

# Chiral symmetry restoration versus deconfinement

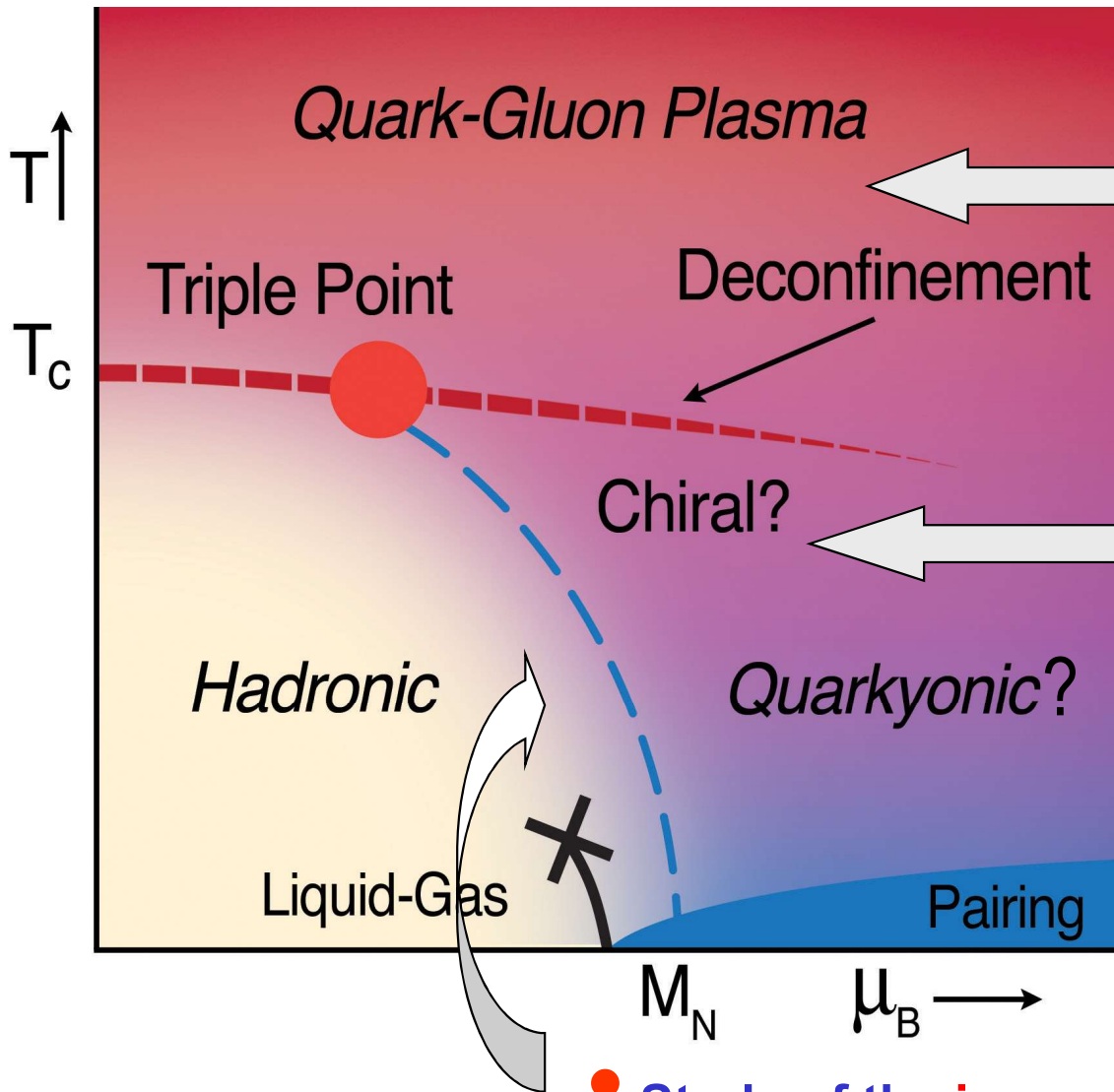
Elena Bratkovskaya

(GSI, Darmstadt & Uni. Frankfurt)

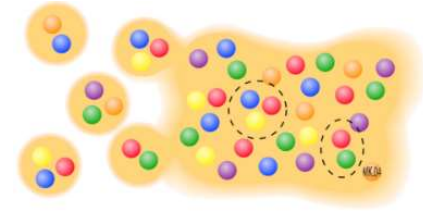


# The ,holy grail‘ of heavy-ion physics:

The phase diagram of QCD



- Search for the **critical point**



- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**

- Search for the signatures of **chiral symmetry restoration**

- Study of the **in-medium** properties of hadrons at high baryon density and temperature

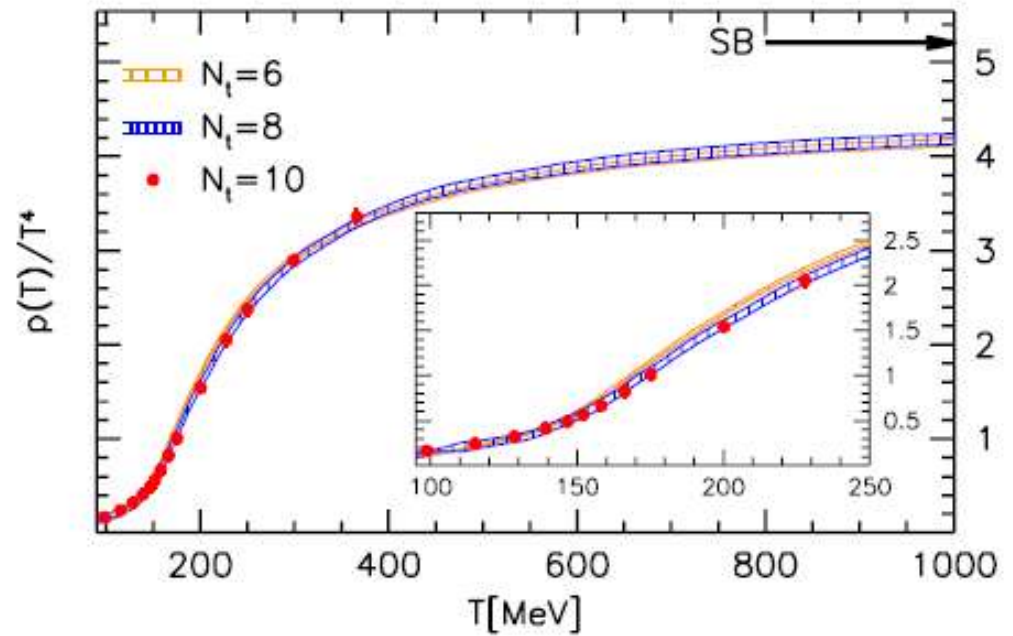
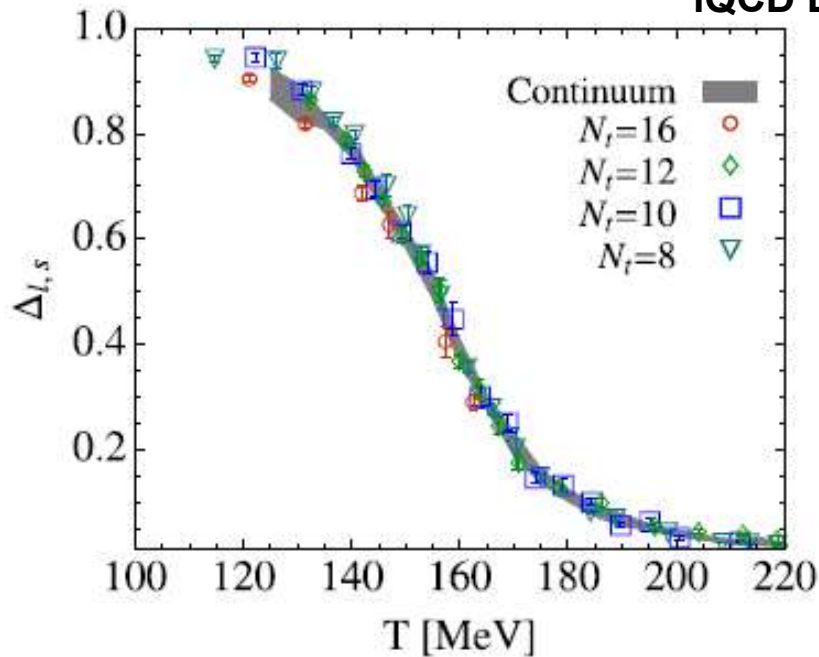
# Information from lattice QCD

chiral symmetry restoration  
with increasing temperature

+

deconfinement phase transition  
with increasing temperature

IQCD BMW collaboration:



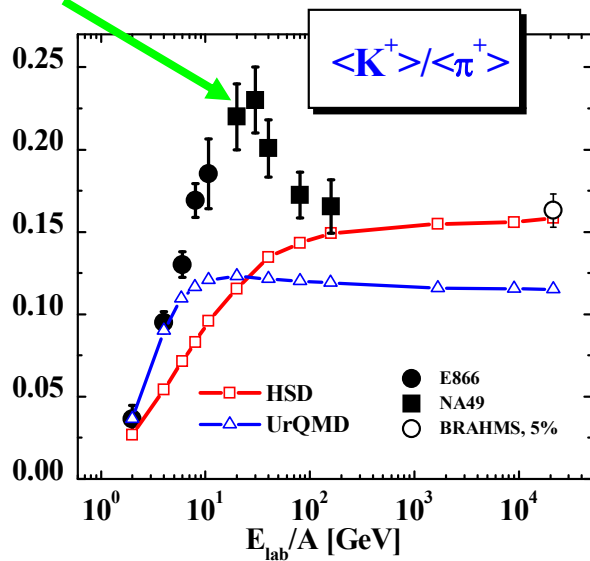
$$\Delta_{l,s} \sim \frac{\langle \bar{q}q \rangle_T}{\langle \bar{q}q \rangle_0}$$

**crossover:** both transitions occur at about the same temperature  $T_C$   
for low chemical potentials

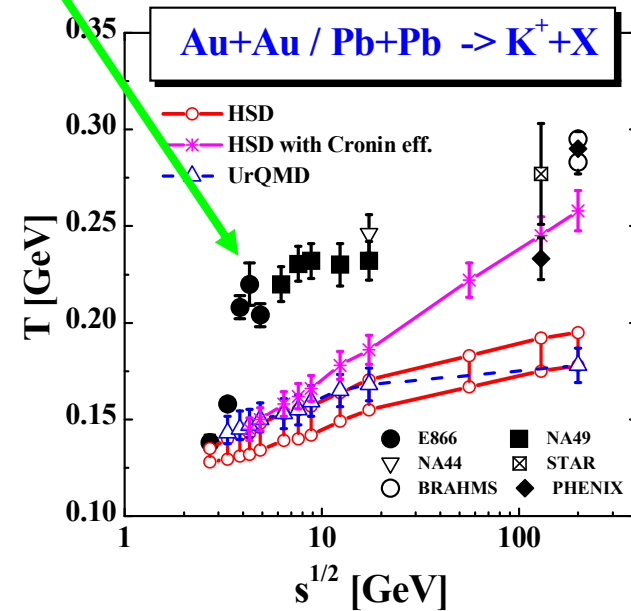
# Hadron-string transport models (HSD, UrQMD) versus observables at ~ 2000

□, 'horn' in  $K^+/\pi^+$

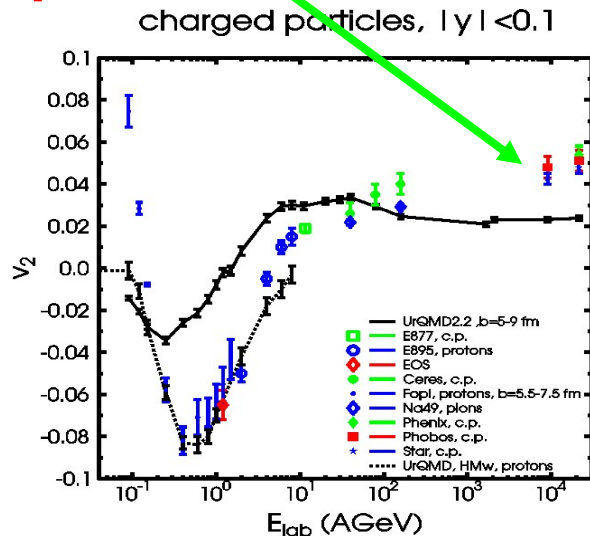
NA49: PRC66 (2002) 054902



□, 'step' in slope T



□ elliptic flow



Exp. data are not reproduced in terms of the hadron-string picture  
**→ evidence for partonic degrees of freedom + .... ?!**

HSD, UrQMD: PRC 69 (2004) 032302

# Dynamical description of heavy-ion collisions

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## The goal:

to study the properties of **strongly interacting matter** under extreme conditions from a microscopic point of view

