

Holography near T_c

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Holographically emulating deconfinement as disappearance
of hadron states

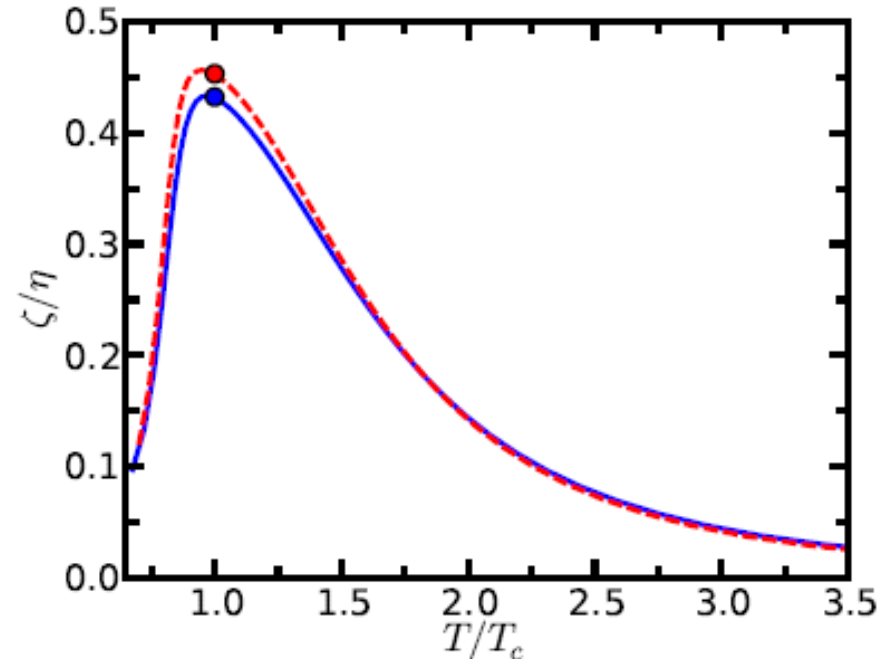
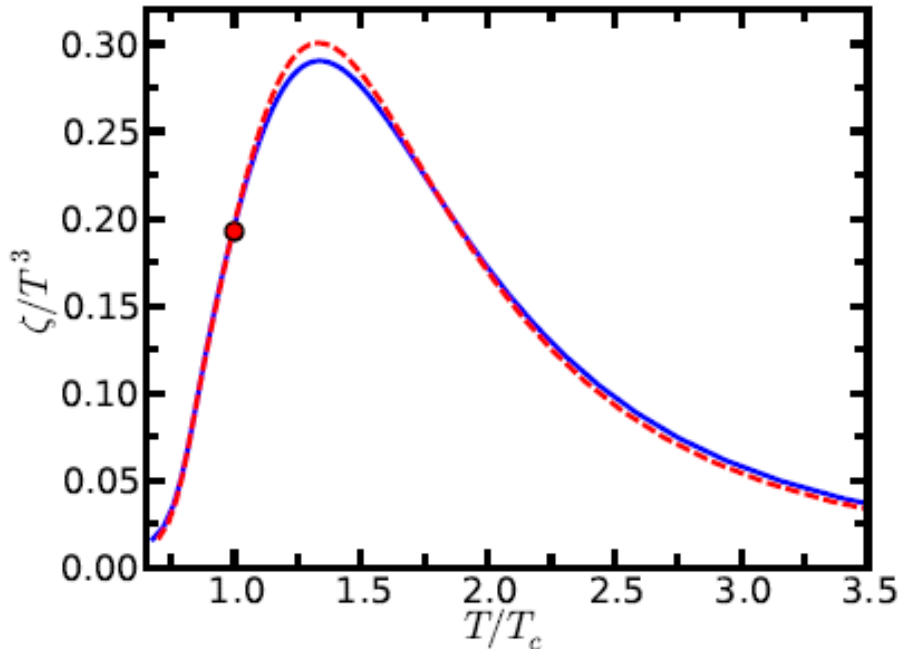
R. Zollner, BK, Phys. Rev. C (2016), CPOD (2016) procs.

Holographic view on the phase diagram

R. Yaresko, J. Knaute, BK, EPJC (2015), PLB (2015)



Holographic Viscosities for NeD



$$S = \frac{1}{2\kappa_5^2} \int d^5x \sqrt{-g} \left[R - \frac{1}{2}(\partial\phi)^2 - V(\phi) \right]$$

Eling-Oz formula [18]

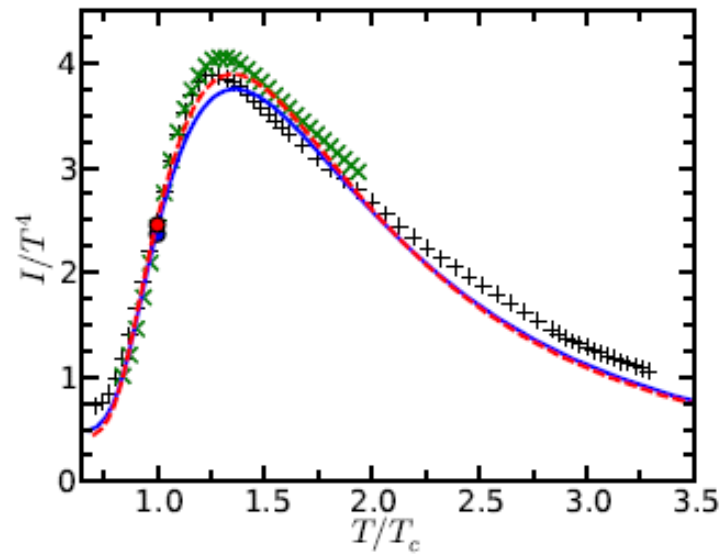
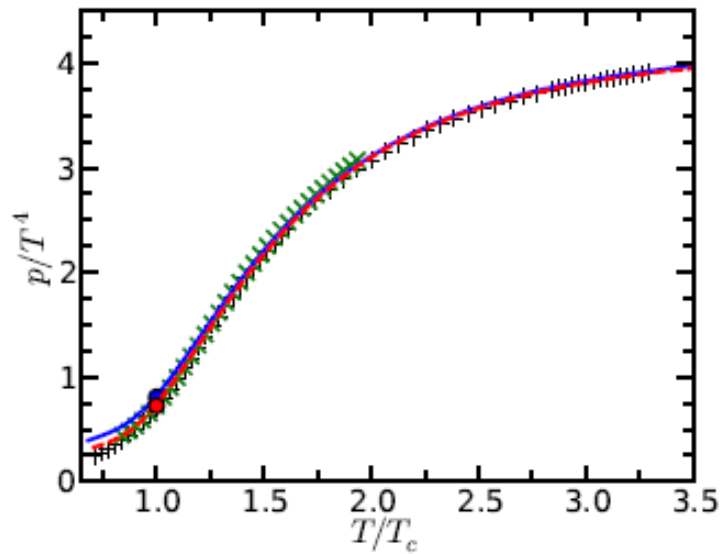
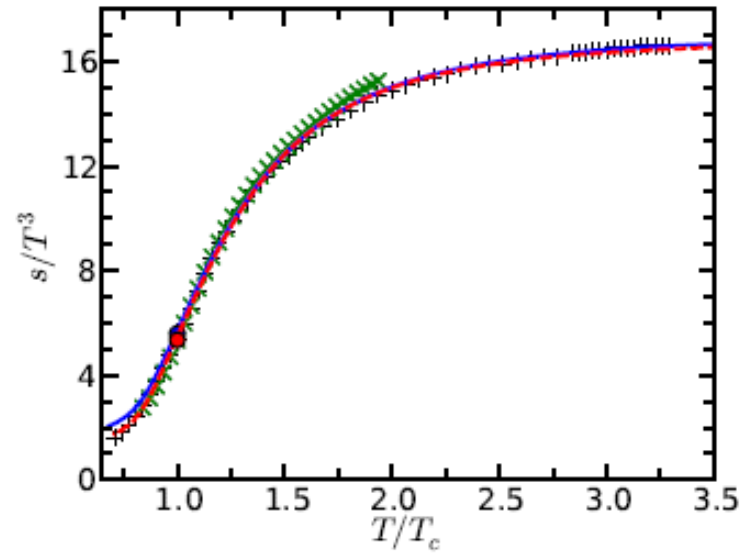
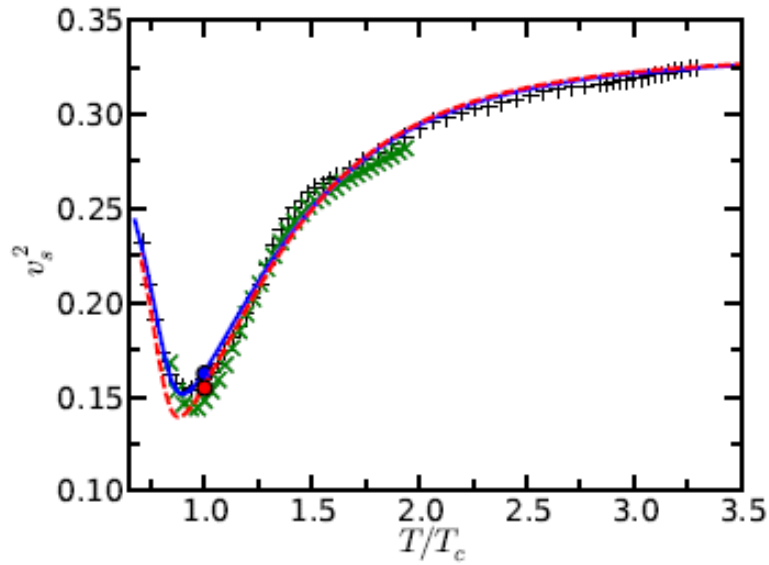
$$\left. \frac{\zeta}{\eta} \right|_{\phi_H} = \left(\frac{d \log s}{d\phi_H} \right)^{-2} = \left(\frac{1}{v_s^2} \frac{d \log T}{d\phi_H} \right)^{-2},$$



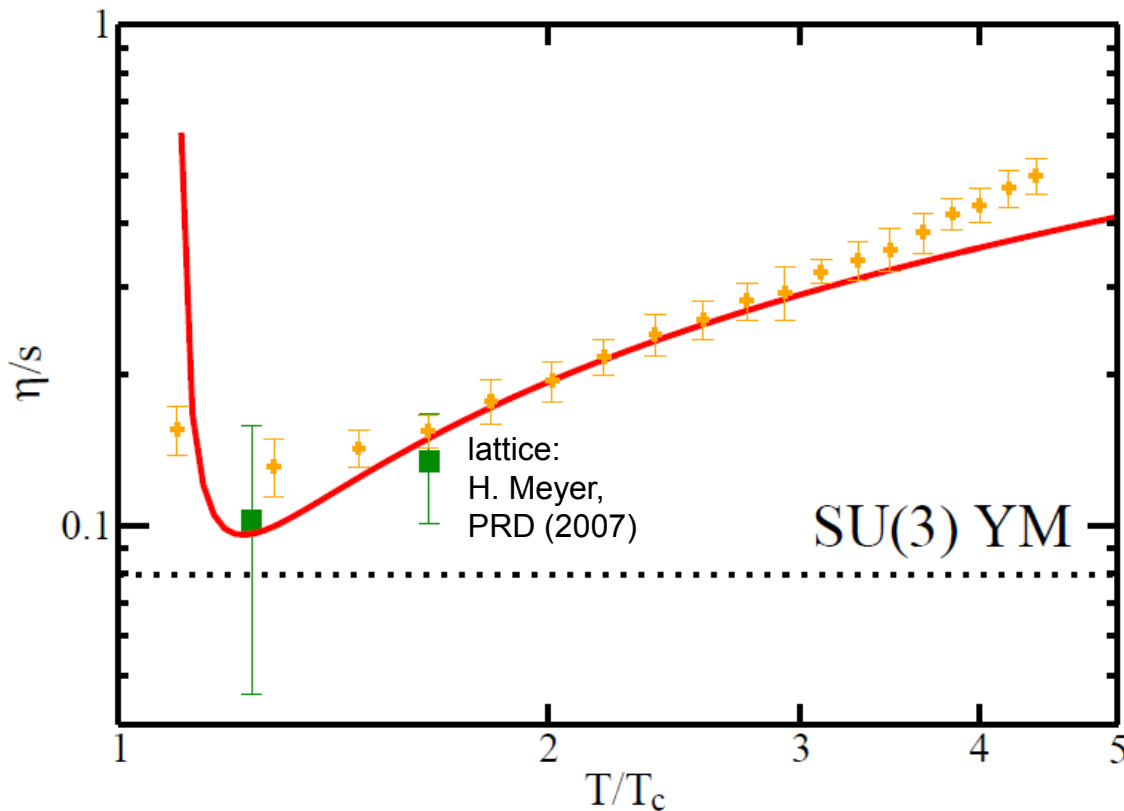
adjusted to QCD

QCD input: $N_f = 2+1$, phys. q masses

Bazazov et al (2014), Borzanyi et al (2014), $T_c = 150$ MeV



Einstein-Hilbert action $\rightarrow \frac{\eta}{s} = 1/4\pi$

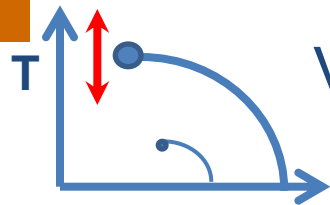


funct. methods:
Christiansen, Pawłowski, Strodthoff,
PRL (2015)

