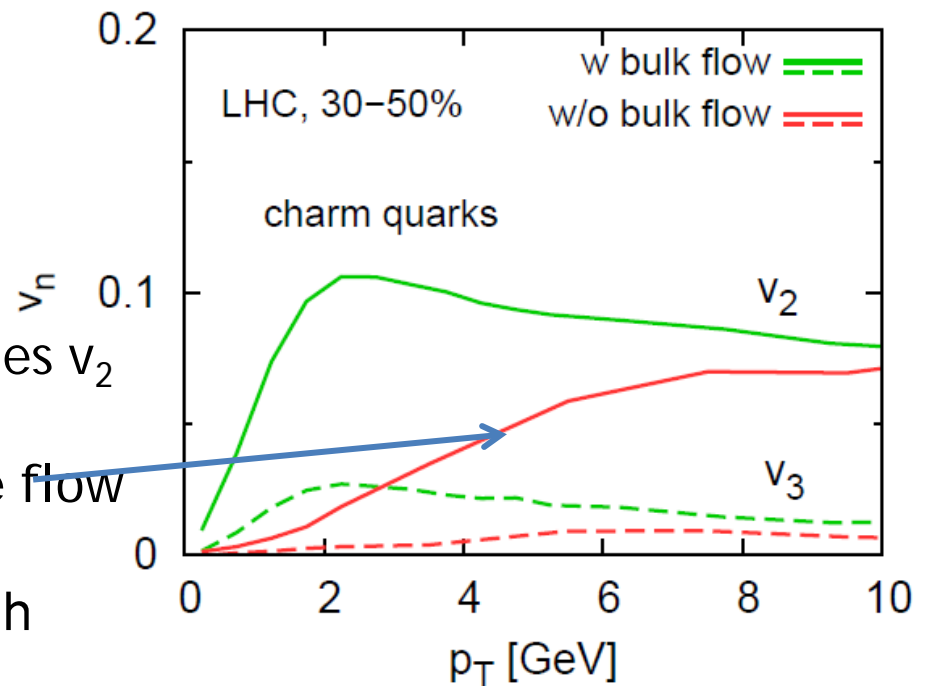


20% of v_2 due to the hadronisation uncertainty
whether fragmentation or coalescence is not essential for v_2

Verification that collective flow creates v_2

Artificial elimination of the collective flow

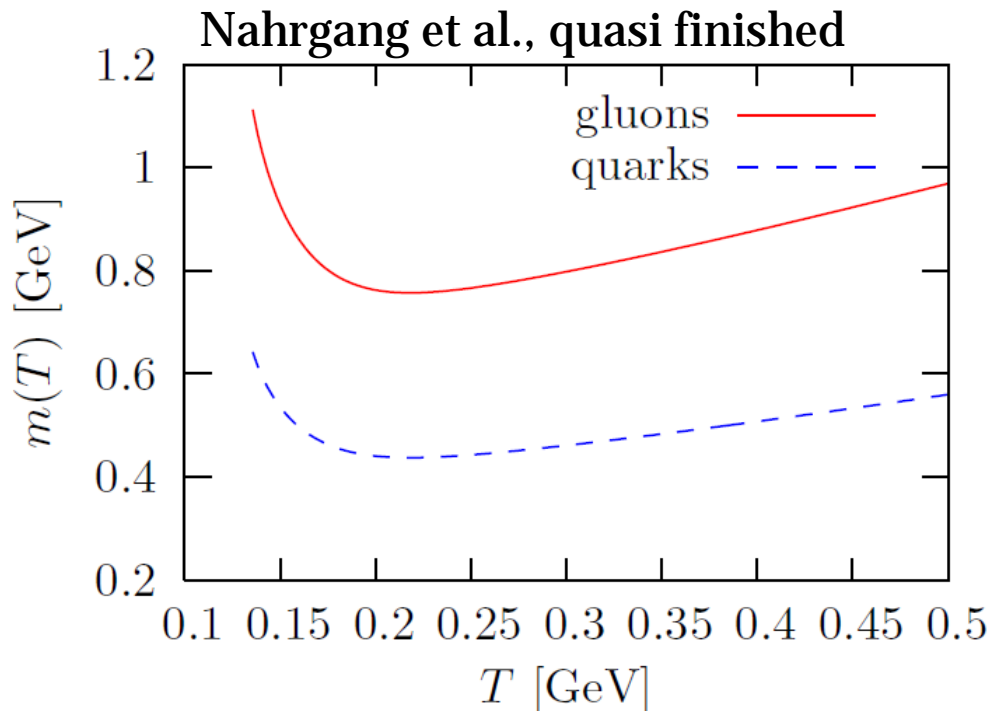
High momentum: different path length in and out of plane



Up to now we have assumed that the plasma consists of **zero mass quark and gluons**