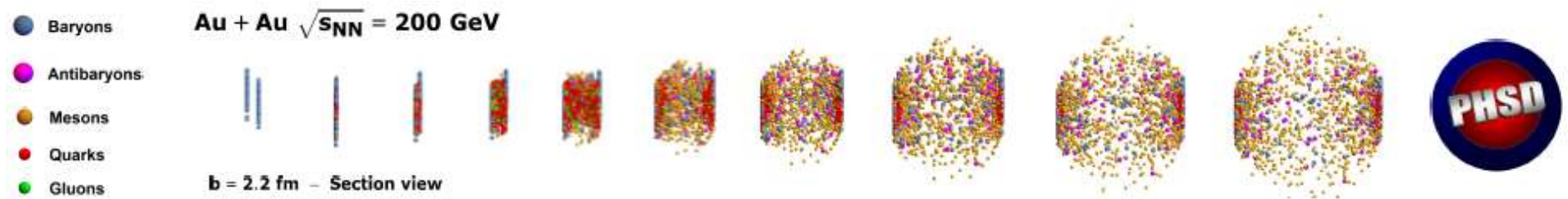
## Realization:

to develop a **dynamical many-body transport approach**

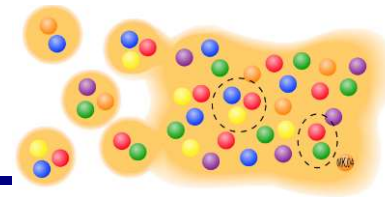
1) applicable for strongly interacting systems,  
which includes:

2) phase transition from hadronic matter to QGP

3) chiral symmetry restoration



# From SIS to LHC: from hadrons to partons



**The goal:** to study of the phase transition from hadronic to partonic matter and properties of the Quark-Gluon-Plasma on a **microscopic level**

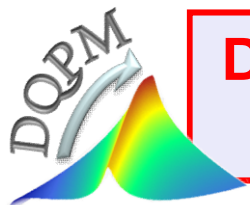
→ need a **consistent non-equilibrium transport approach**

- ❑ with explicit **parton-parton interactions** (i.e. between quarks and gluons)
- ❑ explicit **phase transition** from hadronic to partonic degrees of freedom
- ❑ **IQCD EoS** for partonic phase (‘cross over’ at  $\mu_q=0$ )
- ❑ **Transport theory for strongly interacting systems:** off-shell Kadanoff-Baym equations for the Green-functions  $S_h^<(x,p)$  in phase-space representation for the **partonic** and **hadronic phase**



→ **Parton-Hadron-String-Dynamics (PHSD)**

**QGP phase is described by**



**Dynamical QuasiParticle Model  
(DQPM)**

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215;  
W. Cassing, EPJ ST 168 (2009) 3

A. Peshier, W. Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

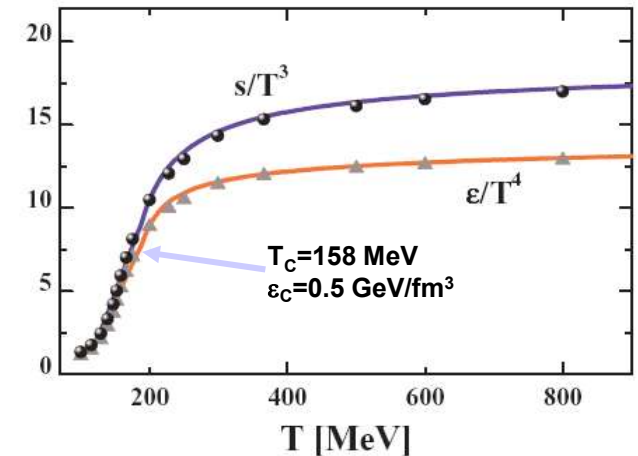
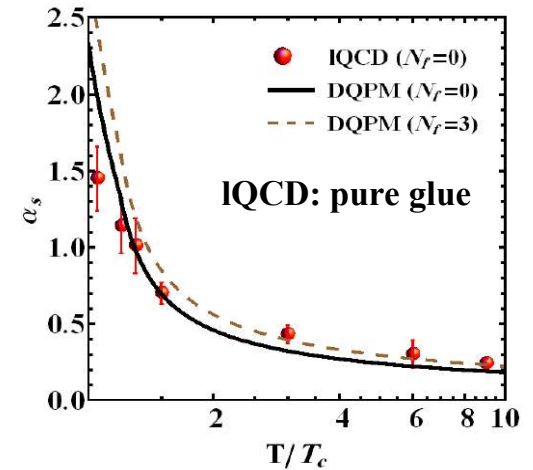
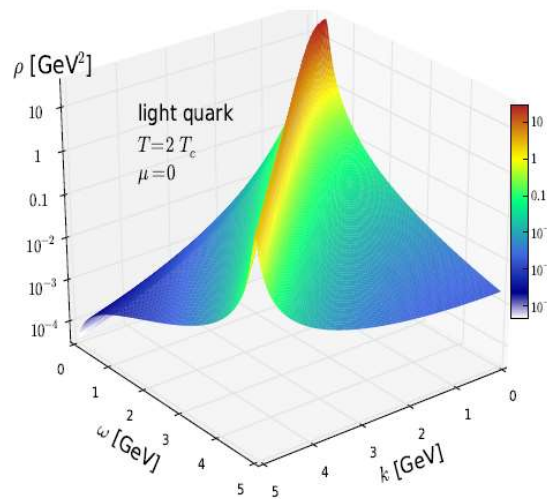
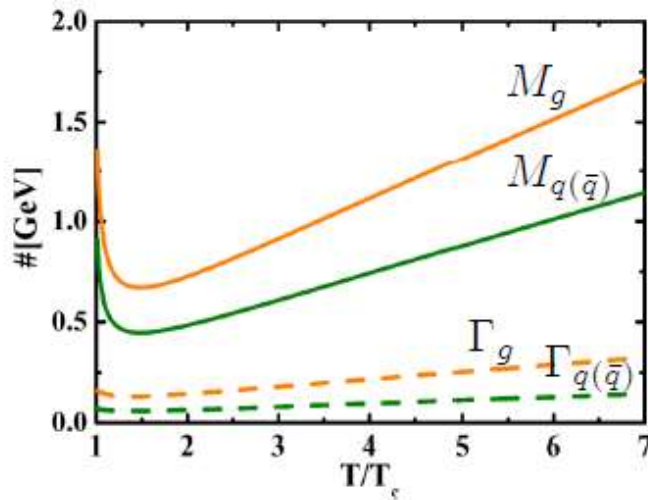
# The Dynamical QuasiParticle Model (DQPM)

- Basic idea: **interacting quasi-particles**: massive quarks and gluons ( $g, q, q_{\text{bar}}$ ) with **Lorentzian spectral functions** :

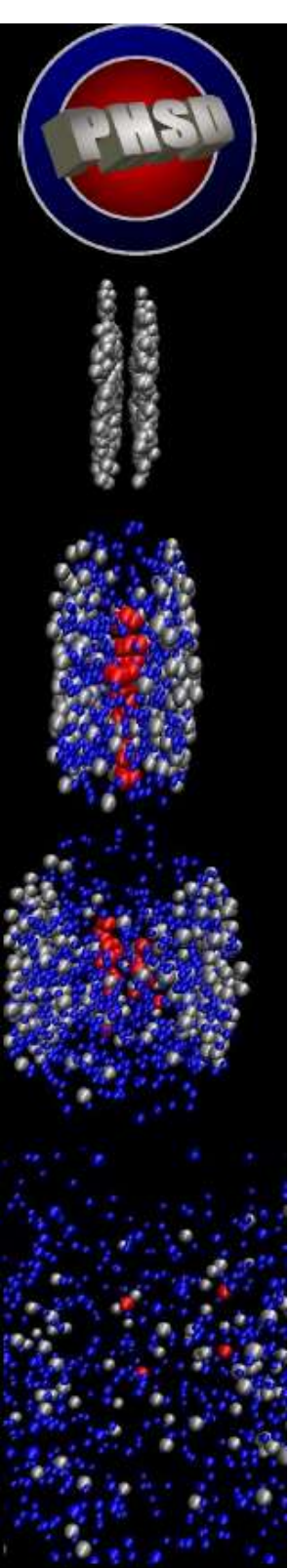
$$\rho_i(\omega, T) = \frac{4\omega\Gamma_i(T)}{\left(\omega^2 - \vec{p}^2 - M_i^2(T)\right)^2 + 4\omega^2\Gamma_i^2(T)} \quad (i = q, \bar{q}, g)$$

- Modeling of the **quark/gluon masses and widths**  $\rightarrow$  HTL limit at high  $T$  with 3 model parameters – fitted to lattice QCD data

$\rightarrow$  **Quasi-particle properties**:  
large width and mass for gluons and quarks



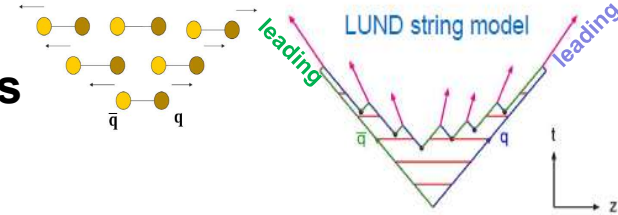
- DQPM** provides **mean-fields (1PI)** for gluons and quarks as well as **effective 2-body interactions (2PI)**
- DQPM** gives **transition rates** for the formation of hadrons  $\rightarrow$  **PHSD**



# Parton-Hadron-String-Dynamics (PHSD)

## Initial A+A collisions – HSD:

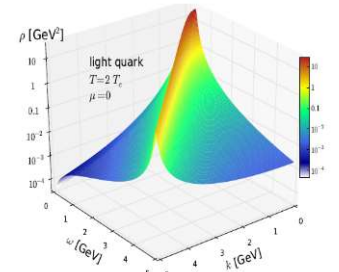
$N+N \rightarrow$  string formation  $\rightarrow$  decay to pre-hadrons



## Formation of QGP stage if $\epsilon > \epsilon_{\text{critical}}$ :

dissolution of pre-hadrons  $\rightarrow$  (DQPM)  $\rightarrow$

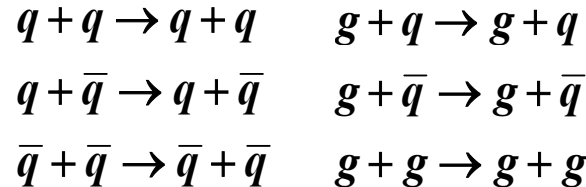
$\rightarrow$  massive quarks/gluons + mean-field potential  $U_q$



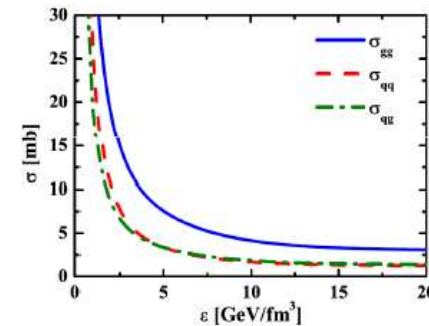
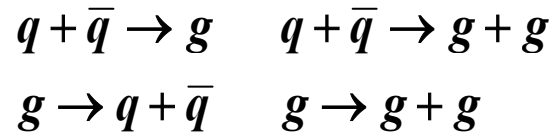
## Partonic stage – QGP:

based on the Dynamical Quasi-Particle Model (DQPM)

### (quasi-) elastic collisions:



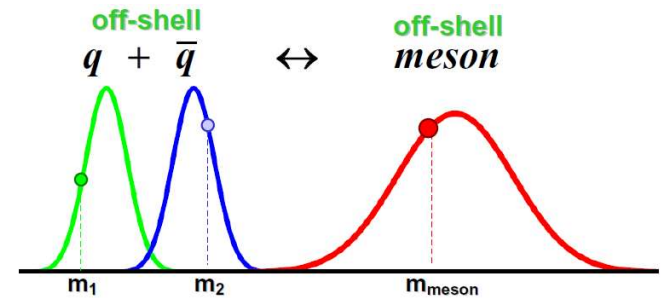
### inelastic collisions:



## Hadronization (based on DQPM):

$$g \rightarrow q + \bar{q}, \quad q + \bar{q} \leftrightarrow \text{meson (or 'string')}$$

$$q + q + q \leftrightarrow \text{baryon (or 'string')}$$



## Hadronic phase: hadron-hadron interactions – off-shell HSD

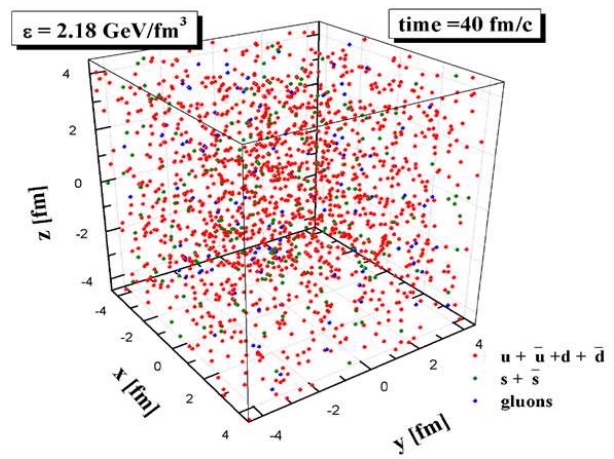




# QGP in equilibrium: Transport properties at finite $(T, \mu_q)$ : $\eta/s$

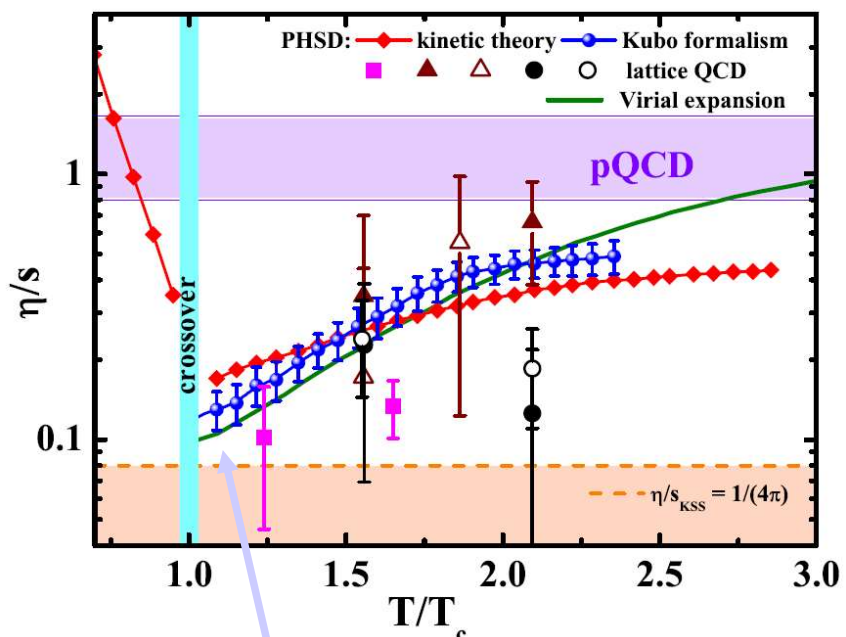
Infinite hot/dense matter =

PHSD in a box:



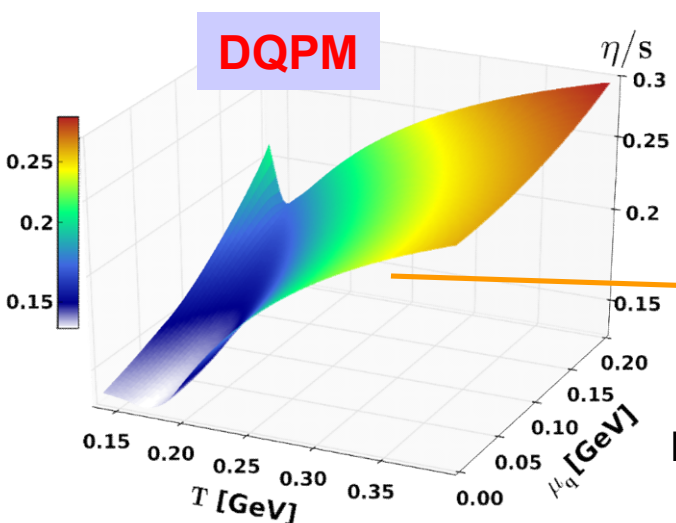
## Shear viscosity $\eta/s$ at finite T

V. Ozvenchuk et al., PRC 87 (2013) 064903



## Shear viscosity $\eta/s$ at finite $(T, \mu_q)$

**IQCD:** 
$$\frac{T_c(\mu_q)}{T_c(\mu_q = 0)} = \sqrt{1 - \alpha \mu_q^2} \approx 1 - \alpha/2 \mu_q^2 + \dots$$



**QGP in PHSD = strongly-interacting liquid-like system**

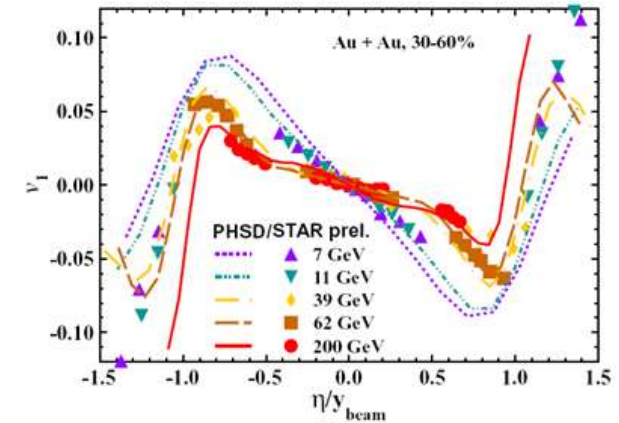
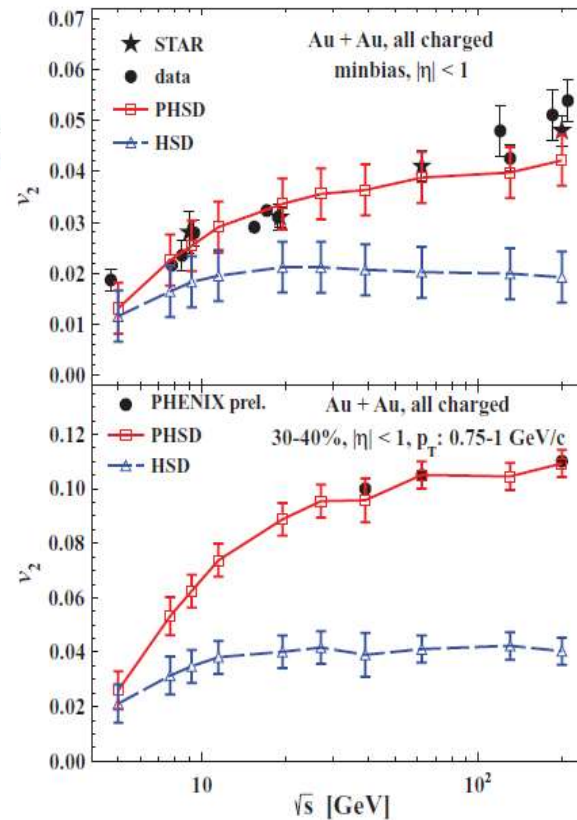
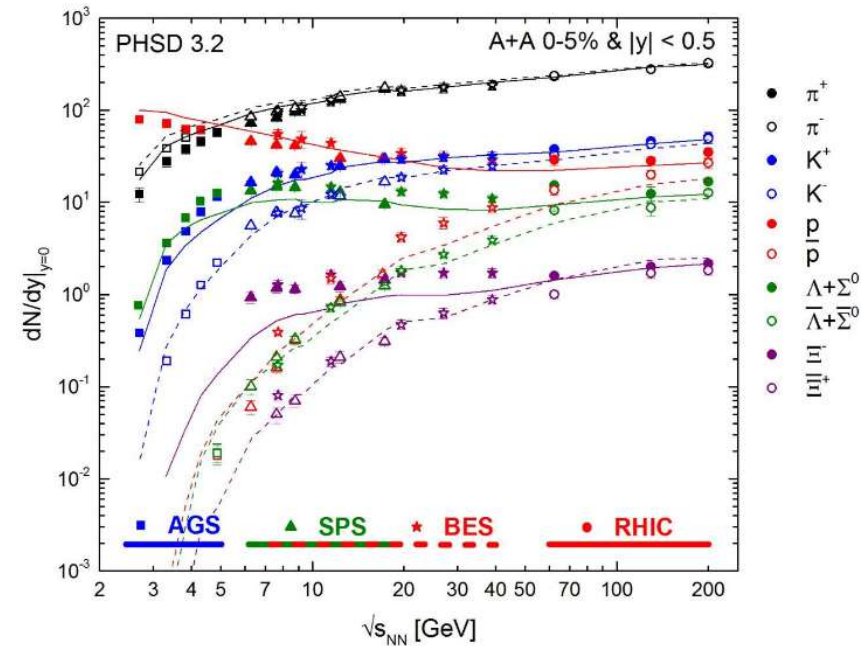
$\eta/s$ :  $\mu_q=0 \rightarrow$  finite  $\mu_q$ : smooth increase as a function of  $(T, \mu_q)$

Review: H. Berrehrhah et al. Int.J.Mod.Phys. E25 (2016) 1642003

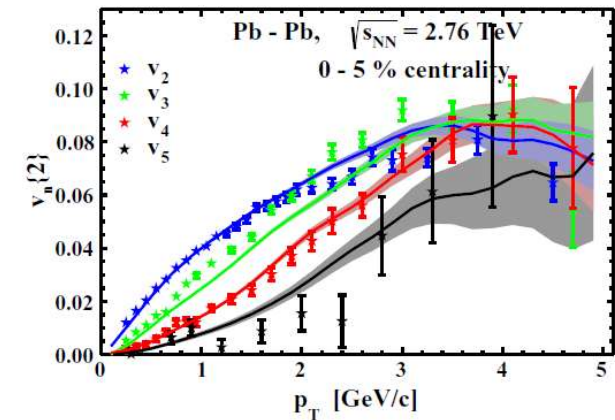
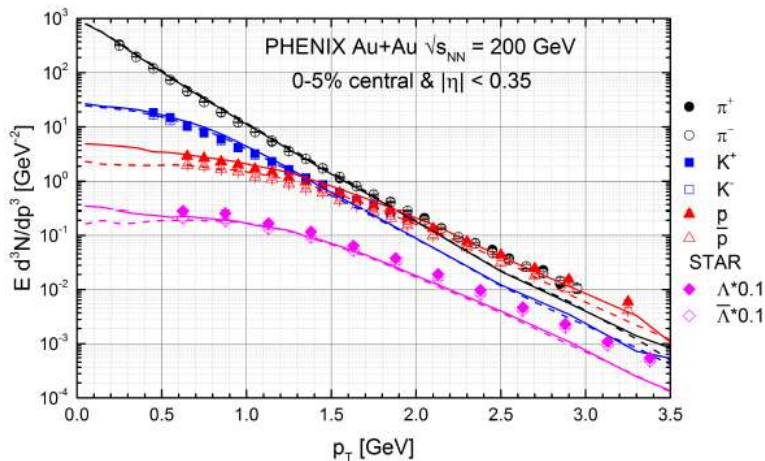


# Non-equilibrium dynamics: description of A+A with PHSD

## PHSD: highlights



### PHSD: P. Moreau



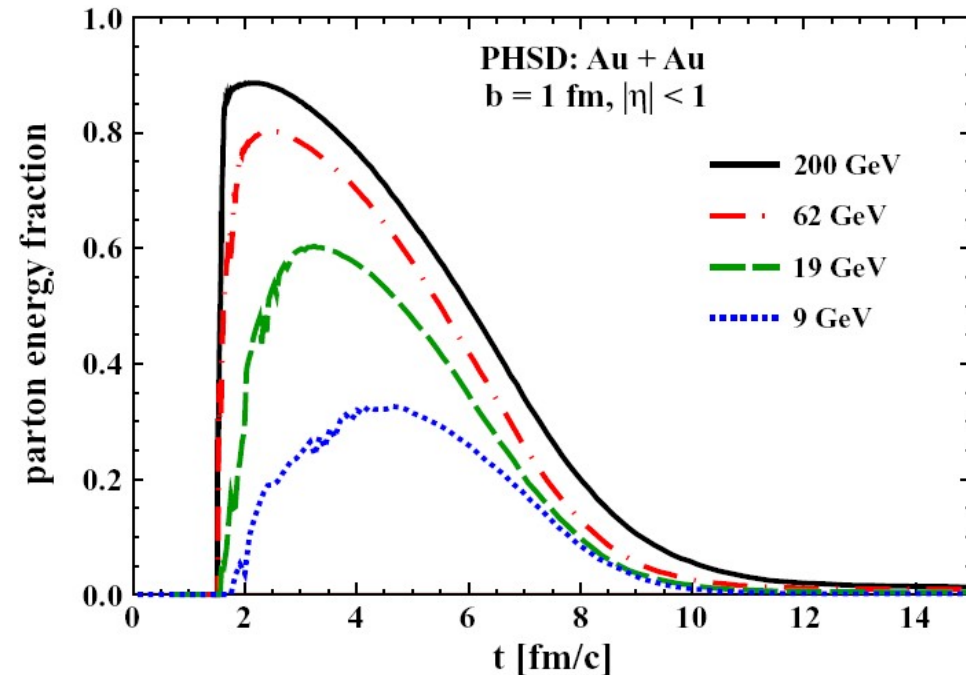
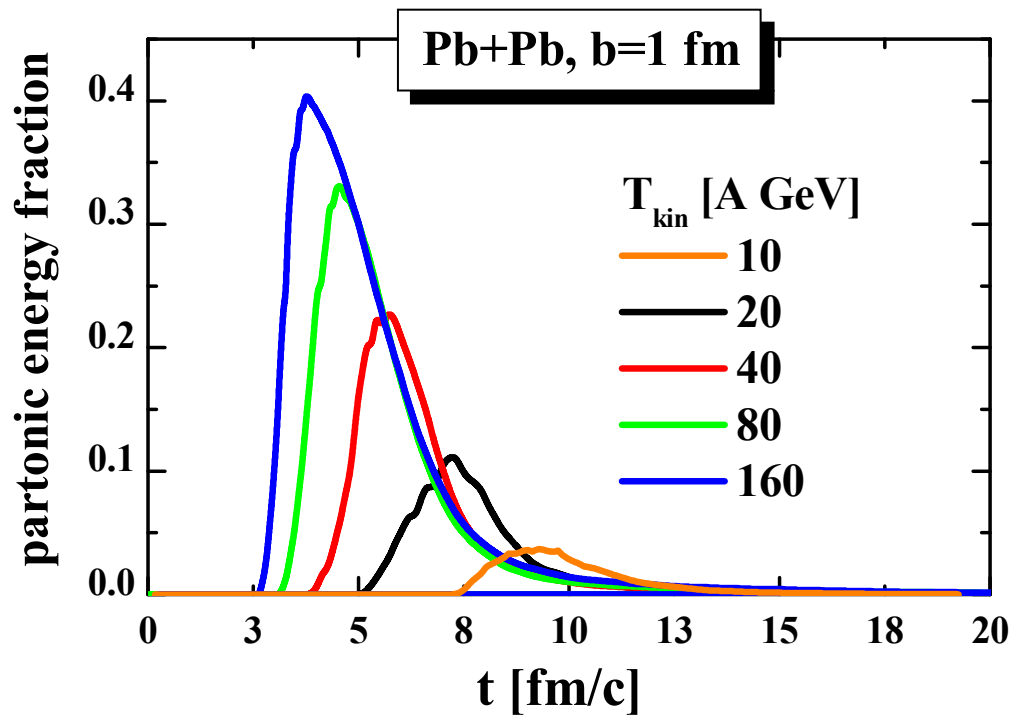
V. Konchakovski et al.,  
 PRC 85 (2012) 011902; JPG42 (2015) 055106