QPM:
M. Bluhm et al., PRC (2011), PLB (2012)

holography:
Kovtun, Starinets, Son, PRL (2015)

adding Gauss-Bonnet terms \rightarrow T dependence



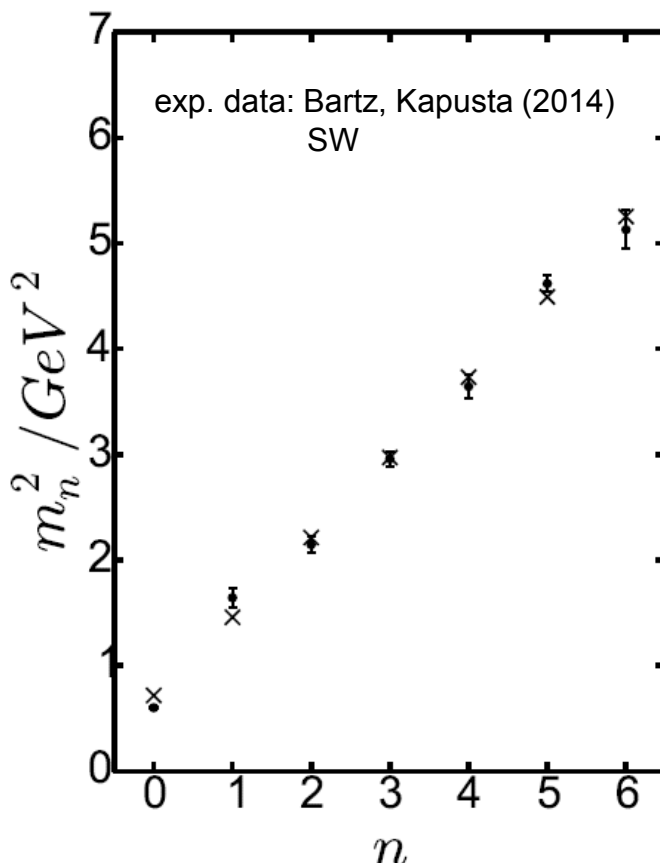
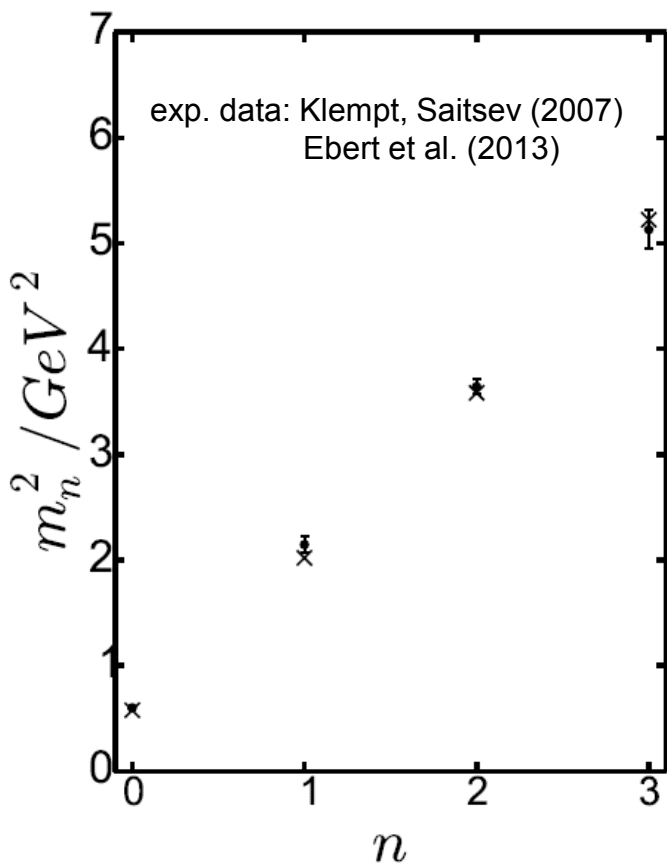
Vector mesons in AdS/CFT – extended soft wall model

5D gravity conf. symmetry breaker sourced by $\bar{q}\gamma^\mu q$

$S_V = F(\text{warp factor, blackening function, } \text{dilaton, } V \text{ wave function})$

soft wall (probe limit): $A(z) = \ln(L/z)^2$ $f(z) = 1 - (z/H)^4$ $\Phi(z) = (cz)^2$

EoM of $V \rightarrow$ Schrödinger eq. in tortoise coordinate, $T = 0 \rightarrow$ Regge type spectrum



rho trajectory
from mod. SW:
 $\tilde{A}, \tilde{f}, \tilde{\phi}$

SW & theor. reasoning:
Karch, Katz, Son, Stephanov
PRD (2006)

A black brane in AdS

(analog to Schwarzschild Black Hole in Friedmann universe)

a patch of the AdS:




AdS with black brane



AdS/CFT dictionary: $T(z_H)$ as Hawking temperature of boundary theory
 $s(z_H)$ as Bekenstein-Hawking entropy

warning: Hawking-Page transition at $T < T_c$

action:
$$S_V = -\frac{1}{4k_V} \int dz d^4x \sqrt{g} e^{-\Phi(z)} F^2$$

 rad. & Lorenz gauge
 $V_\mu = \epsilon_\mu \varphi(z) \exp\{ip_\nu x^\nu\}$

ansatz:
$$ds^2 = e^{A(z)} \left(f(z) dt^2 - d\vec{x}^2 - \frac{1}{f(z)} dz^2 \right)$$

EoM:
$$\left(\partial_\xi^2 - (U_T - m_n^2) \right) \psi = 0,$$



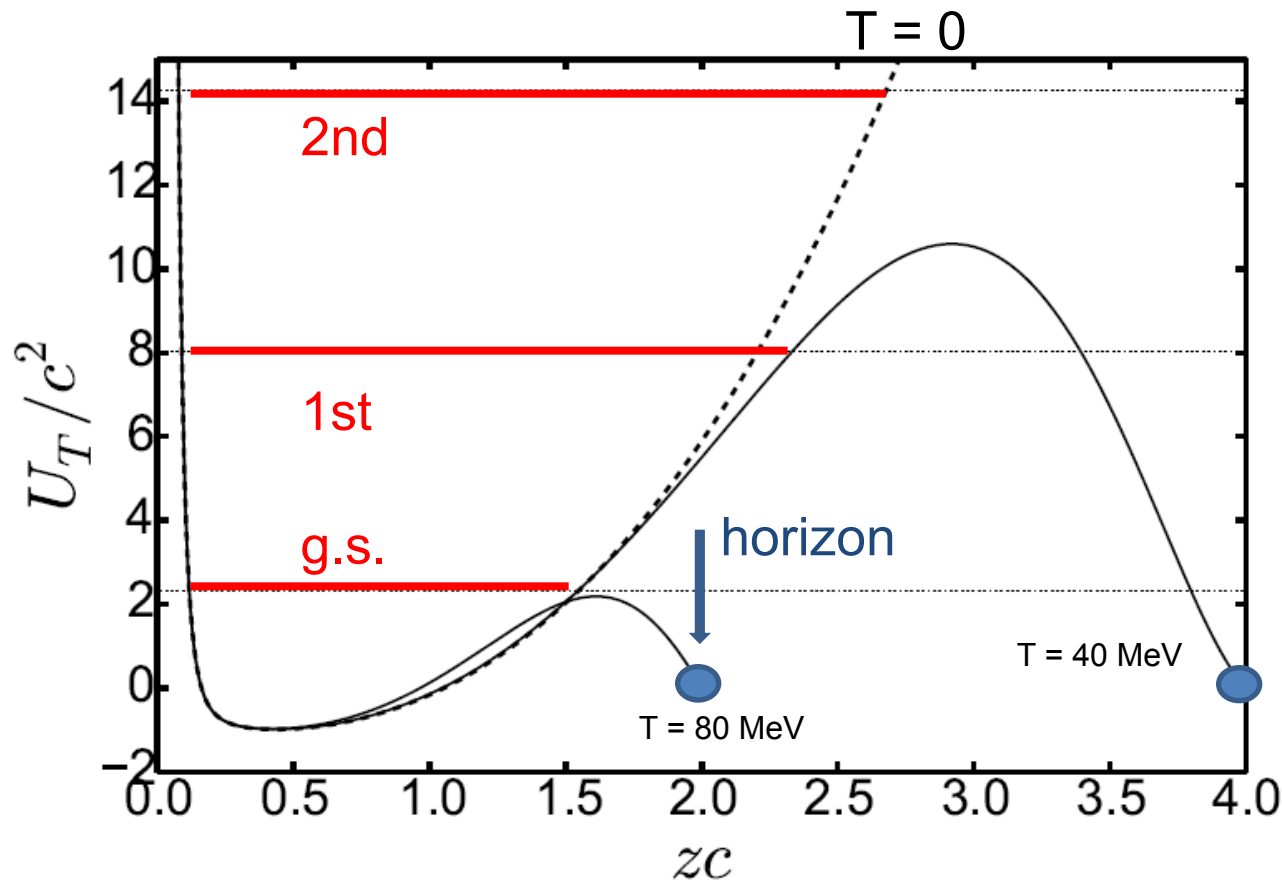
$$U_T = \left(\frac{1}{2} \left(\frac{1}{2} \partial_z^2 A - \partial_z^2 \Phi \right) + \frac{1}{4} \left(\frac{1}{2} \partial_z A - \partial_z \Phi \right)^2 \right) f^2 + \frac{1}{4} \left(\frac{1}{2} \partial_z A - \partial_z \Phi \right) \partial_z f^2.$$