This is however not proven. The lattice EOS can **be well modeled by assuming large masses of quarks and gluons**

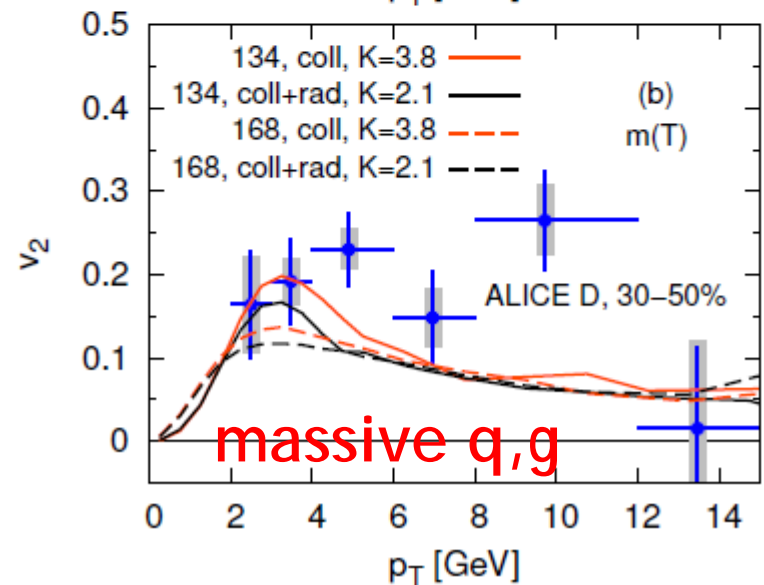
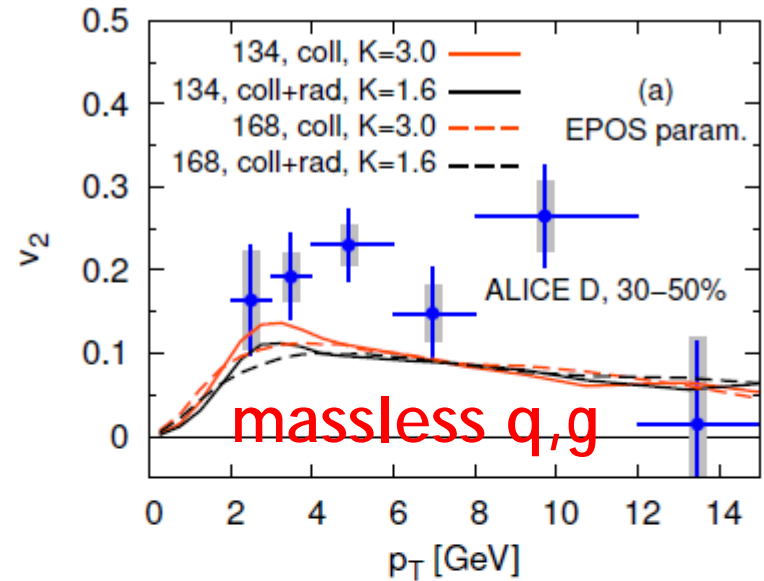
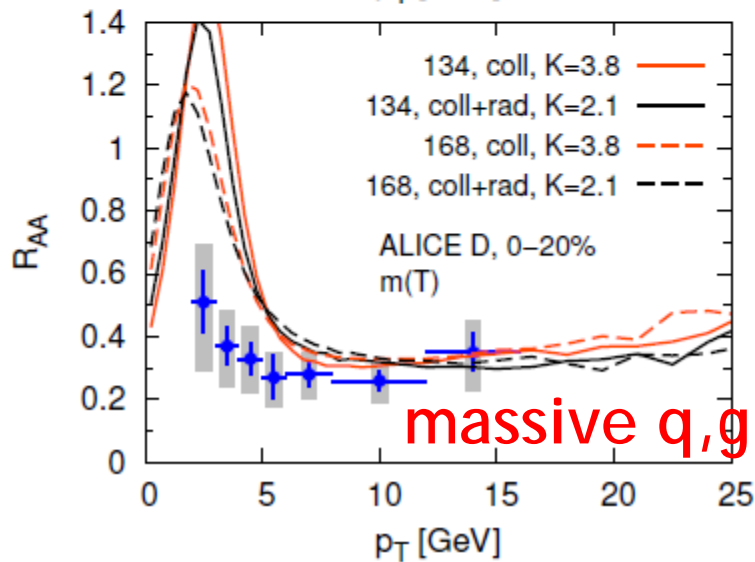
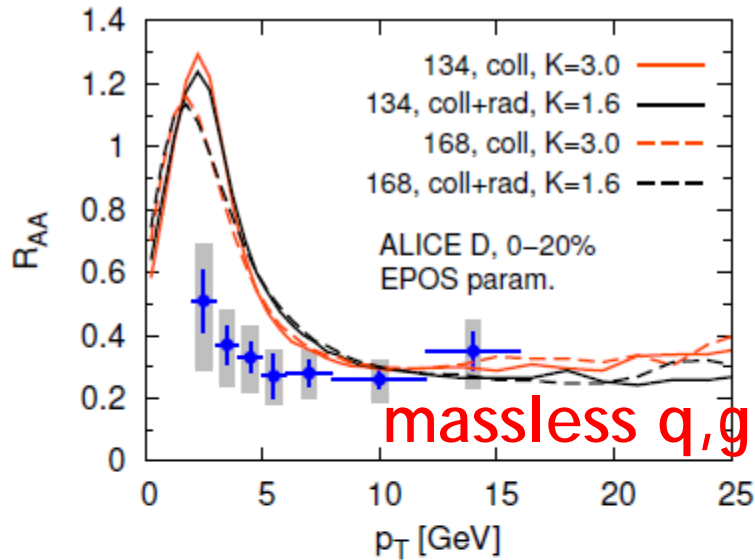
DQPM (Dynamical quasi particle model)
(Kaempfer, Peshier, Bluhm, Cassing, Bratkovskaya)