PHSD provides a good description of 'bulk' observables ( $y$ -,  $p_T$ -distributions, flow coefficients  $v_n$ , ...) from SPS to LHC



# Partonic energy fraction in central A+A

Time evolution of the partonic energy fraction vs energy at midrapidity



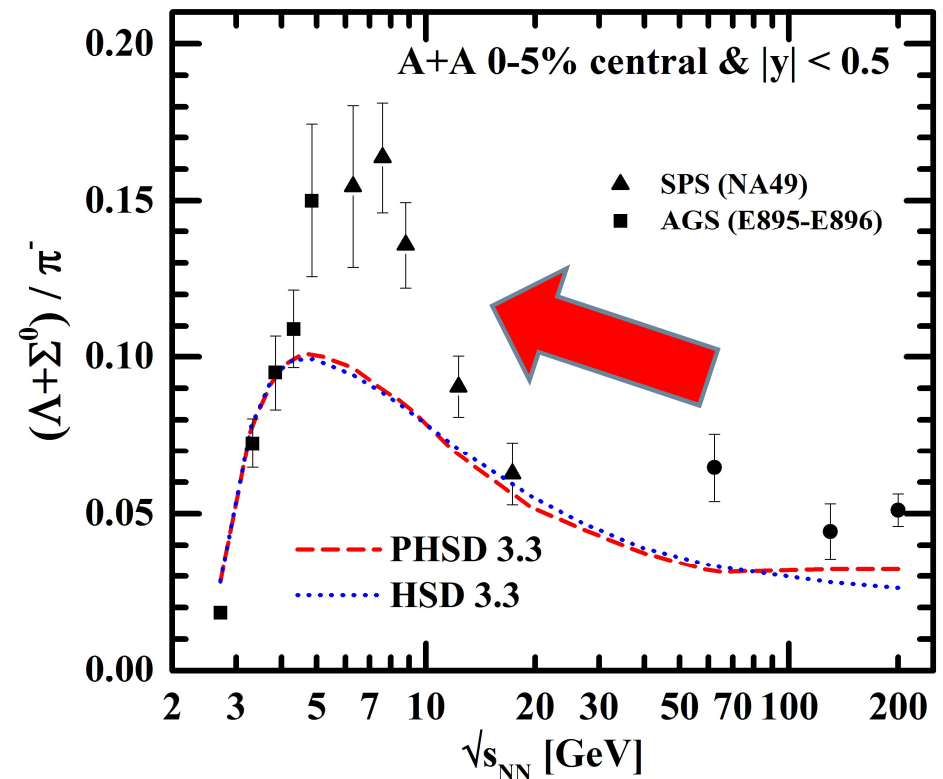
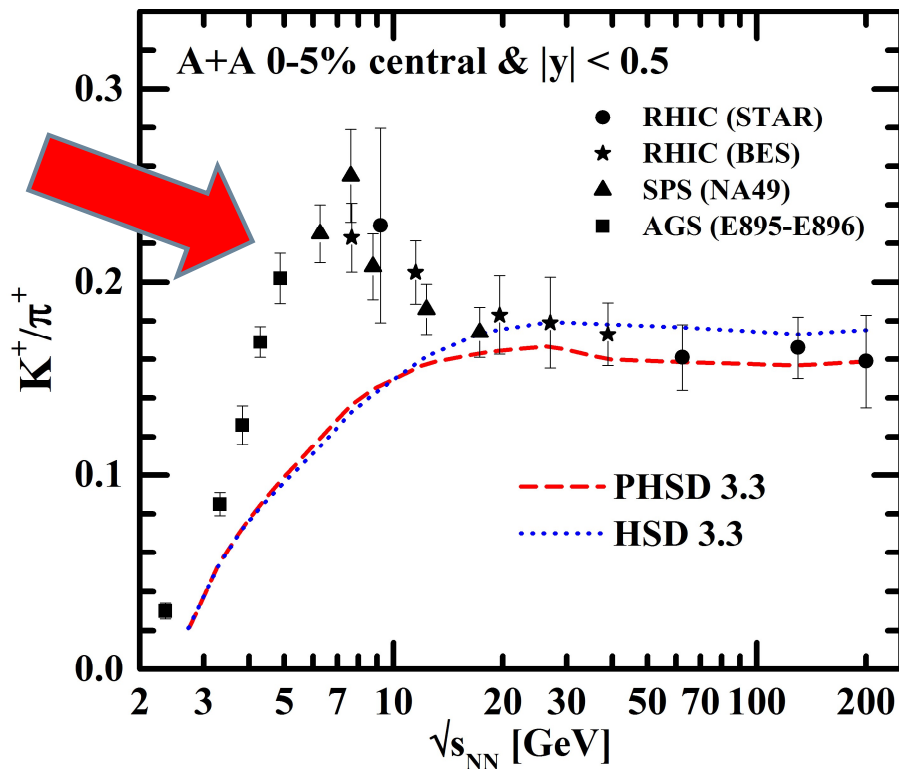
- Strong increase of partonic phase with energy from AGS to RHIC
- SPS: Pb+Pb, 160 A GeV: only about 40% of the converted energy goes to partons; the rest is contained in the large hadronic corona and leading particles
- RHIC: Au+Au, 21.3 A TeV: up to 90% - QGP



# Problem: $K^+/\pi^+$ ,horn' – 2015

**PHSD:** even when considering the creation of a QGP phase, the  $K^+/\pi^+$  ,horn' seen experimentally by NA49 and STAR at a bombarding energy  $\sim 30$  A GeV (FAIR/NICA energies!) remains unexplained !

→ 'Horn' is not traced back to deconfinement ?!



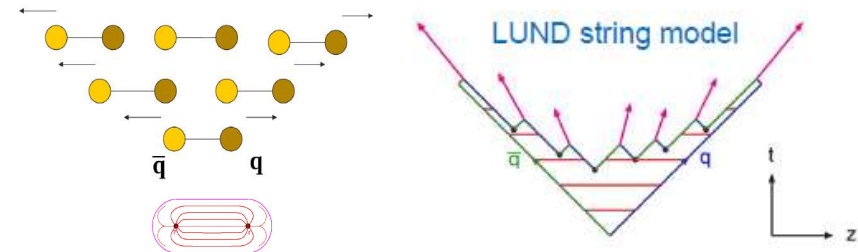
- Can it be related to **chiral symmetry restoration** in the hadronic phase?!



# ,Quark flavor chemistry' in the LUND string model

## □ In PHSD:

the ,flavor chemistry' of the final hadrons is mainly defined by the LUND string model



## □ LUND model:

1) 'quark flavor chemistry' is determined by the Schwinger-formula

According to the Schwinger-formula, the probability to form a massive  $s\bar{s}$  pair in a string-decay is suppressed in comparison to a light flavor pair ( $u\bar{u}, d\bar{d}$ ):

$$\frac{P(s\bar{s})}{P(u\bar{u})} = \frac{P(s\bar{s})}{P(d\bar{d})} = \gamma_s = \exp\left(-\pi \frac{m_s^2 - m_q^2}{2\kappa}\right)$$

with  $\kappa$ - string tension;

in vacuum:  $\kappa \sim 0.9 \text{ GeV/fm} = 0.176 \text{ GeV}^2$

The relative production factors in PHSD/HSD are:

$$u : d : s : uu = \begin{cases} 1 : 1 : 0.3 : 0.07 & \text{at SPS to RHIC;} \\ 1 : 1 : 0.4 : 0.07 & \text{at AGS energies.} \end{cases}$$

$m_s, m_q$  ( $q=u,d$ ) – constituent ('dressed') quark masses due to the coupling to the vacuum

2) 'Kinematics' is determined by the fragmentation function  $f(x, m_T)$

$$f(x, m_T) \approx \frac{1}{x} (1 - x^a) \exp(-bm_T^2/x)$$



# Schwinger mechanism in vacuum

I. In vacuum (e.g. p+p collisions) :

- 'dressing' of bare quark masses is due to the coupling to the vacuum scalar quark condensate ( cf. Dyson-Schwinger Bethe-Salpeter approaches)

$$m_q^V = m_q^0 - g_s \langle q\bar{q} \rangle_V \quad (V \equiv \text{vacuum})$$

$$\text{bare quark masses: } m_u^0 = m_d^0 \approx 7\text{MeV}, m_s^0 \approx 100\text{MeV}$$

- vacuum scalar quark condensate is fixed by Gell-Mann-Oakes-Renner relation:

$$f_\pi^2 m_\pi^2 = -\frac{1}{2}(m_u^0 + m_d^0) \langle \bar{q}q \rangle_V \quad \Rightarrow \quad \langle \bar{q}q \rangle_V \approx -3.2 \text{ fm}^{-3}$$

$f_\pi$  and  $m_\pi$  are the pion decay constant and pion mass

→ Constituent quark masses in vacuum :  $m_q \equiv m_q^V$

$$m_u^V = m_d^V \approx 0.35\text{GeV}, \quad m_s^V \approx 0.5\text{GeV}$$



# Schwinger mechanism in medium

## II. In medium (e.g. A+A collisions) :

- In the presence of **a hot and dense hadronic medium**, the degrees of freedom modify their properties, e.g. **the in-medium constituent quark masses**:

$$m_q^* = m_q^0 - g_s \langle q\bar{q} \rangle \quad \Rightarrow \quad m_q^* = m_q^0 + (m_q^V - m_q^0) \frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V} \quad (q = u, d, s)$$

- **The scalar quark condensate  $\langle q\bar{q} \rangle$**  is viewed as an **order parameter for the restoration of chiral symmetry**:

$$\langle \bar{q}q \rangle = \begin{cases} \neq 0 & \text{chiral non-symmetric phase;} \\ = 0 & \text{chiral symmetric phase.} \end{cases}$$

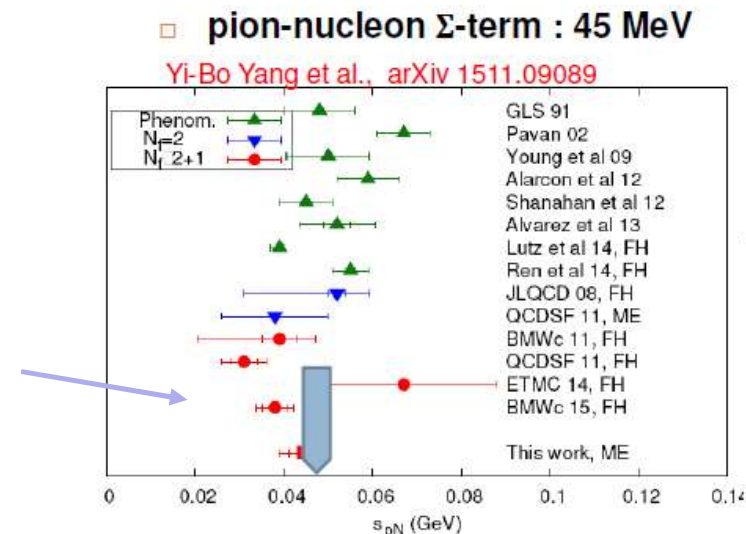
- The behavior of the scalar quark condensate  $\langle q\bar{q} \rangle$  in the **hadronic medium (baryons + mesons)** can be obtained e.g. from **non-linear  $\sigma - \omega$  model**:

$$\frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V} = 1 - \frac{\Sigma_\pi}{f_\pi^2 m_\pi^2} \rho_S - \sum_h \frac{\sigma_h \rho_S^h}{f_\pi^2 m_\pi^2}$$

baryonic medium
mesonic medium

B. Friman et al., Eur. Phys. J. A 3, 165, 1998

where  $\rho_s$  is the **scalar nuclear density**,  
 $\rho_s^h$  is the **scalar meson density**,  
 $\Sigma_\pi \approx 45$  MeV is the **pion-nucleon  $\Sigma$ -term**,  
 $\sigma_h = m_\pi/2$  for light mesons;  $=m_\pi/4$  - strange mesons





# Scalar density in PHSD

1)  $\rho_s$  is the **scalar density of baryonic matter**:

$d = 4$  in case of isospin symmetric nuclear matter

$$\rho_s = d \int \frac{d^3 p}{(2\pi)^3} \frac{m_N^*(x)}{\sqrt{p^2 + m_N^{*2}}} f_N(x, \mathbf{p})$$

where the **in-medium nucleon mass** is

$$m_N^*(x) = m_N^V - g_s \sigma(x)$$

with  $m_N^V$  denoting **the nucleon mass in vacuum**

**Scalar field  $\sigma(x)$**  mediates the scalar interaction with the surrounding medium with a  $g_s$  coupling

$\sigma(x)$  is defined/determined locally by the **nonlinear gap equation**:

$$m_\sigma^2 \sigma(x) + B \sigma^2(x) + C \sigma^3(x) = g_s \rho_s = g_s d \int \frac{d^3 p}{(2\pi)^3} \frac{m_N^*(x)}{\sqrt{p^2 + m_N^{*2}}} f_N(x, \mathbf{p})$$

Within the **non-linear  $\sigma - \omega$  model** for nuclear matter, the **parameters  $g_s$ ,  $m_\sigma$ , B, C** can be **fixed** in order to reproduce the main nuclear matter quantities at **saturation**, i.e. saturation density, binding energy per nucleon, compression modulus and the effective nucleon mass.