spirit of soft-wall model: ansatz for A, f, phi

vector mesons = normalizable modes

Schrödinger equivalent potential

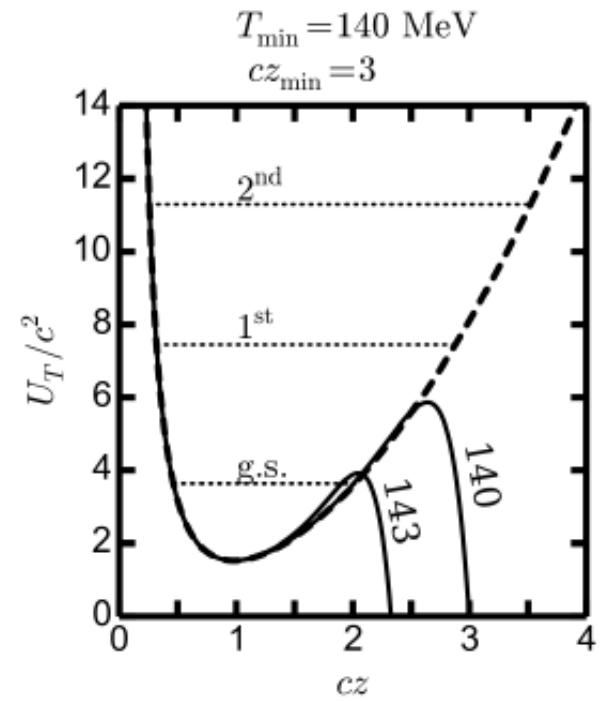
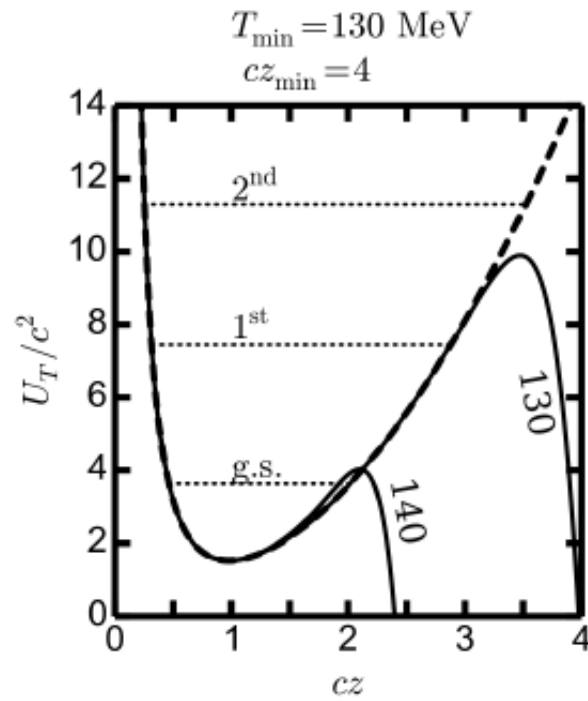
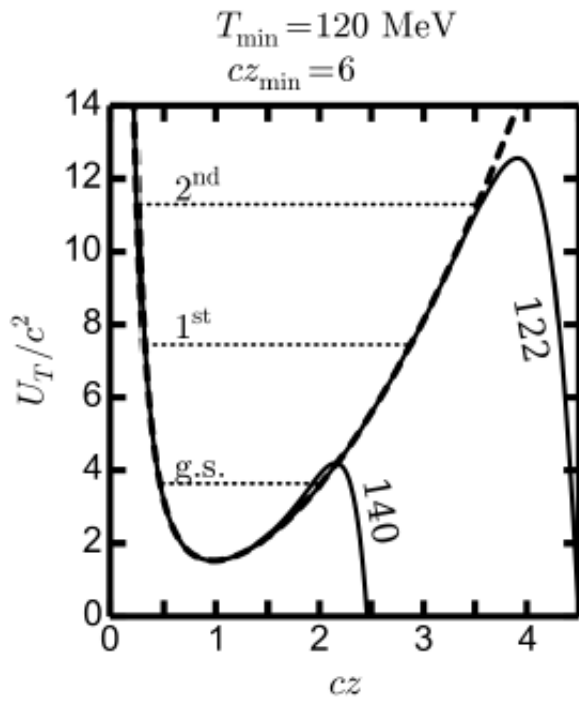
for modes in Klein-Kaluza decomposition of V in axial gauge

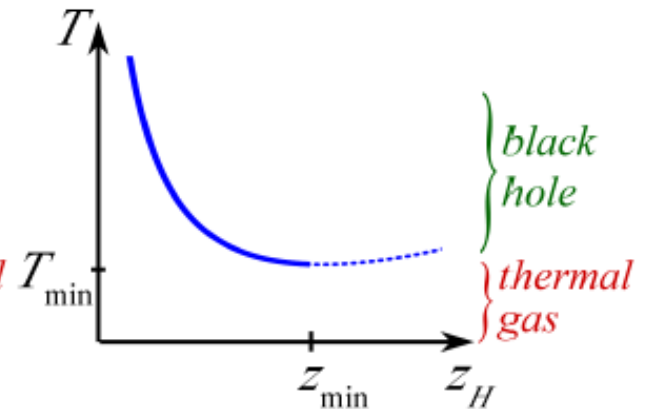
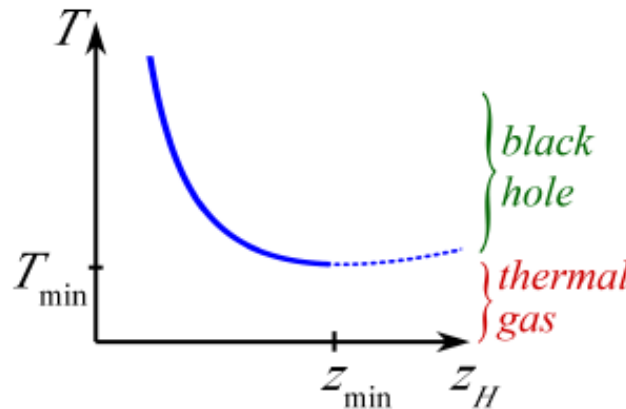
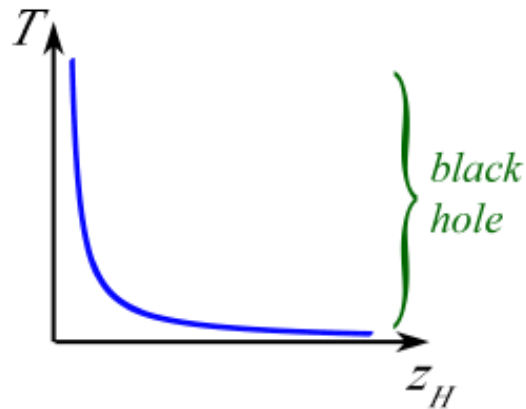
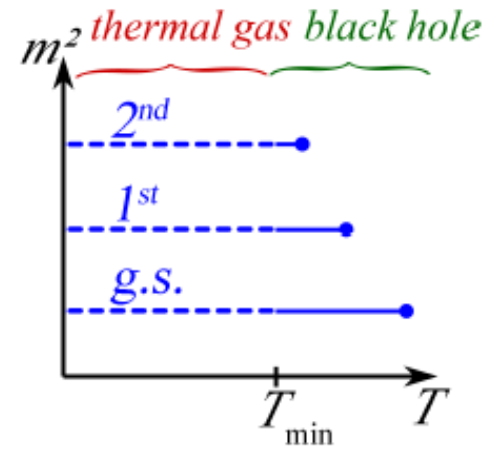
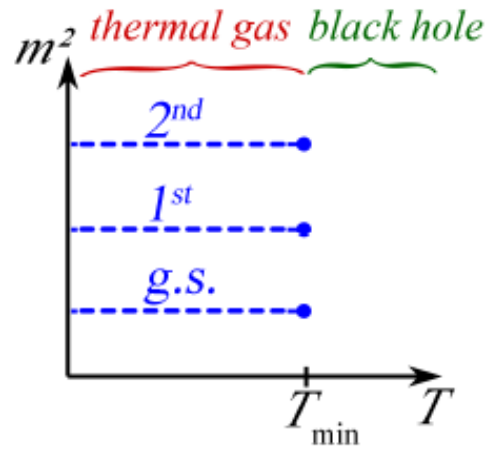
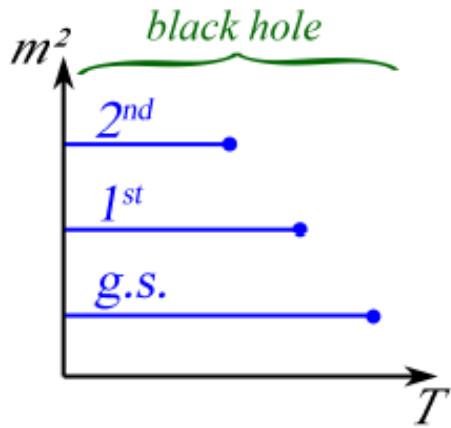


SW($T > 0$):
Colangelo, Giannuzzi,
Nicotri, JHEP (2012)

$H \rightarrow T(H)$
needs
fine tuning

sequential disappearance upon temperature increase





sequential vs. instantan. vs. mixed sequential disappearance

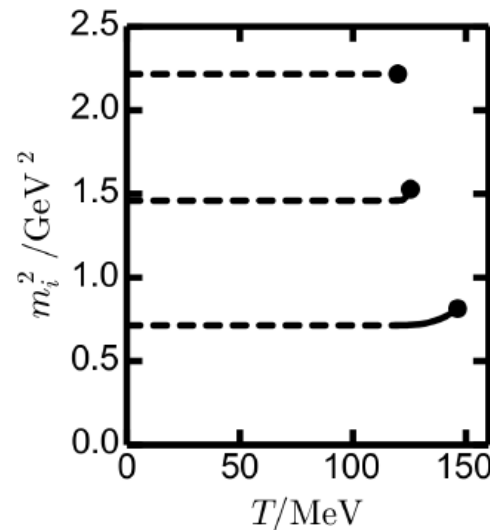
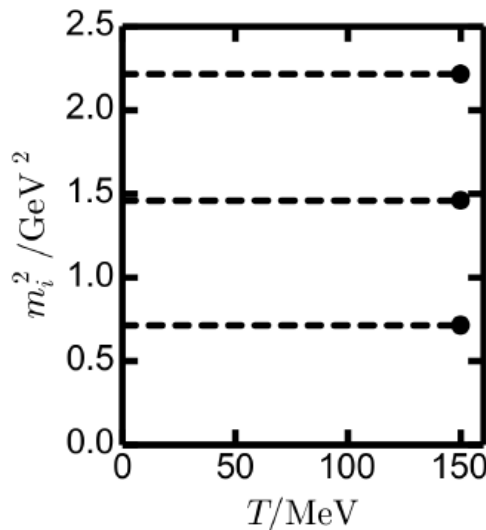
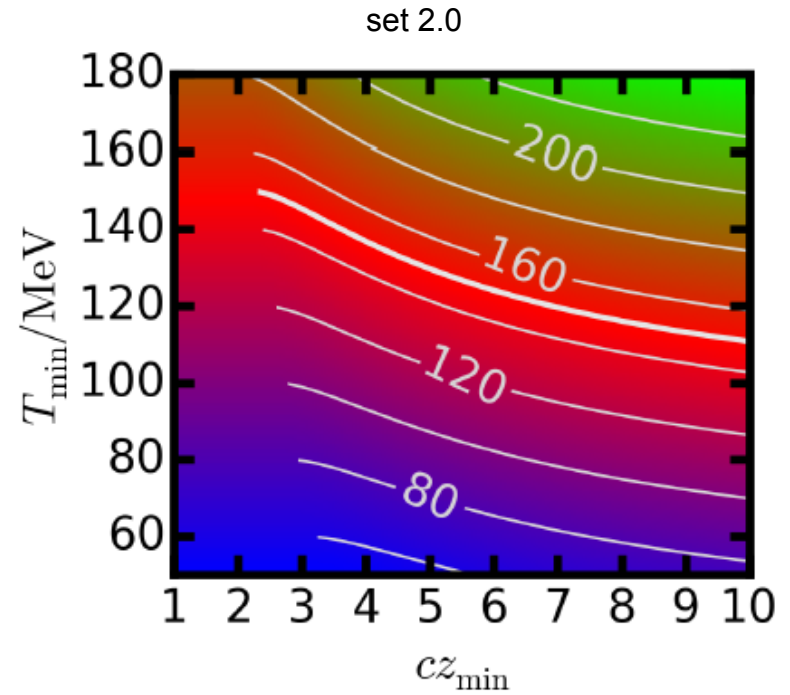
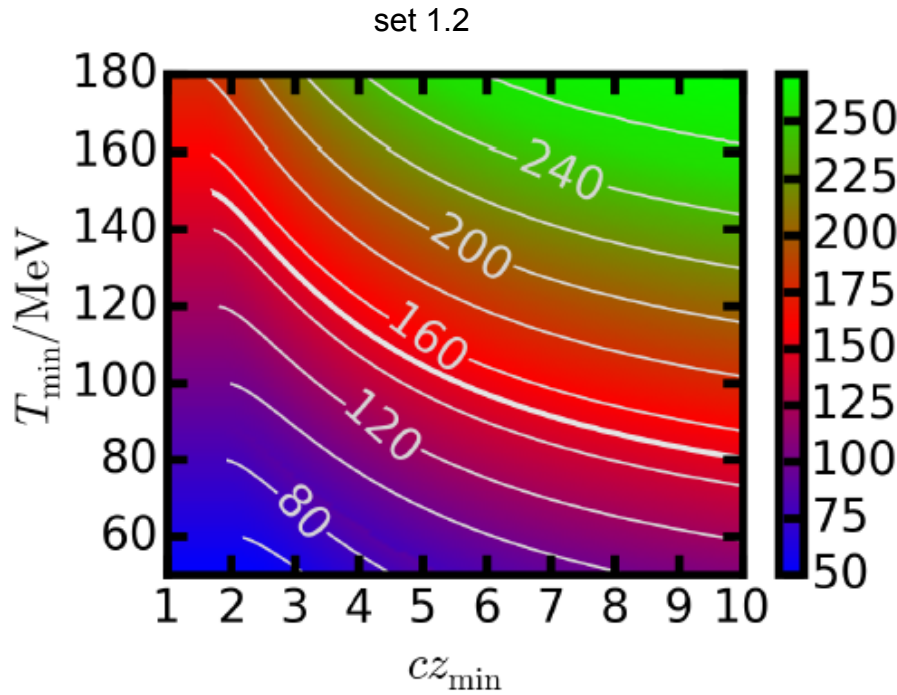
thermodyn. options:

continuous – cross over – 2nd order – 1st order transitions

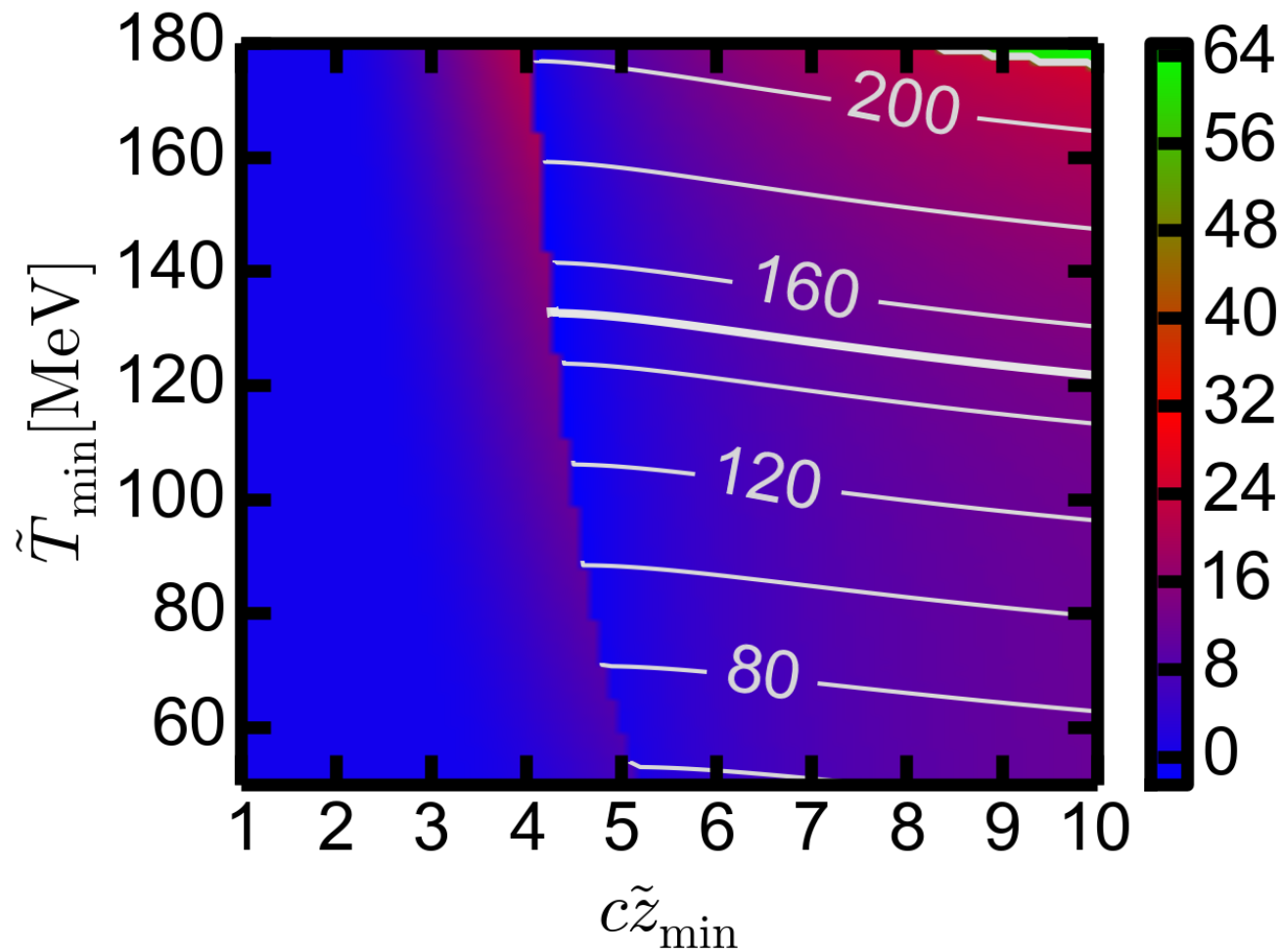


HZDR

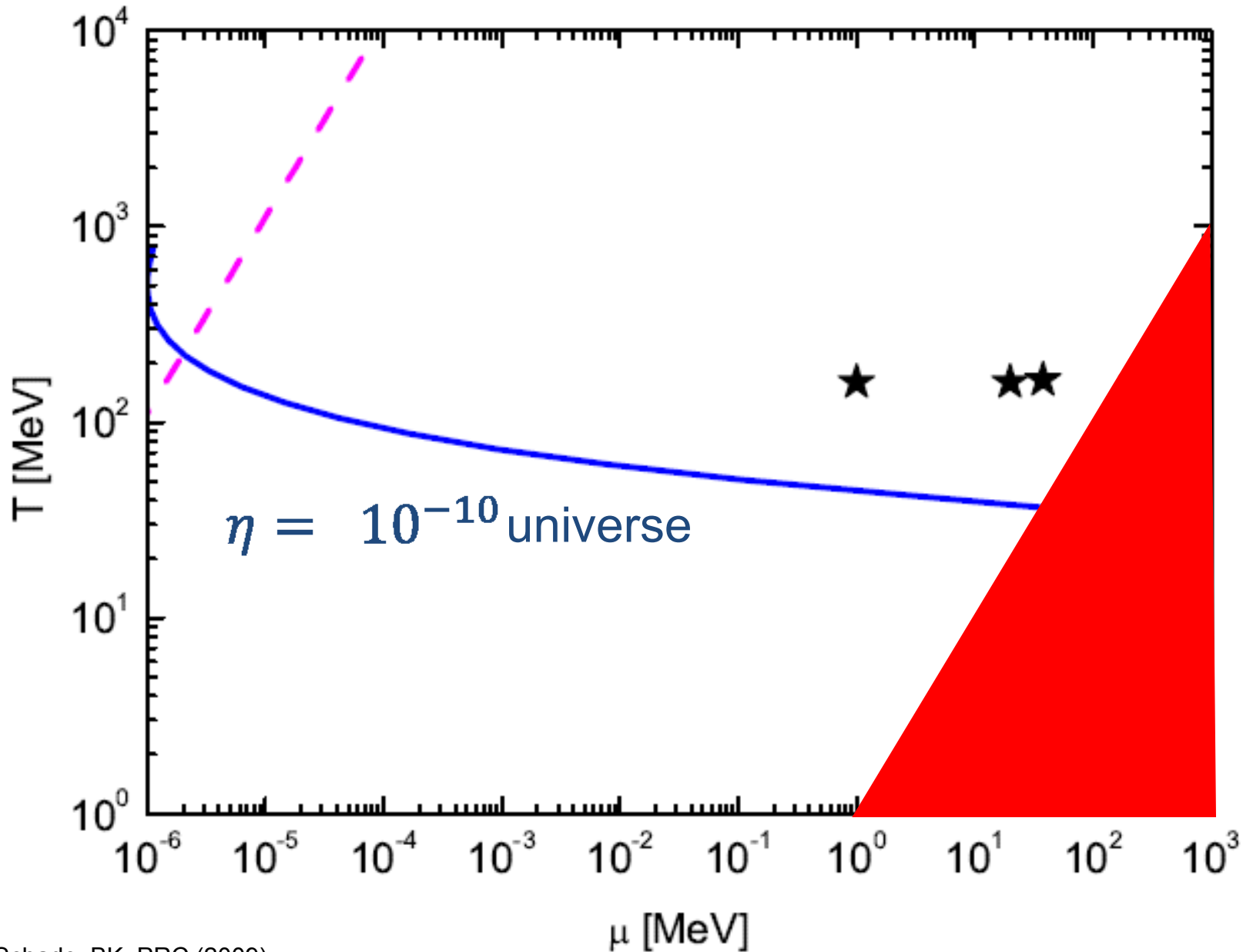
A two-parameter model for Tdis (T_{\min} , z_{\min})



contours: $T_{\text{dis}}(2\text{nd})$, color code: $T_{\text{dis}}(2\text{nd}) - T_{\text{dis}}(\text{g.s.})$



Cosmic Swing: from estimates to precision

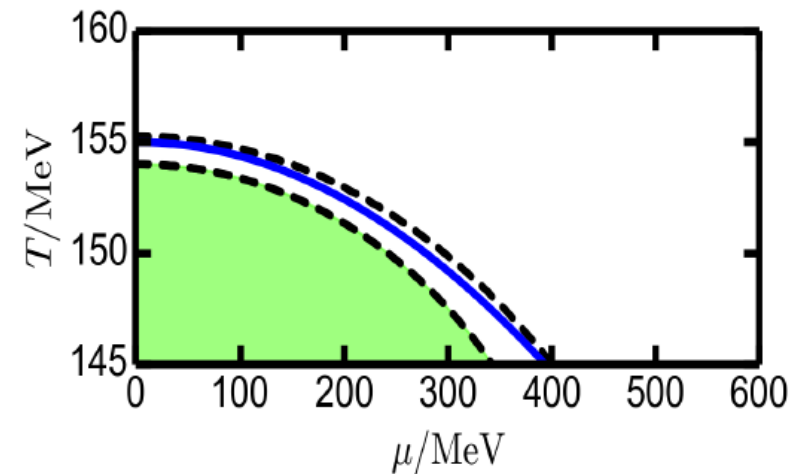
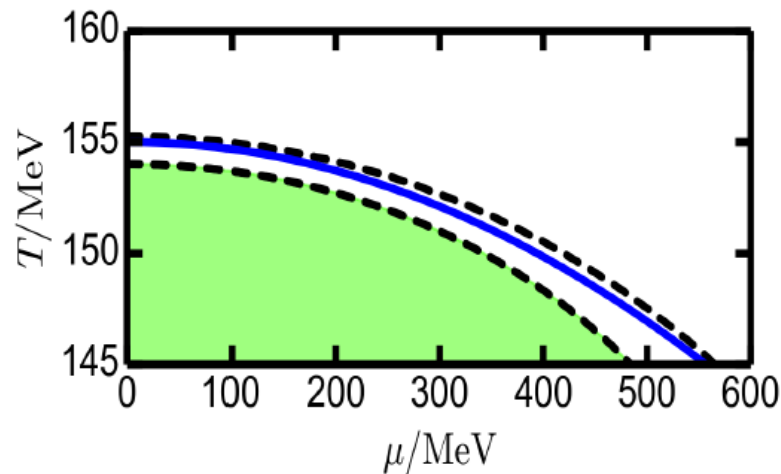
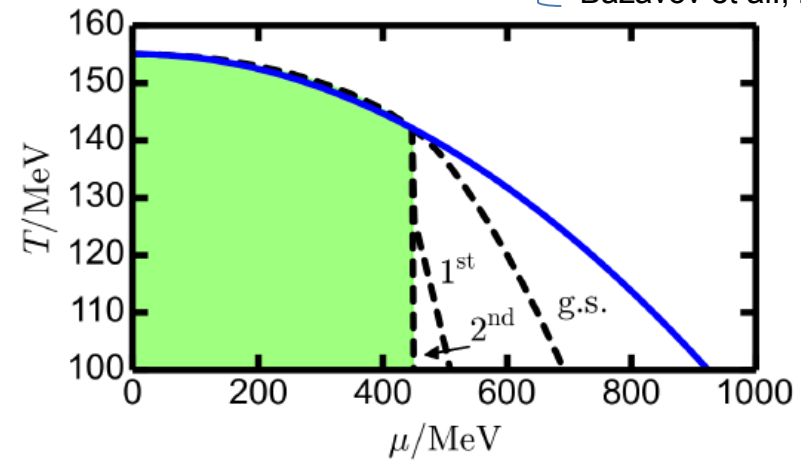
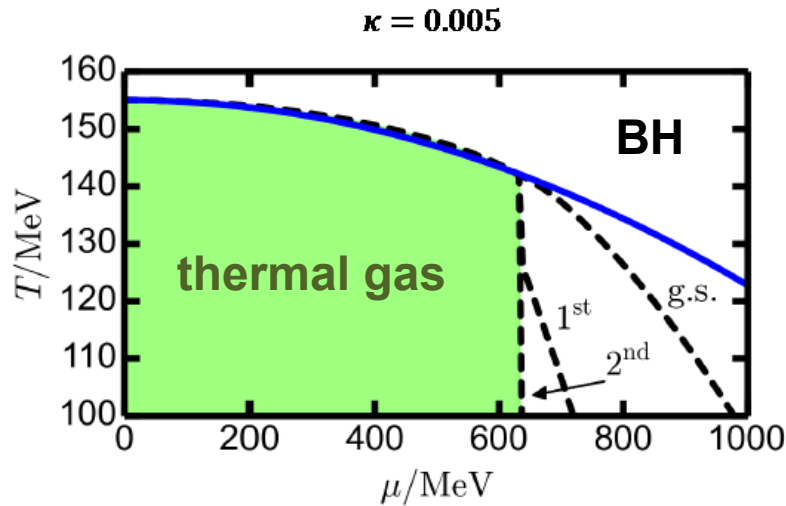