Simpler as PHSD approach
(no width of the particles
no potential interaction)

but masses are numerically
quite close

Using Epos as event generator for the plasma the differences are minor



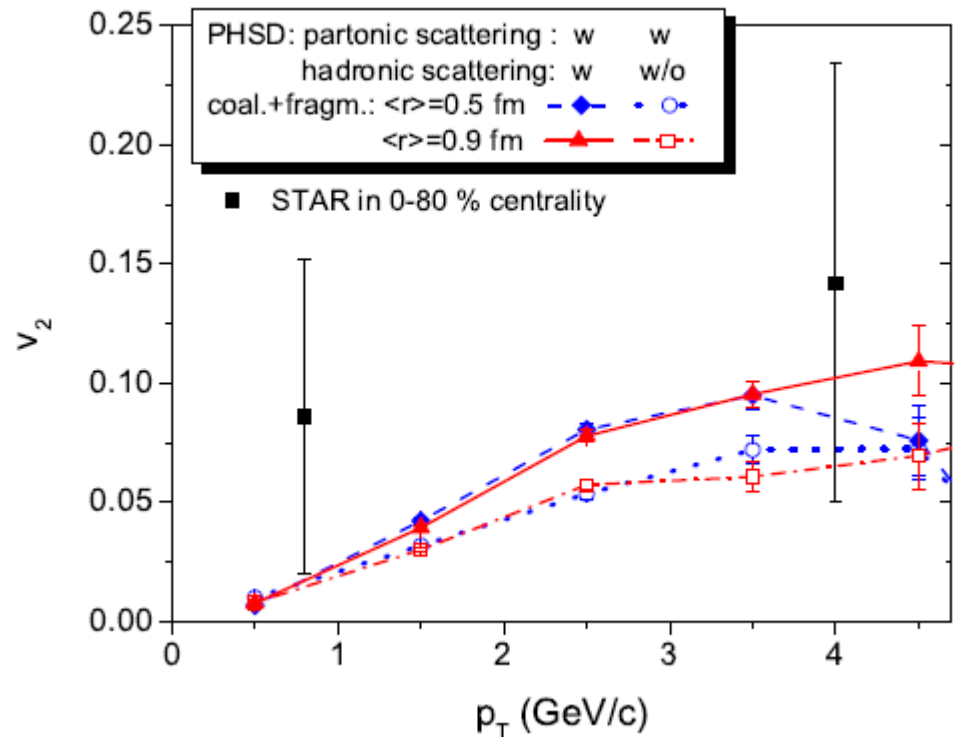
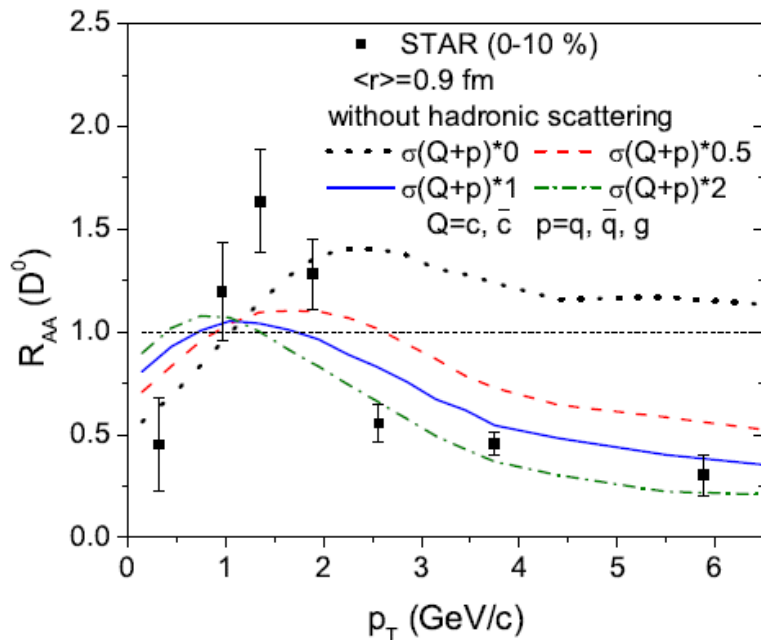
... but then we realized that PHSD just need $K=1$
to reproduce the data