2)  $\rho_s^h$  is the **scalar density of mesons** of type h (from PHSD):

$$\rho_s^h(x) = \frac{(2s+1)(2t+1)}{(2\pi)^3} \int d^3 \mathbf{p} \frac{m_h}{\sqrt{p^2 + m_h^2}} f_h(x, \mathbf{p})$$

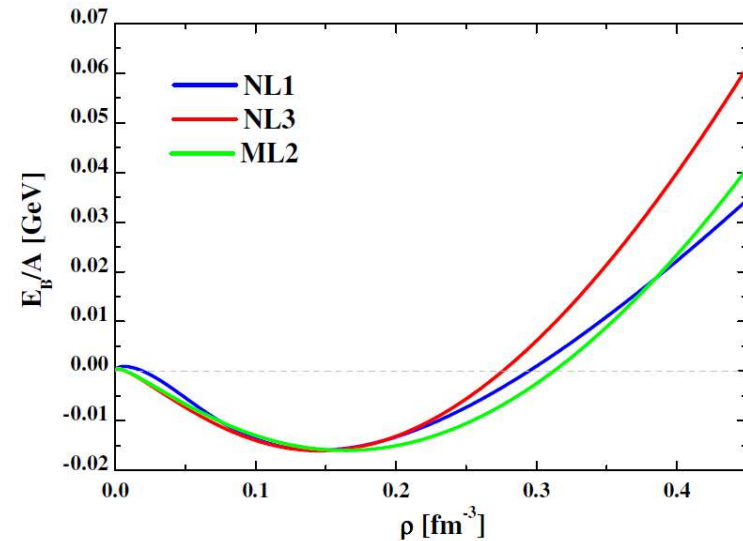




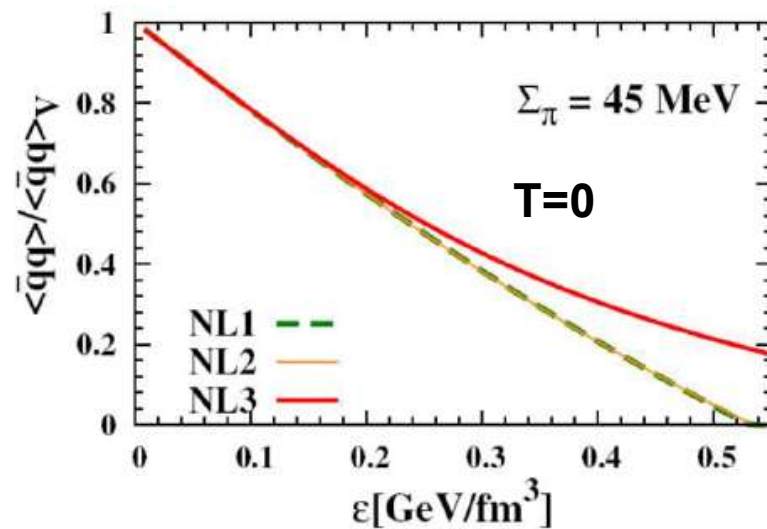
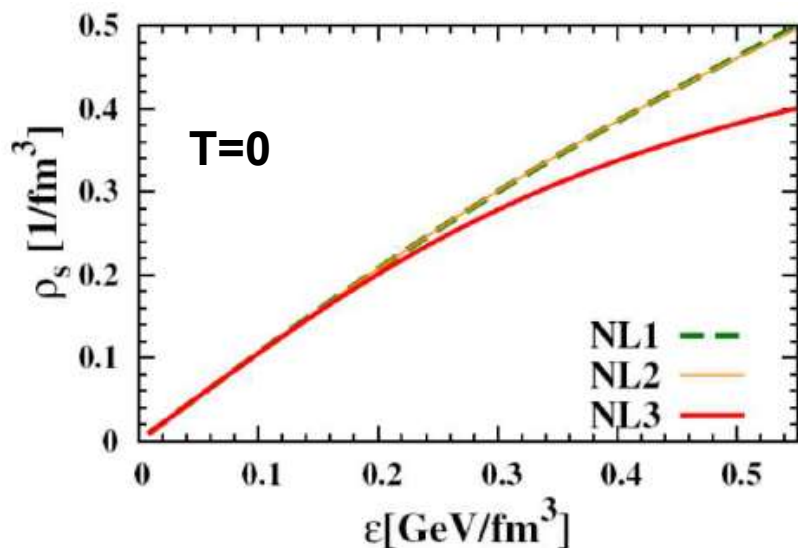
# Sensitivity to the EoS of nuclear matter

Parameter sets NL1, NL3 and ML2 for the **nonlinear  $\sigma - \omega$  model** employed in the transport calculations

	NL1	ML2	NL3
$g_s$	6.91	9.28	9.50
$g_v$	7.54	10.59	10.95
$B$ (1/fm)	-40.6	5.1	1.589
$C$	384.4	9.8	34.23
$m_s$ (1/fm)	2.79	2.79	2.79
$m_v$ (1/fm)	3.97	3.97	3.97
$K$ (MeV)	380	354	380
$m^*/m$	0.83	0.68	0.70



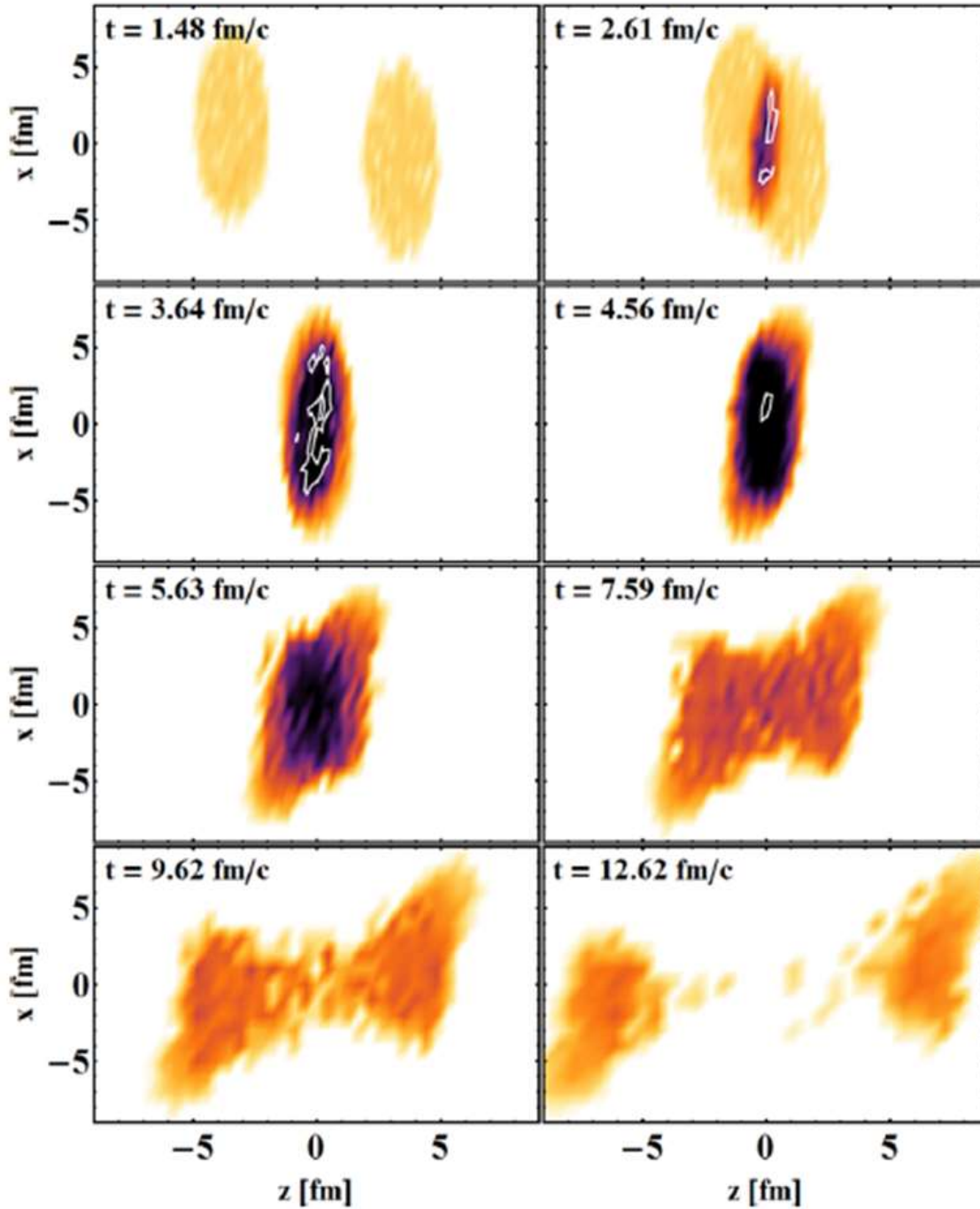
NL1,NL3: A. Lang *et al.*, Z. Phys. A 340, 287 (1991)  
 ML2: F. de Jong and R. Malfliet, Phys. Rev. C 44, 998 (1991).



$\epsilon$  is the energy density of nuclear matter

**→ low sensitivity to the nuclear EoS**

PHSD: Au+Au @ 30 AGeV, b = 2.2 fm



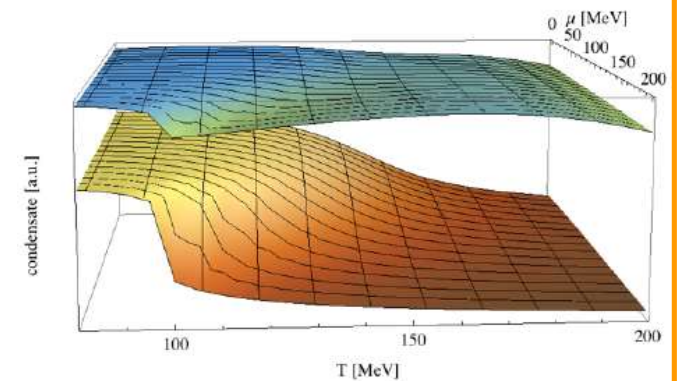
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Ratio of the **scalar quark condensate** compared to the **vacuum** as a function of time:

$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$

Cf. Chistian Fischer:



W. Cassing, A. Palmese, P. Moreau, E.L. Bratkovskaya, PRC 93, 014902 (2016), arXiv:1510.04120



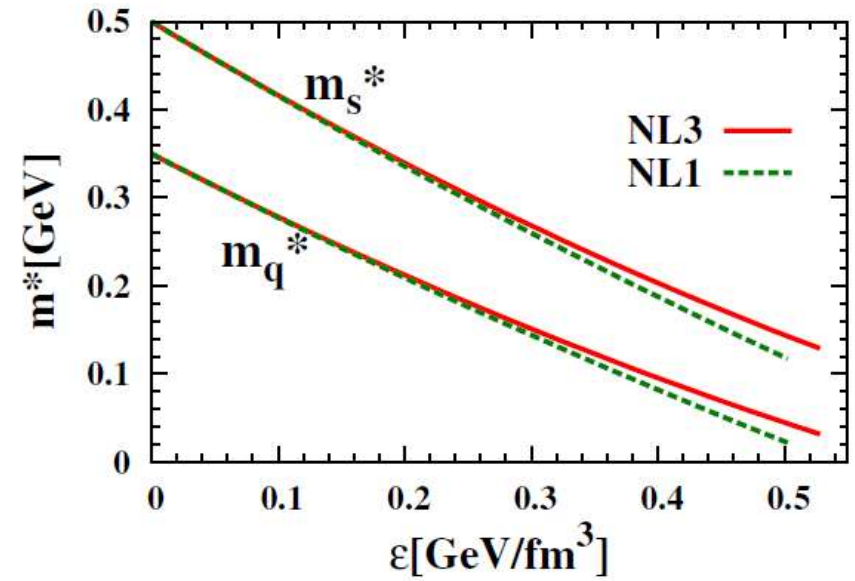
# Modeling of the chiral symmetry restoration in PHSD