stars: chem. freeze-out ABC
(Andronic, Braun-Munzinger, Cleymans et al.)

Schwarzschild \rightarrow Reissner-Nordstrom BH

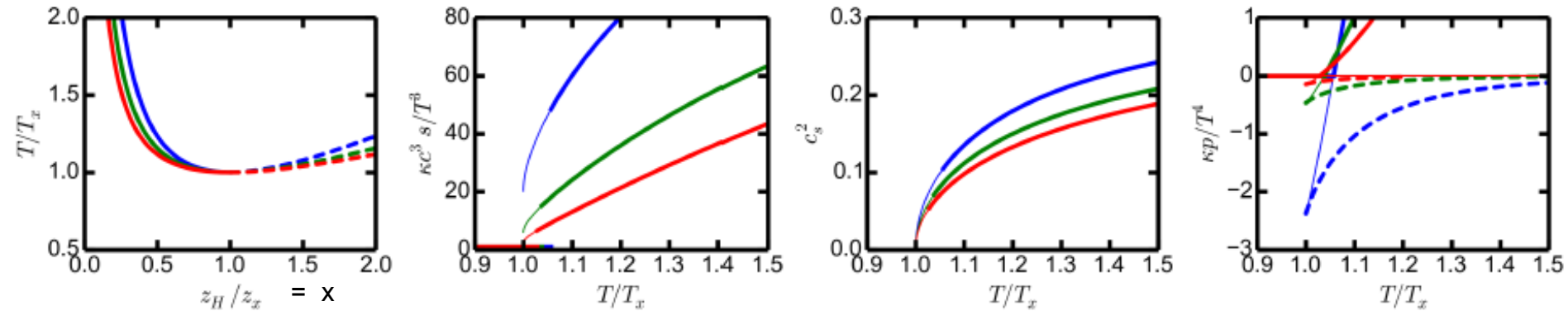
$$T_{f.o.}(\mu) \cong T_c(\mu) \cong T_0 \left(1 - \kappa \left(\frac{\mu}{T_0} \right)^2 + \dots \right)$$

$\kappa=0.01$ { Becattini et al., 1605.09694
Bazavov et al., PRD (2016)



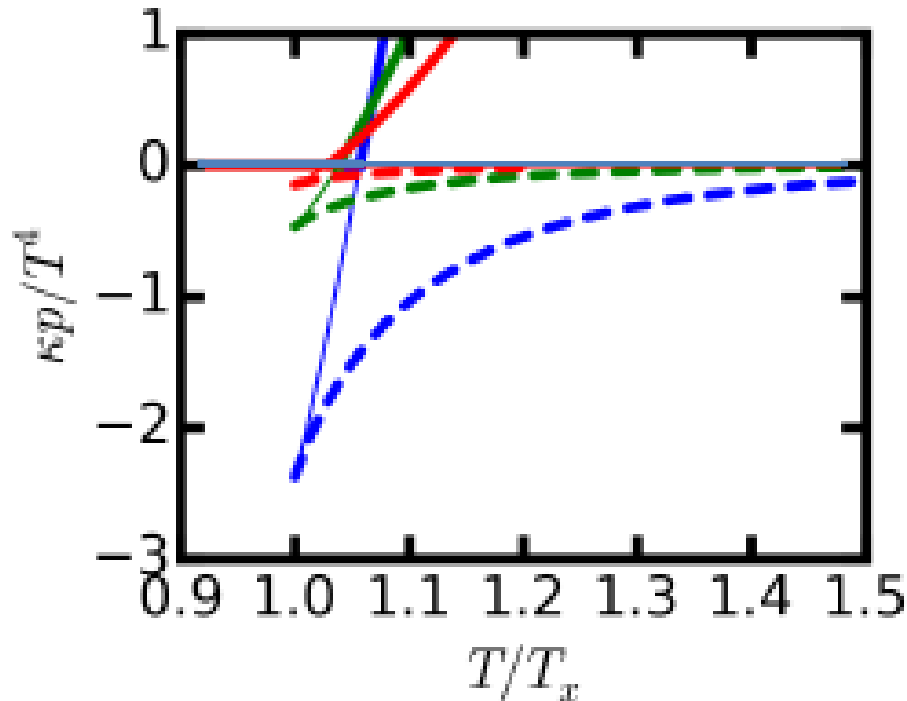
C12 argument for freezing out at T_c -

AdS-BH vs. Thermal Gas: FOPT



$$\frac{T}{T_x} = \frac{1}{x\theta} + 1 - \frac{2}{\theta} + \frac{x}{\theta}$$

$$\theta = \pi z_x T_x = 2/3 \text{ (blue), } 1 \text{ (green), } 4/3 \text{ (red)}$$



Kiritsis et al. (2008):

$$p(\text{BH}) \sim Nc^2$$

$$p(\text{therm.gas}) \sim O(Nc^0)$$

2+1 flavor QCD: phase diagram/Columbia plot

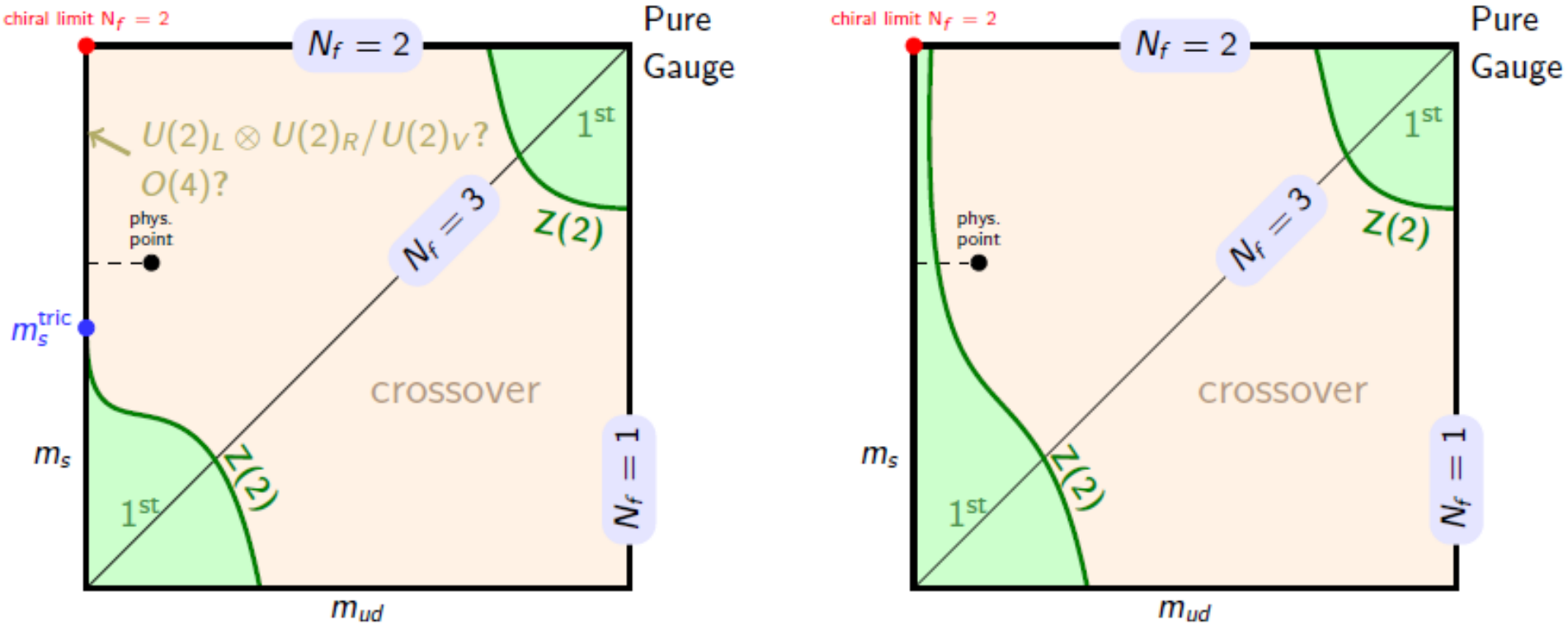
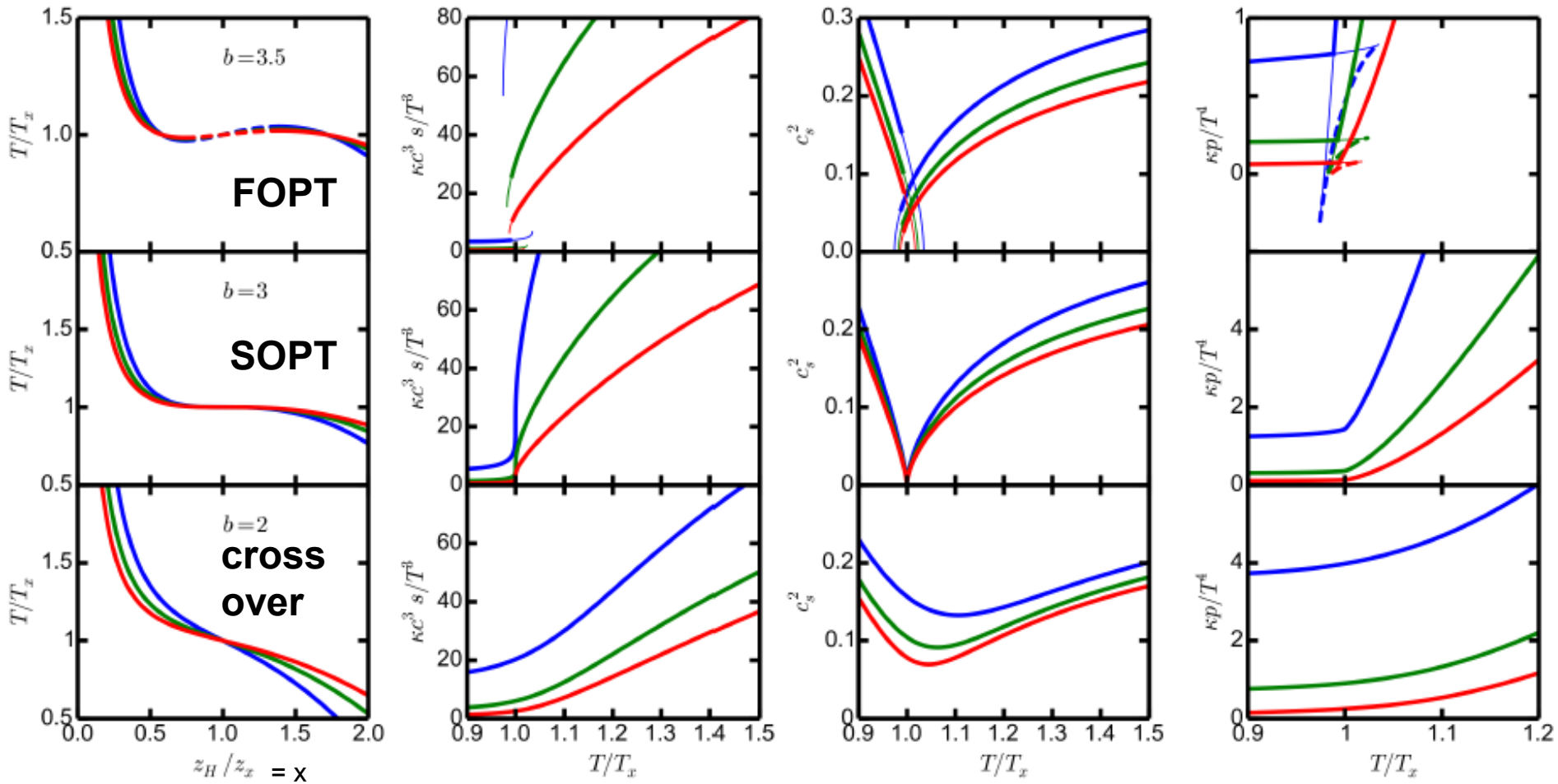