(taisoo et al. arxiv 1503.03039)

hydrodynamics \leftrightarrow non-equilibrium ?

different initial conditions ?

different hadronization ?



Conclusions

All **experimental midrapidity RHIC and LHC data are compatible** with the assumption that

pQCD describes energy loss and elliptic flow v_2 of heavy quarks.

The present heavy quark data **do not allow for discriminating** between different pQCD processes:
radiative and collisional energy loss

Special features

running coupling constant

adjusted Debye mass

Landau Pomeranschuk Migdal

Description of the **expansion** of the medium (freeze out, initial cond.) has to be controlled by light hadrons (->EPOS)

Collaborators

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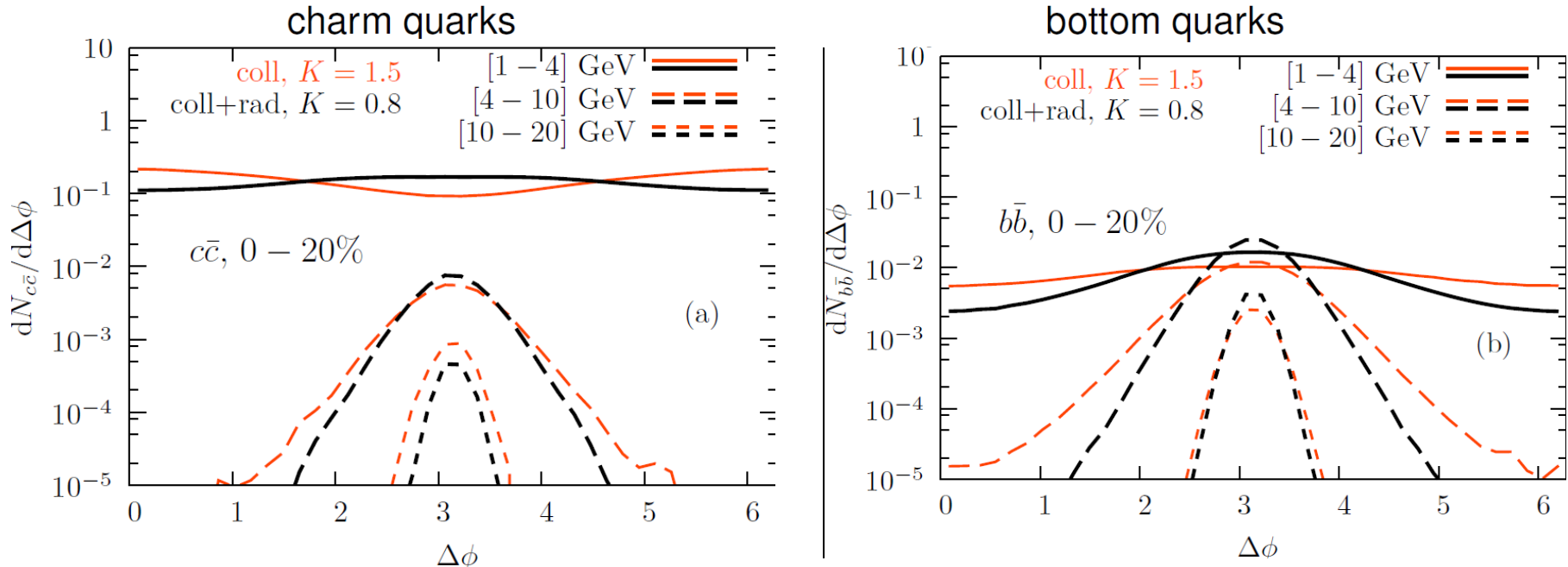
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Duke

Marlene Nahrgang
Steffen Bass

Heavy-quark azimuthal correlations

central collisions, back-to-back initialization, no background from uncorrelated pairs



- Stronger broadening in a purely **collisional** than in a **collisional+radiative** interaction mechanism
- Variances in the intermediate p_T -range:
0.18 vs. **0.094** (charm) and **0.28** vs. **0.12** (bottom)
- At low p_T initial correlations are almost washed out: small residual correlations remain for the **collisional+radiative** mechanism, “partonic wind” effect for a purely **collisional** scenario.
- Initial correlations survive the propagation in the medium at higher p_T .