- In the **Schwinger formula** the **in-medium constituent masses**  $m_{q;s}^*$  (instead of vacuum  $m_{q;s}$ ) have to be considered:

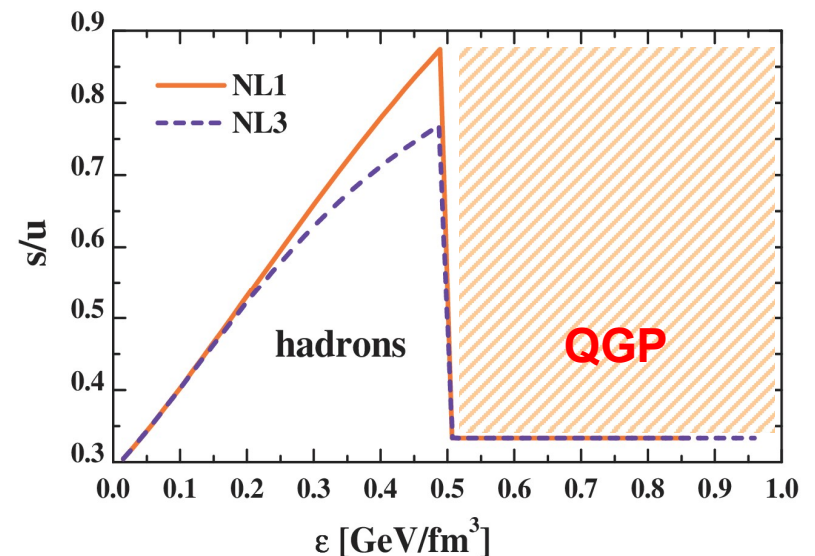
$$\frac{P(s\bar{s})}{P(u\bar{u})} = \frac{P(s\bar{s})}{P(d\bar{d})} = \gamma_s = \exp\left(-\pi \frac{m_s^{*2} - m_q^{*2}}{2\kappa}\right)$$

- As a consequence of the **chiral symmetry restoration (CSR)**, the **strangeness production probability increases** with the local energy density  $\varepsilon$ .

- In the **QGP** phase, the string decay doesn't occur anymore and this effect is therefore suppressed.

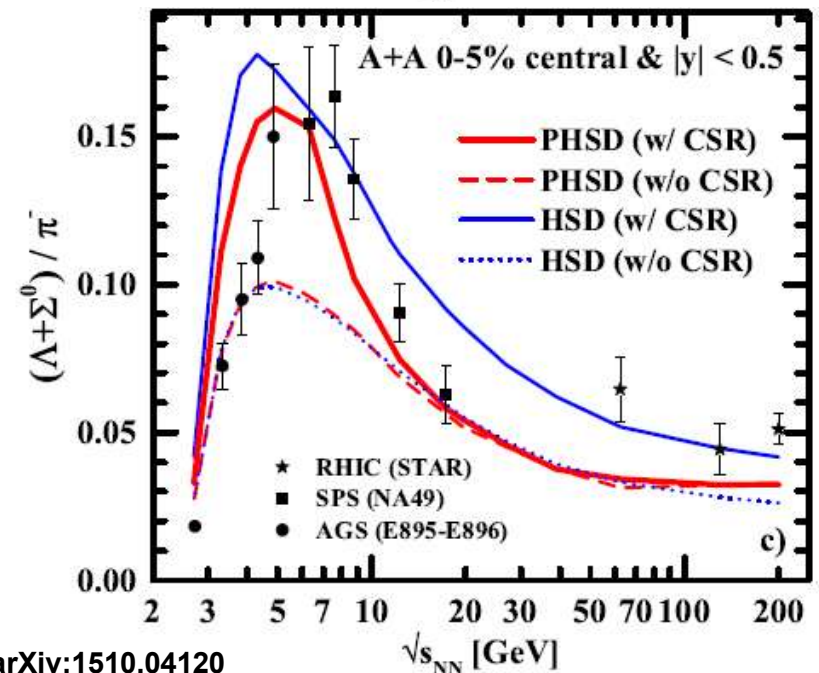
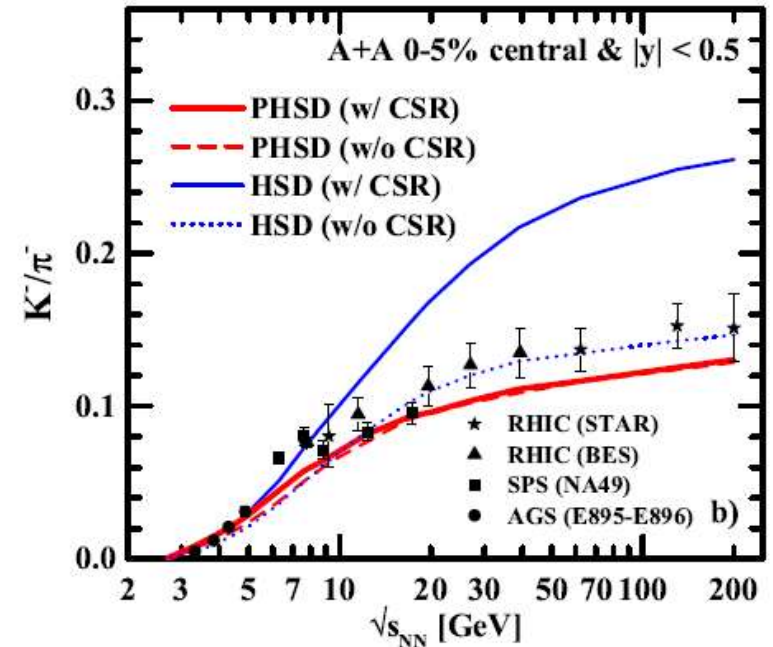
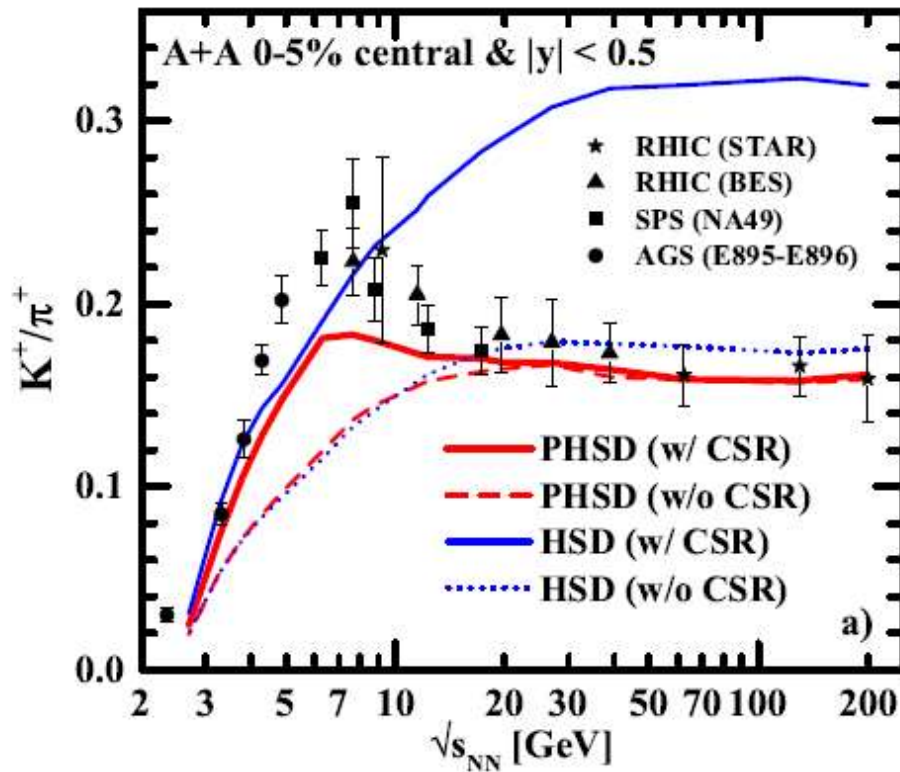


The strangeness ratio  $s/u$  in the string decay





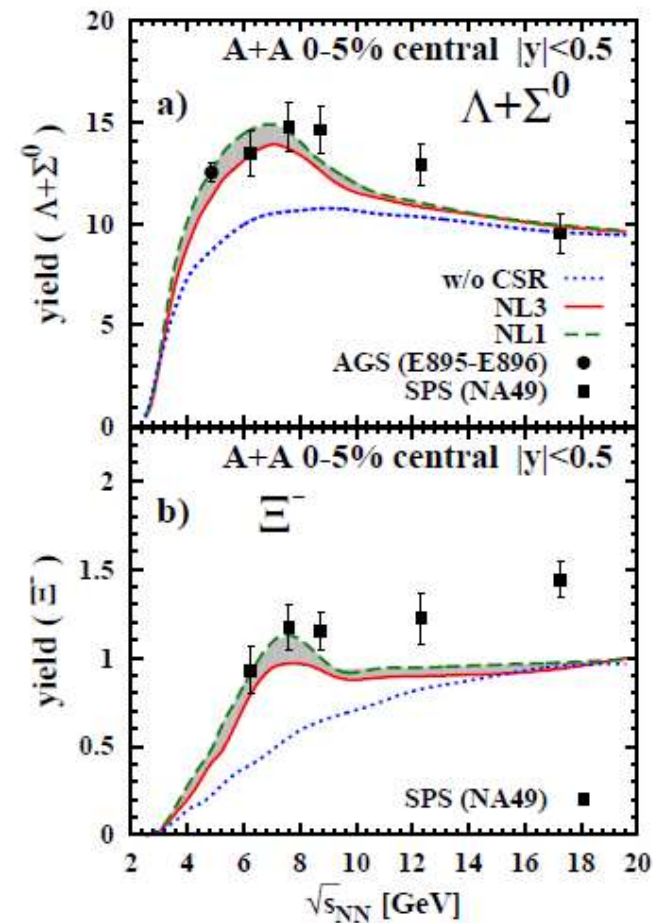
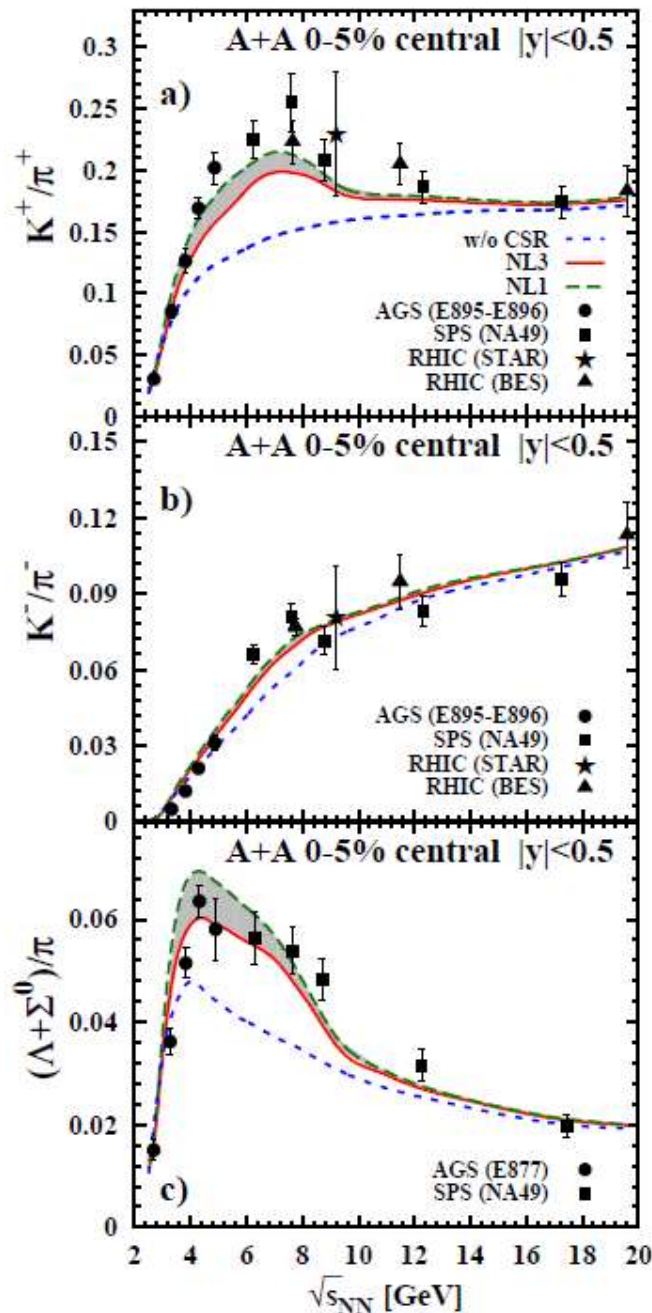
# PHSD results with chiral symmetry restoration



→ The **strangeness enhancement** seen experimentally at FAIR/NICA energies probably involves the approximate **restoration of chiral symmetry in the hadronic phase**