Figure 1: Possible scenarios for the QCD phase diagram at $\mu = 0$ as function of quark mass.

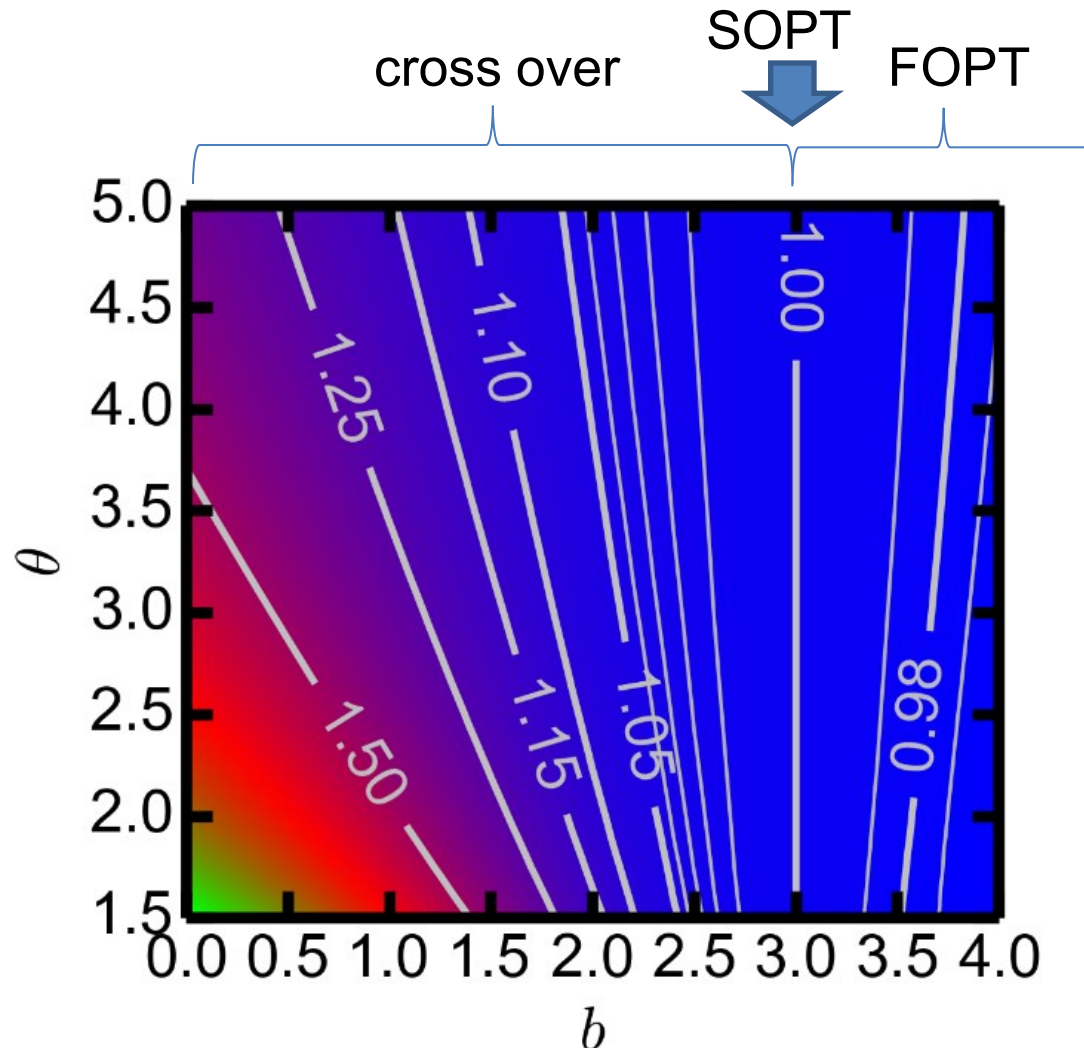
from Pinke & Philipsen, 2015

all the way AdS-BH: thermodynamics



$$\frac{T}{T_x} = \frac{1}{x\theta} + 1 - \frac{b}{\theta} + \frac{bx}{\theta} - \frac{x^2}{\theta}$$

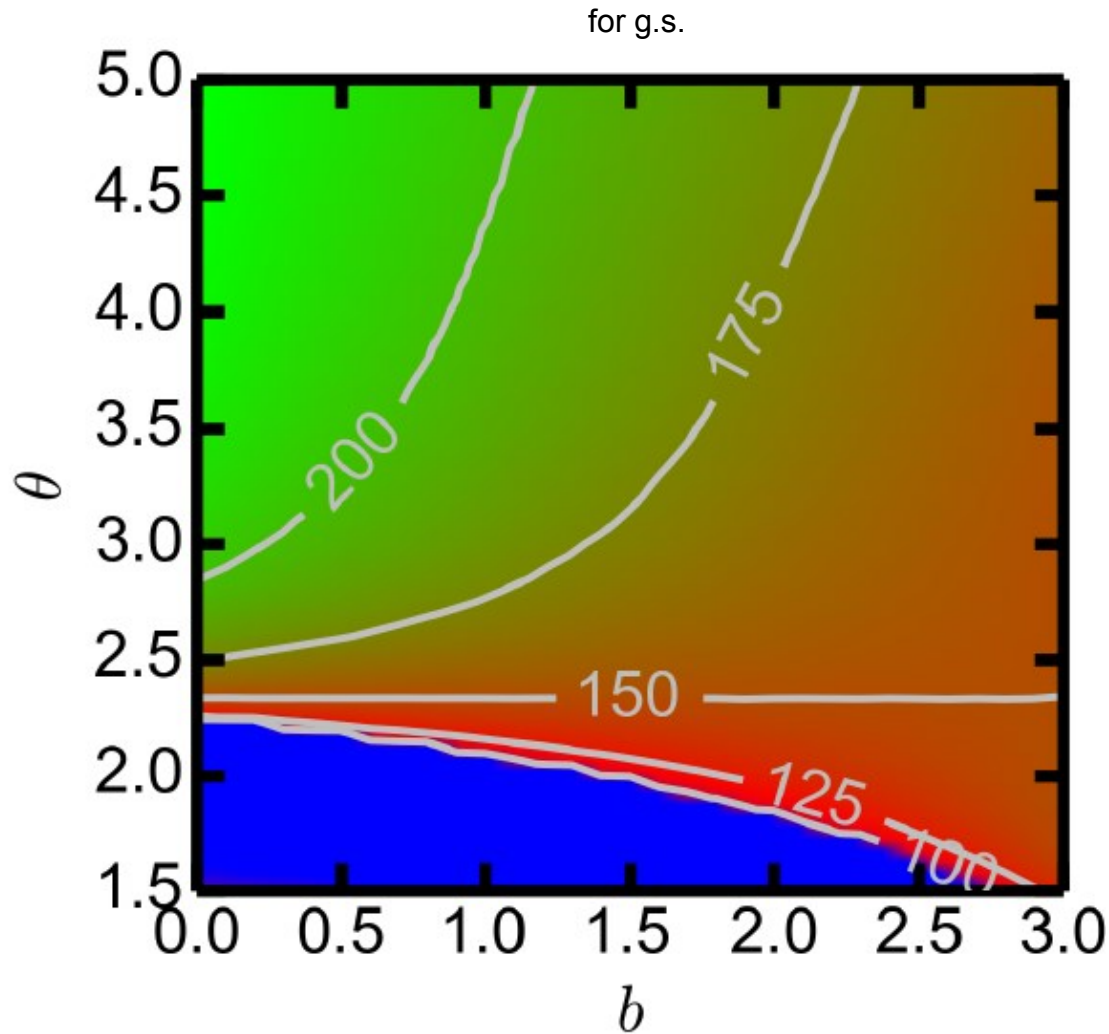
contour plot T_c/T_x vs. Theta - b



$$\theta = \pi z_x T_x$$

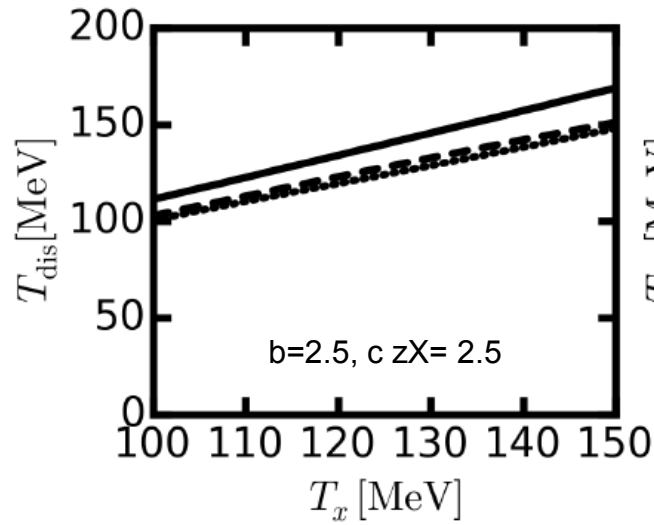
- hadron masses → scale setting c in dilaton
- thermodynamics → T_x from $T_c(\text{QCD})$
- deconfinement → $T_{\text{dis}} = T_c$

contour plot Tdis vs. Theta - b at Tx = 150 MeV

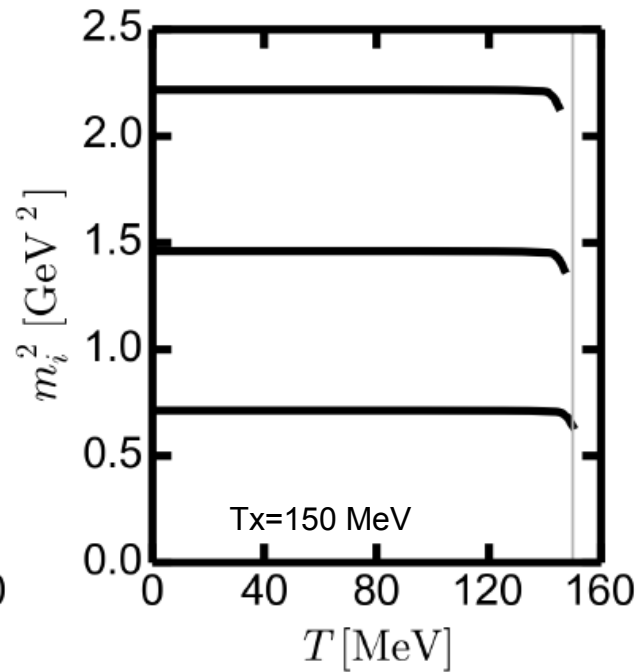
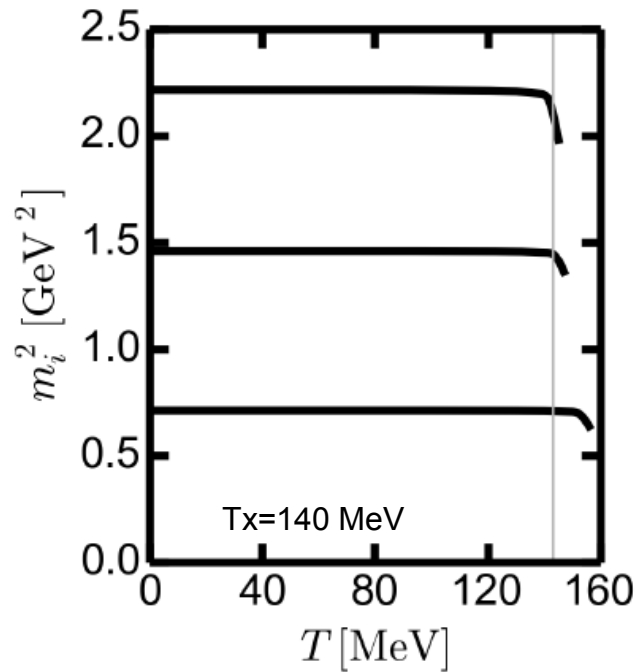
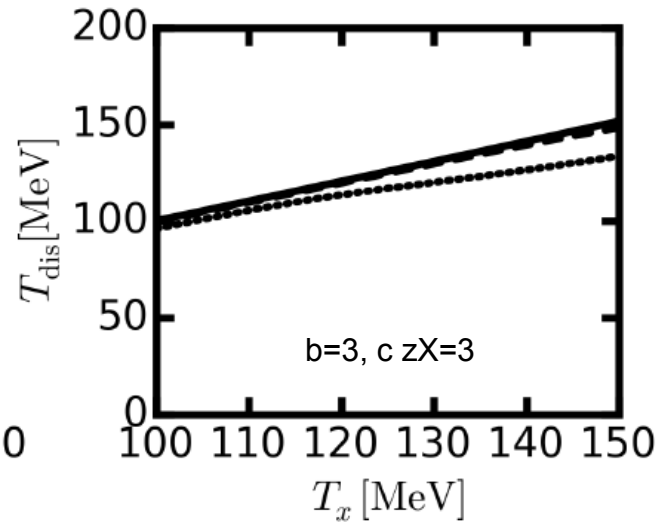


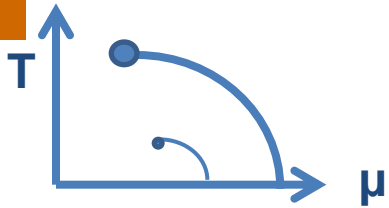
fine tuning of $T_x \rightarrow T_c = T_{dis}$

cross over



2nd order PT





A holographic phase diagram: update of the Gubser model

5D Einstein-dilaton-Maxwell model

$$S = \frac{1}{2\kappa_5} \int d^5x \sqrt{-g} \left(R - \frac{1}{2} \partial^\mu \phi \partial_\mu \phi - V(\phi) - \frac{f(\phi)}{4} F_{\mu\nu}^2 \right) + S_{GH}$$

DeWolfe, Gubser, Rosen, PRD (2010, 2011)

solve Einstein eqs. + EoM for dilaton and Maxwell
with proper conds. at boundary and horizon,
get T, s, μ, n (AdS/CFT dictionary),
integrate to get $p(T, \mu)$ to be used for susceptibilities

adjustments at $\mu = 0$: (i) lattice QCD thermodynamics $\rightarrow V(\phi)$

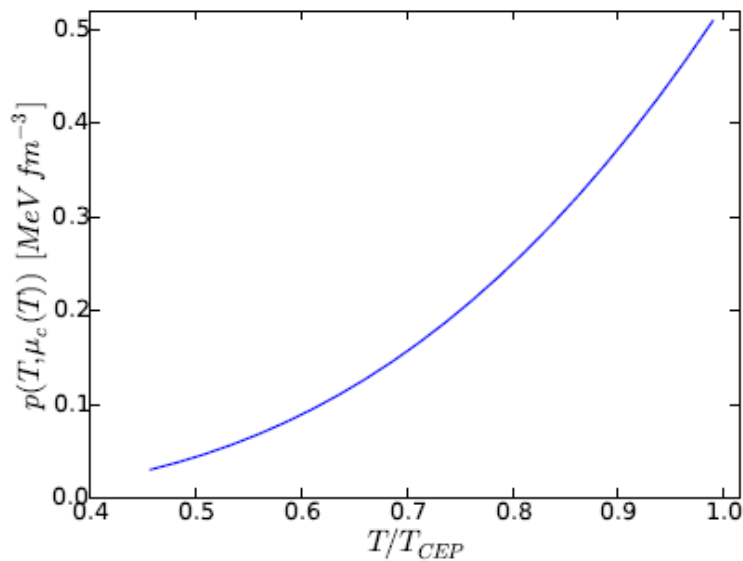
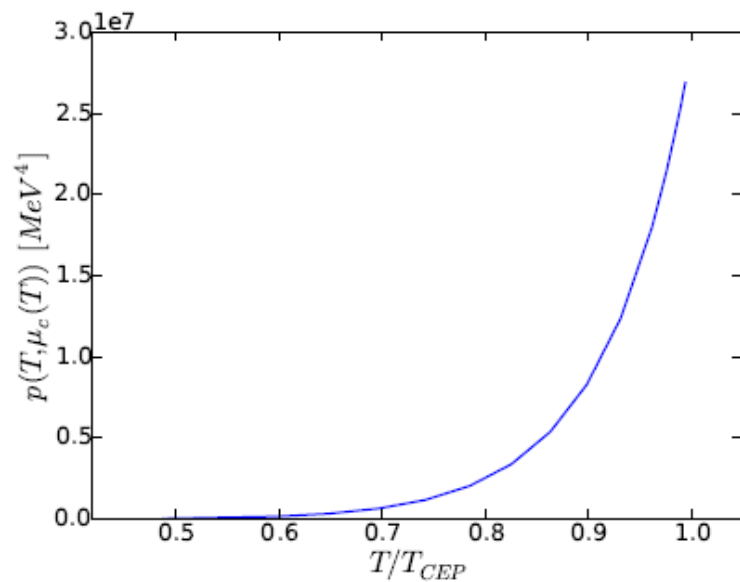
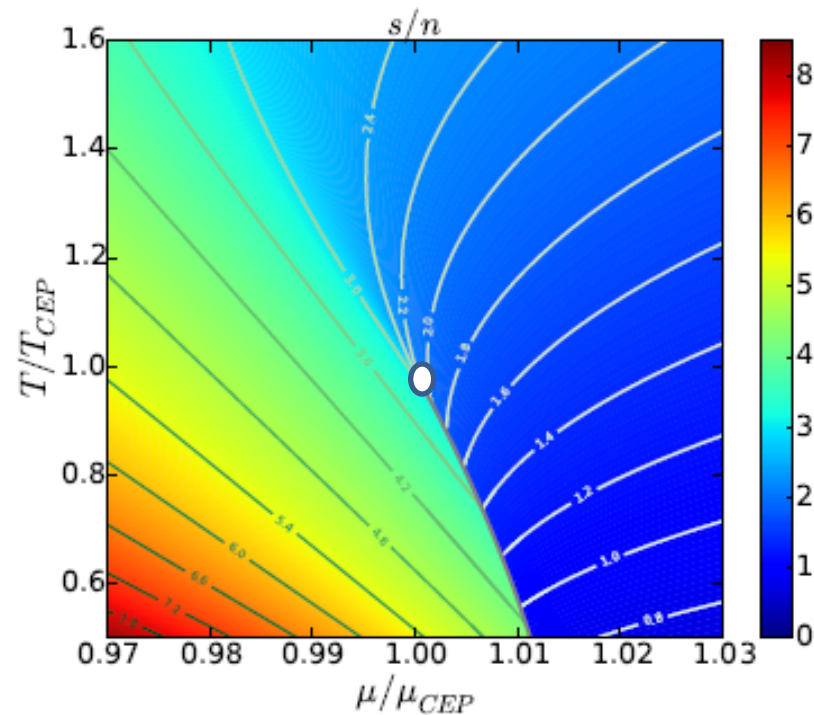
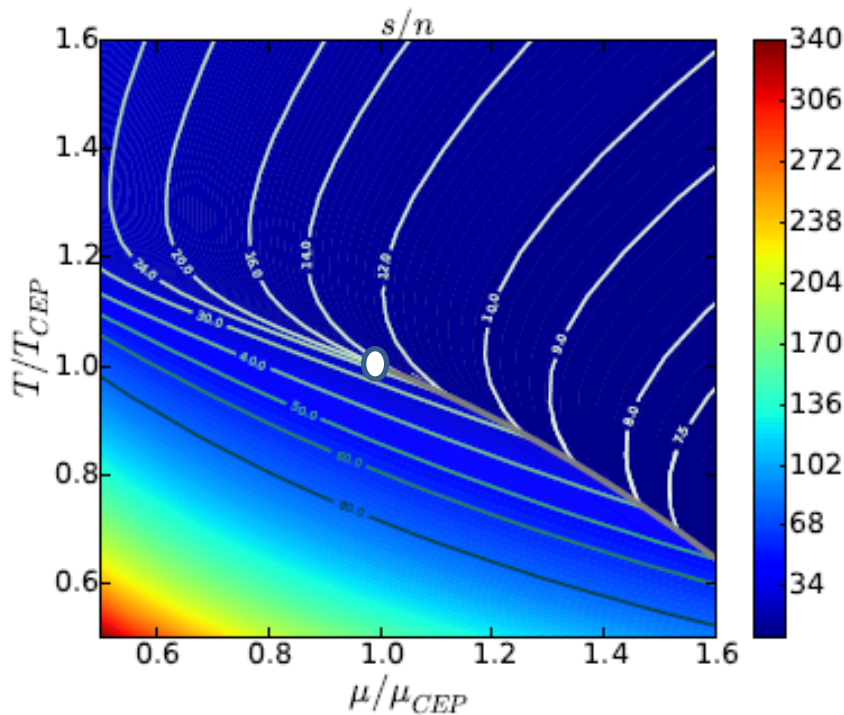
cf. Yaresko, BK, PLB (2015), Yaresko, Knaute, BK, EPJC (2015)