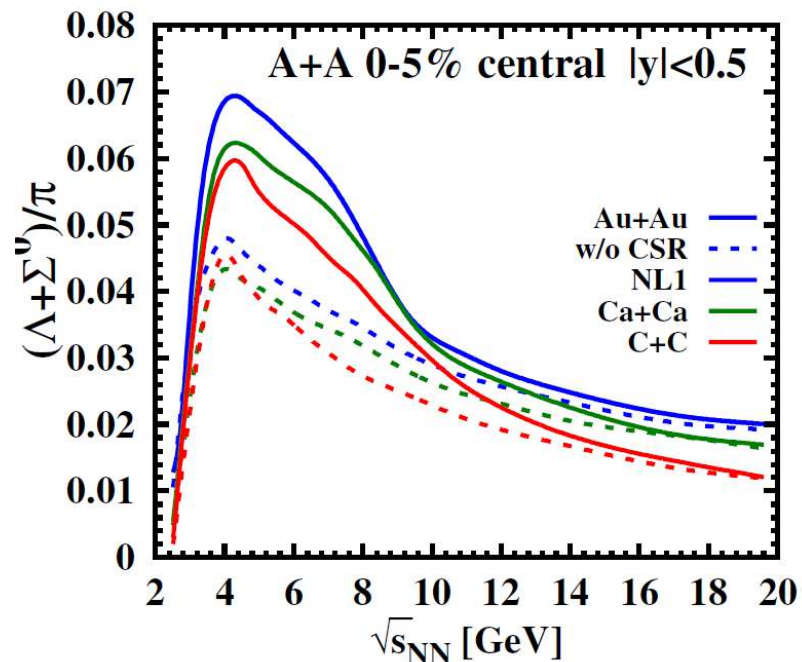
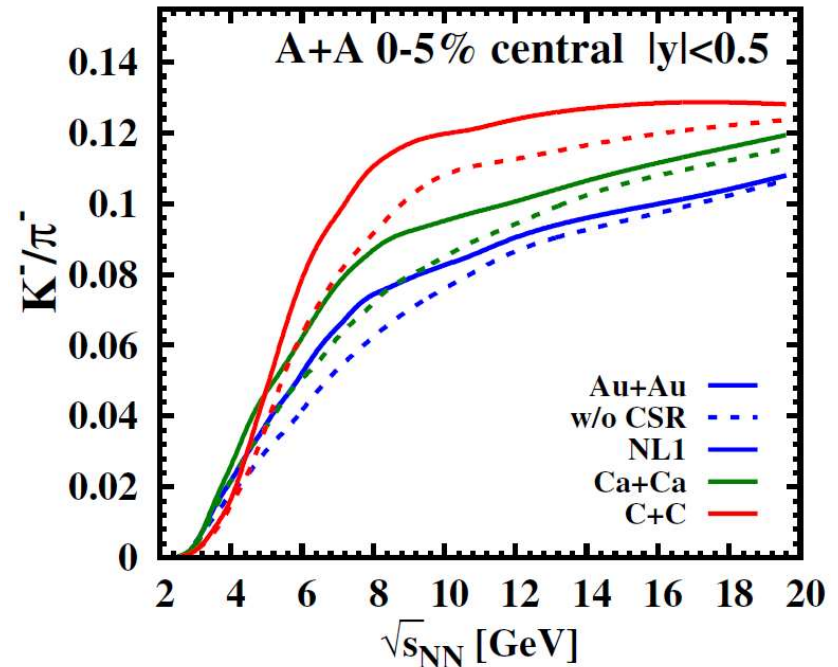
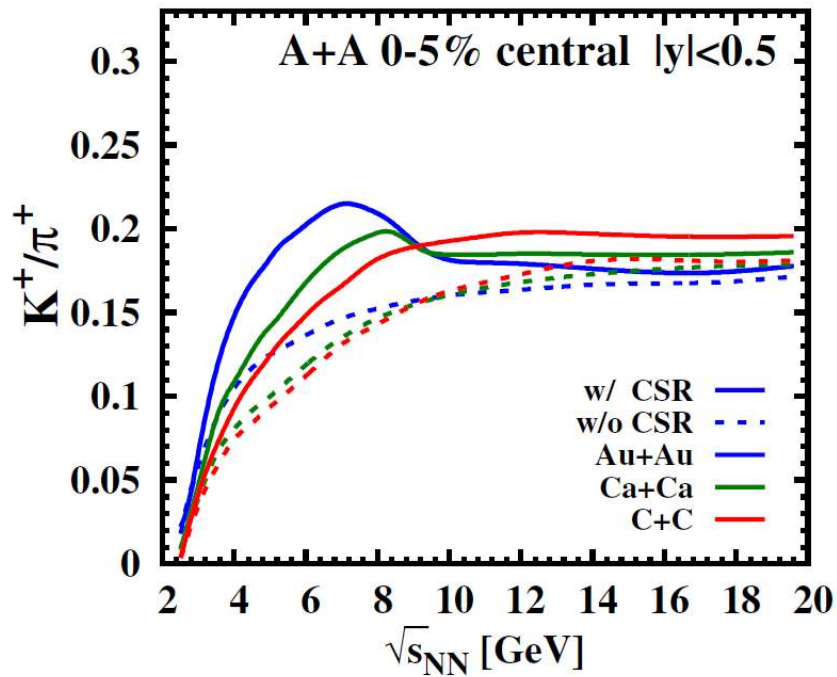
# Excitation function of hadron ratios and yields



- Influence of EoS: NL1 vs NL3 → **low sensitivity to the nuclear EoS**
- Excitation function of the **hyperons**  $\Lambda + \Sigma^0$  and  $\Xi^-$  show analogous peak as  $K^+/\pi^+$ ,  $(\Lambda + \Sigma^0)/\pi$  ratios due to CSR



# Sensitivity to the system size: A+A collisions



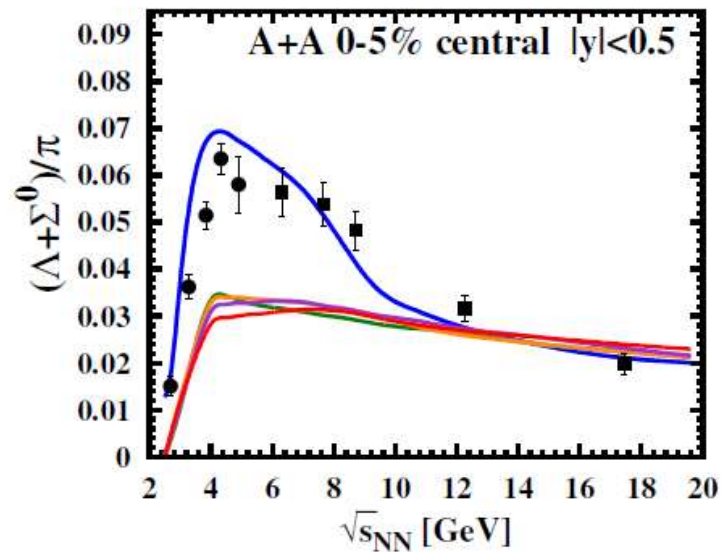
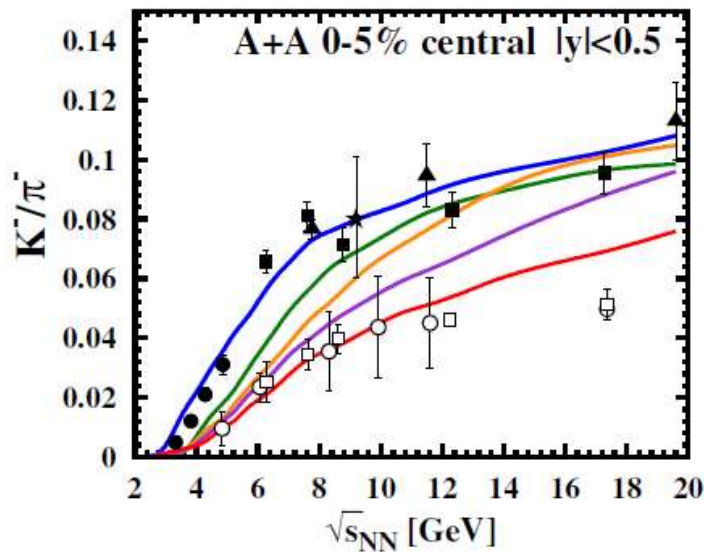
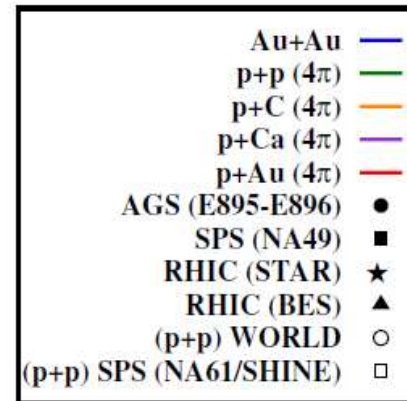
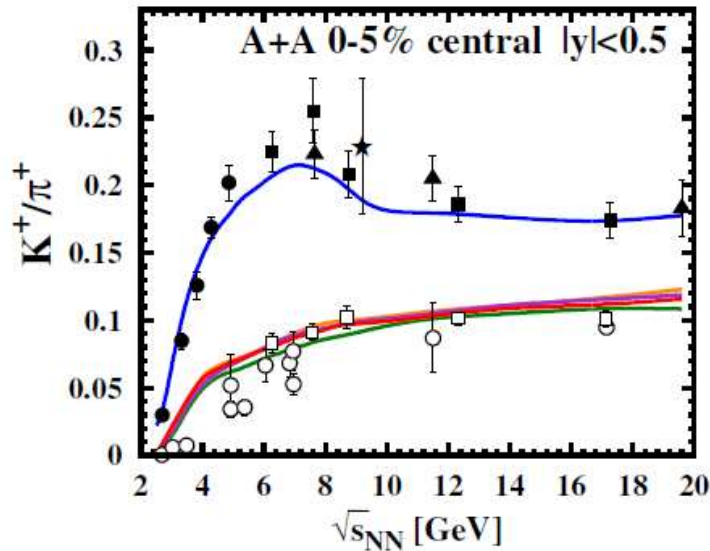
If the **system size is smaller**:

- the peak of  $K^+/\pi^+$  **disappears**
- the peak of  $(\Lambda+\Sigma^0)/\pi$  **remains** in the same position in energy



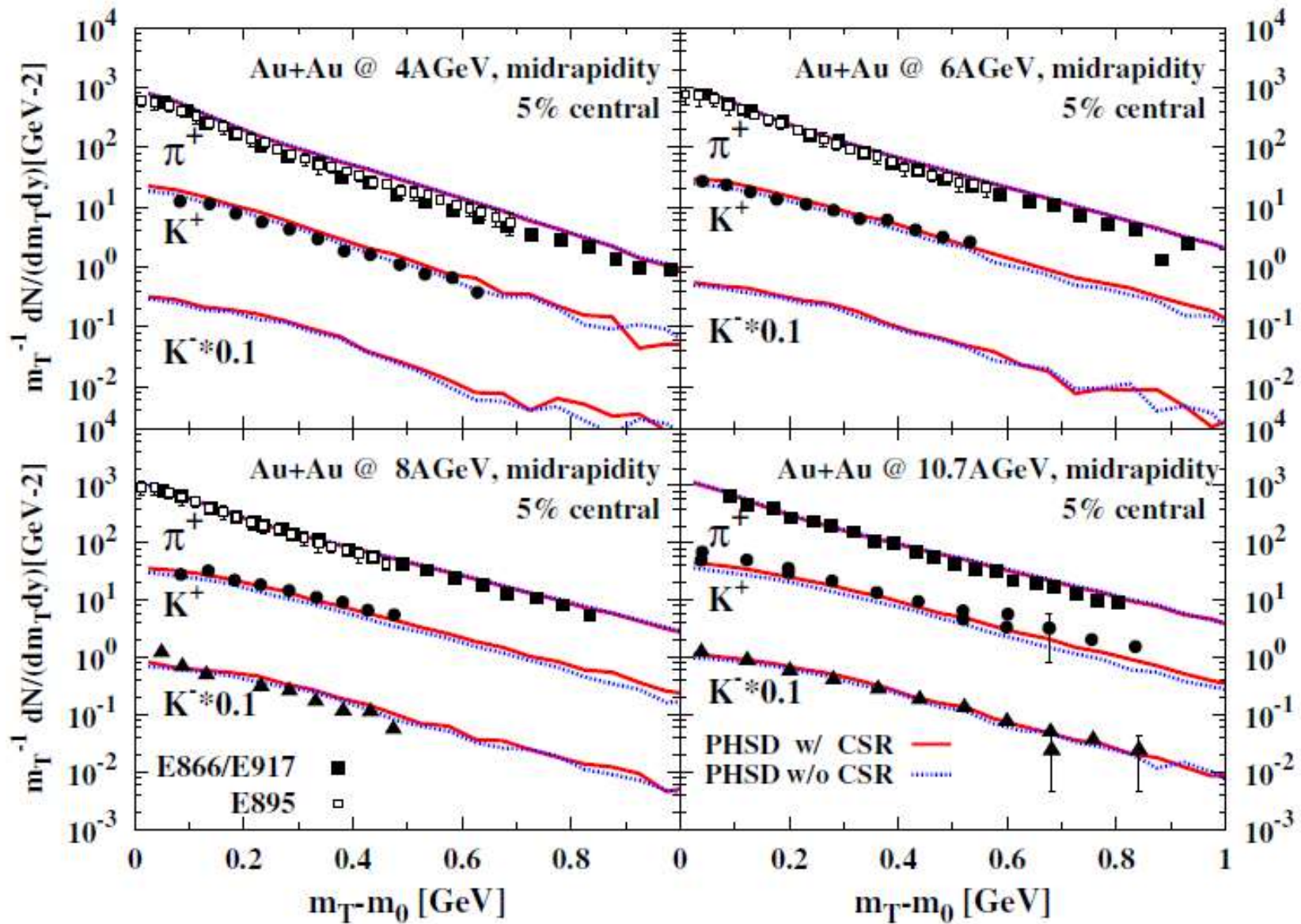
# Sensitivity to the system size: p+A collisions