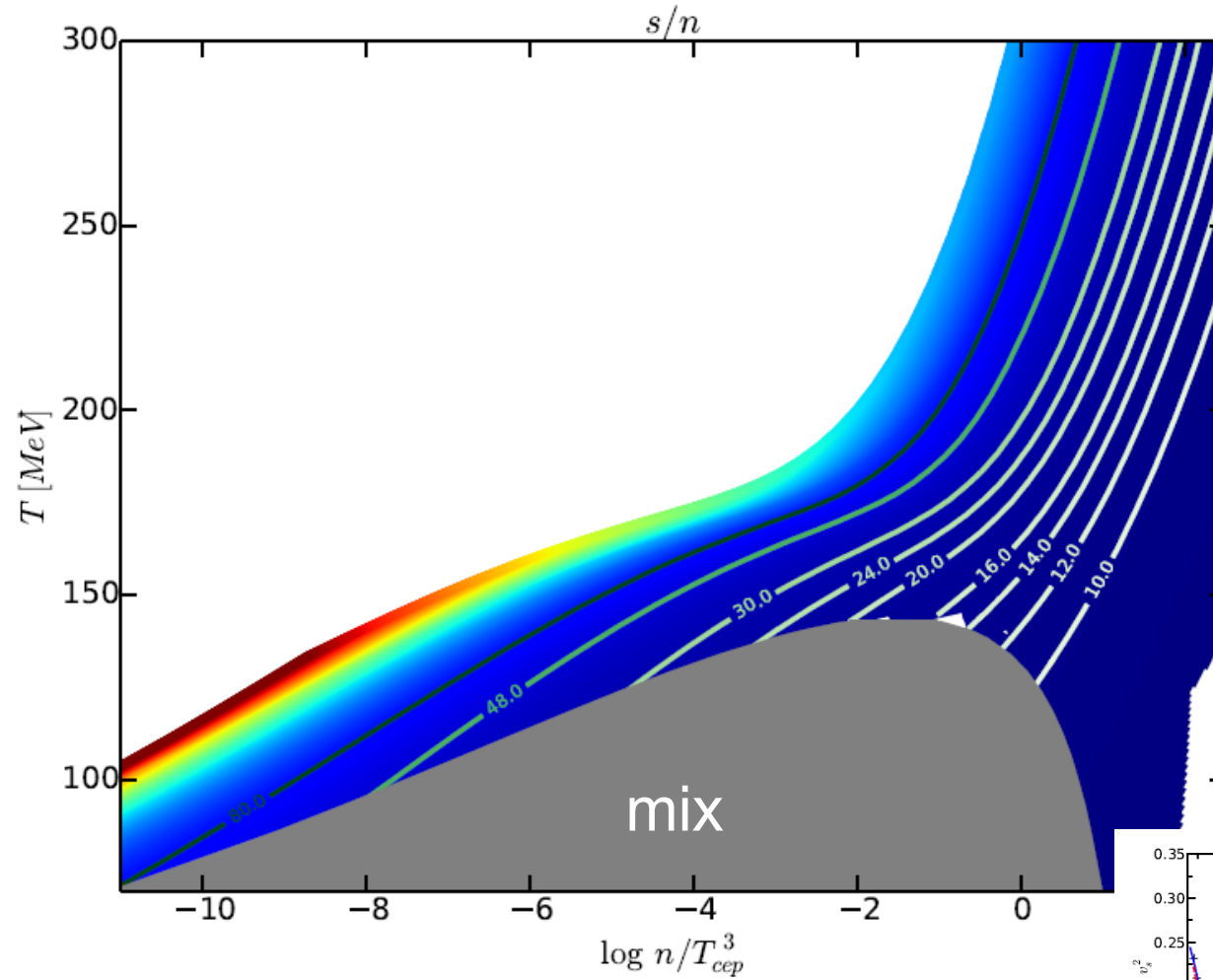
(ii) susceptibilities $\rightarrow f(\phi)$

work in progress

Holography a la Gubser et al.

vdW a la Gorenstein et al.

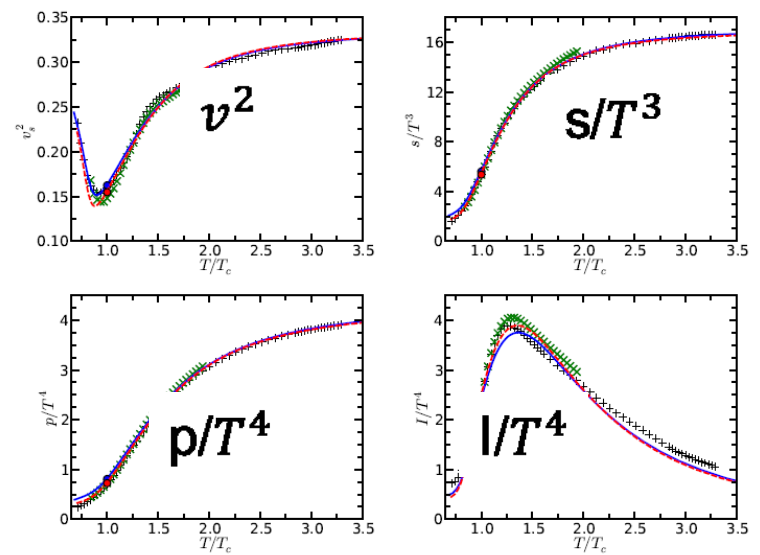




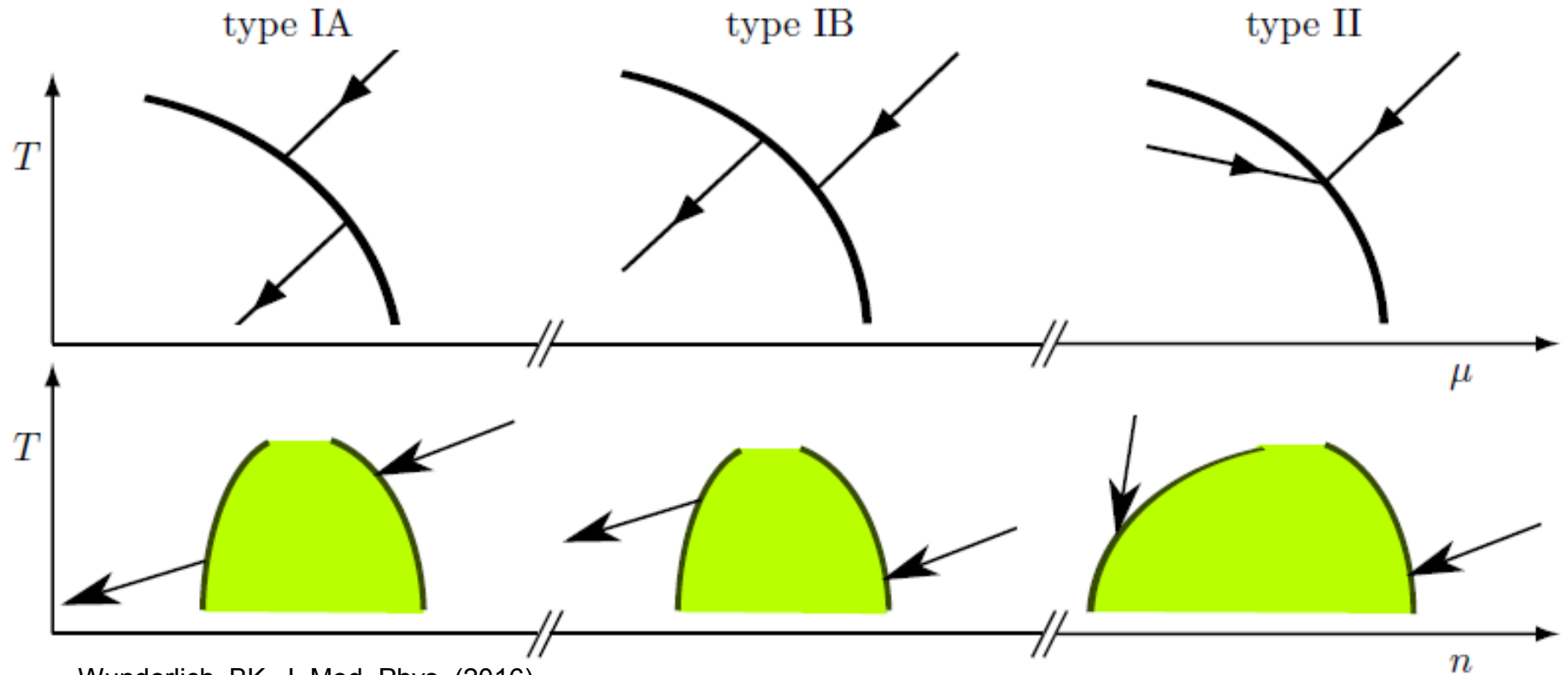
QCD input: $N_f = 2+1$, phys. q masses
 Bazazov et al (2014), Borzanyi et al (2014)

surprize: incoming isentropes only
 (as in vdW)

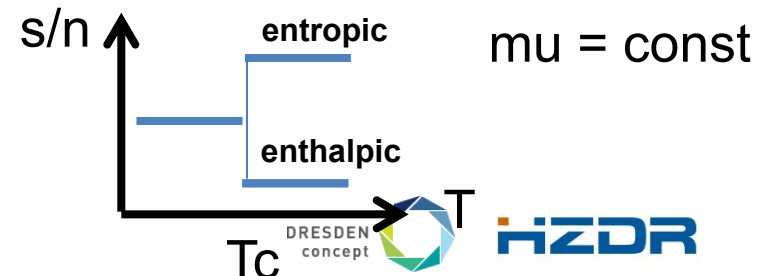
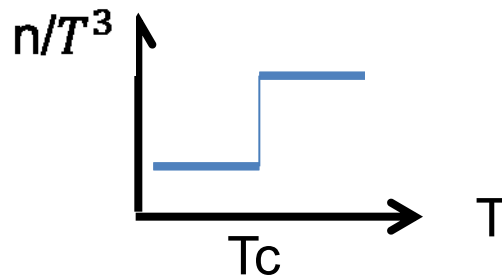
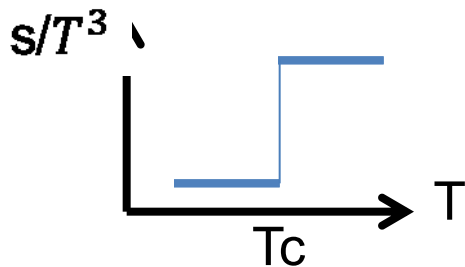
Steinheimer, Randrup, Koch, PRC (2014),
 Steinheimer, Randrup, PRL (2012),
 Hempel, Dexheimer, Schramm, Iosilevskiy, PRC (2013)
 and others claim: deconfinement is accompanied by
 dropping pressure on critical curve



Crossing the phase border line



Wunderlich, BK, J. Mod. Phys. (2016)



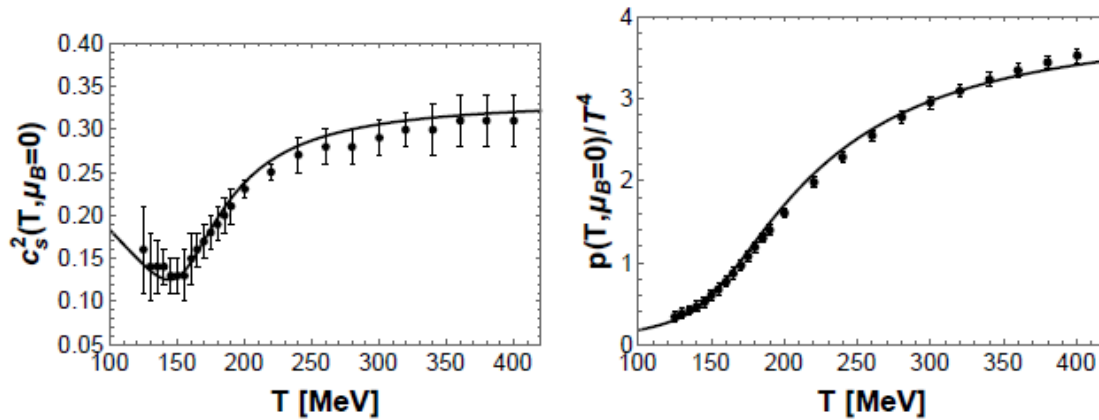
Summary

- (i) Bulk viscosity = 0.5 shear viscosity at T_c

- (ii) extended soft wall model for vector mesons:
 - + $T = 0$: two options for rho Regge trajectories
 - + $T > 0$: emulating deconfinement as disappearance (instant. vs. sequential) of hadrons at $T(QCD)$
 - + contact to thermodynamics (ambient medium mimicked by dilation via ansatz)
 - ? construction of a phase diagram

- (iii) holographic phase diagram:
 - + accommodates QCD thermodynamics (medium mimicked by self consist. dilaton)
 - no individual hadrons sourcing dilaton below T_c
 - vdW behavior (w/o tuning 4th order susceptibility)

Results of the Sao Paulo Group



Rougemont et al.
JHEP (2015), PRL (2015)