□ In p+A collisions strange to non-strange particle ratios show **no peaks**





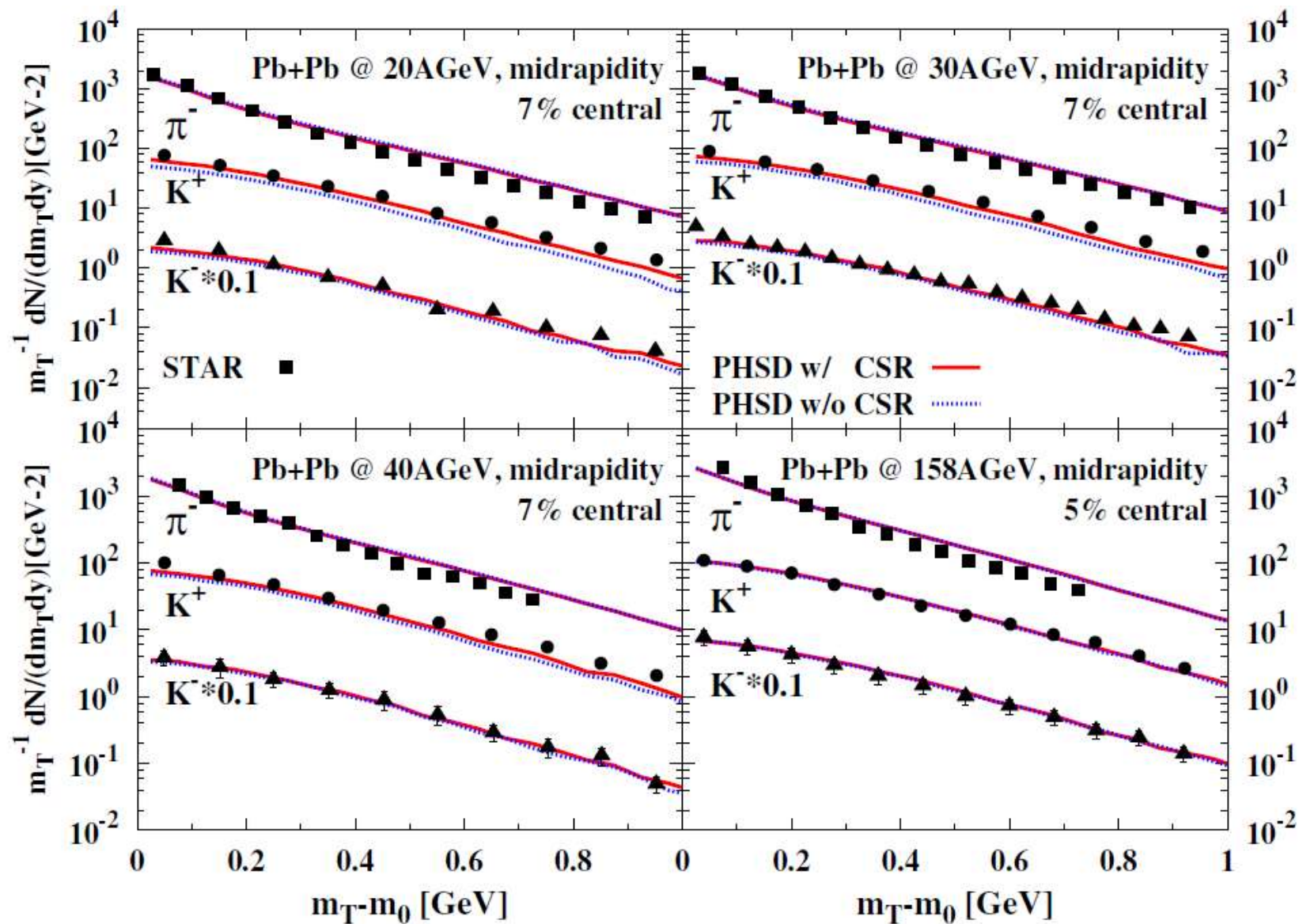
# $m_T$ spectra of pions and $K^{+/-}$ at AGS energies







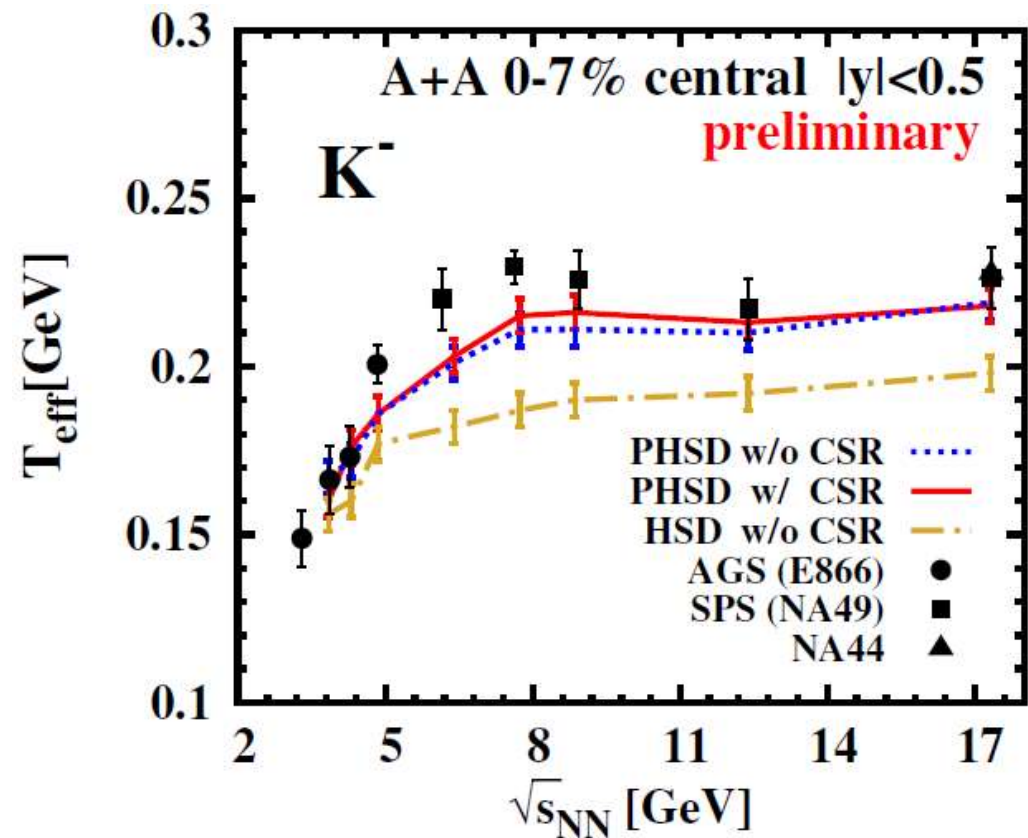
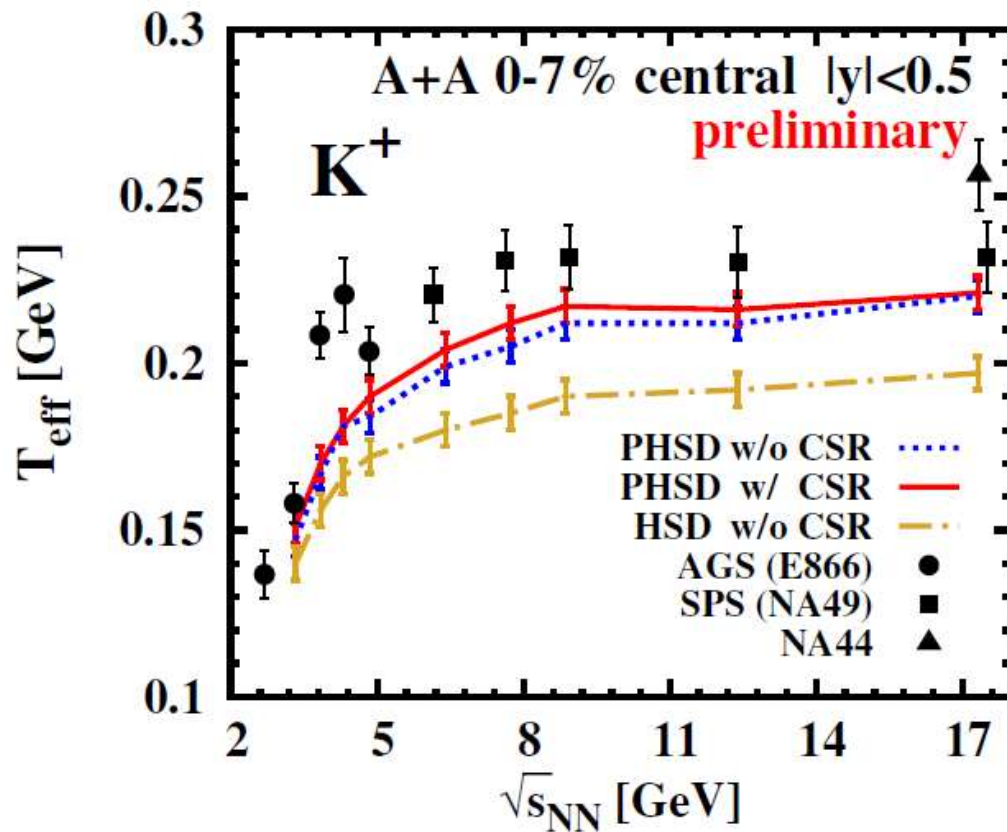
# $m_T$ spectra of pions and $K^{+/-}$ at SPS energies





# Excitation function of $T_{\text{eff}}$

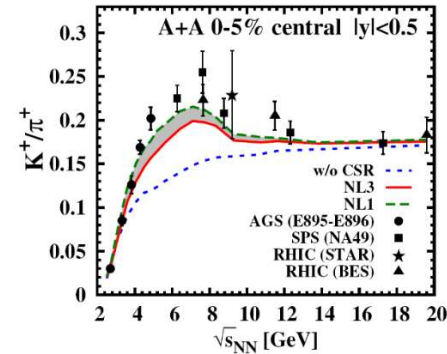
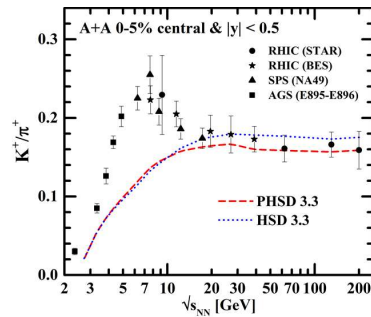
Alessia Palmese



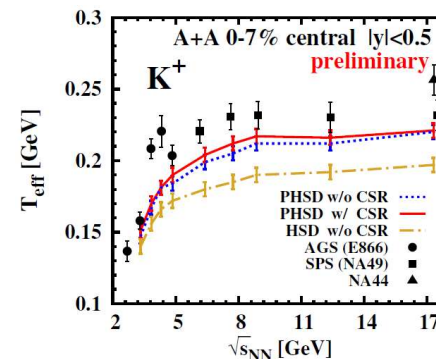
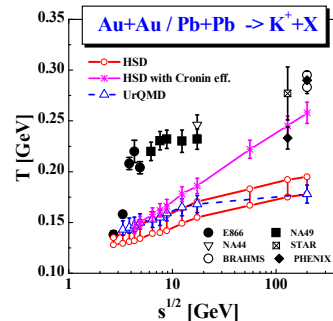
→ Increase of slope  $T_{\text{eff}}$  due to the QGP

→ Small effect of chiral symmetry restoration on slope  $T_{\text{eff}}$

# Summary

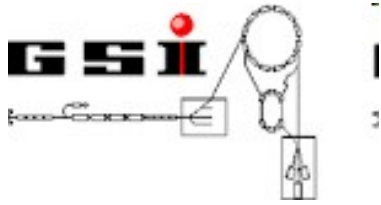


- ❑ The **strangeness ‘enhancement’ (‘horn’)** seen experimentally by NA49 and STAR at a bombarding energy  $\sim 20\text{-}30$  A GeV (FAIR/NICA energies!) cannot be attributed to deconfinement
- ❑ Including essential aspects of **chiral symmetry restoration** in the hadronic phase, we observe a **rise in the  $K^+/\pi^+$  ratio** at low  $\sqrt{s_{NN}}$  and then a **drop** due to the appearance of a deconfined partonic medium  $\rightarrow$  a **‘horn’** emerges
- ❑ **Hardening of  $m_T$  spectra** due to the **QGP**



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# PHSD group



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# DAAD