

# Azimuthal flow and chiral magnetic effect in nucleus-nucleus collisions

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# Basic Concept of HSD

## HSD – Hadron-String-Dynamics transport approach

Ehehalt, Cassing, Nucl.Phys. A602 (1996) 449; Cassing, Bratkovskaya, Phys. Rep.308 (1999) 65.

- the phase-space density  $f_i$  follows the **transport equations**

$$\left( \frac{\partial}{\partial t} + (\nabla_{\vec{p}} H) \nabla_{\vec{r}} - (\nabla_{\vec{r}} H) \nabla_{\vec{p}} \right) f_i(\vec{r}, \vec{p}, t) = I_{coll}(f_1, f_2, \dots, f_M)$$

with **collision terms**  $I_{coll}$  describing:

- **elastic and inelastic hadronic reactions:**

**baryon-baryon, meson-baryon, meson-meson**

- **formation and decay of baryonic and mesonic resonances**

- **string formation and decay**

(for inclusive particle production:  $BB \rightarrow X$ ,  $mB \rightarrow X$ ,  $X = \text{many particles}$ )

- implementation of **detailed balance** on the level of  $1 \leftrightarrow 2$  and  $2 \leftrightarrow 2$  reactions (+  **$2 \leftrightarrow n$  multi-particle reactions in HSD !**)
- no explicit phase transition from hadronic to partonic degrees of freedom

# The Dynamical QuasiParticle Model (DQPM)

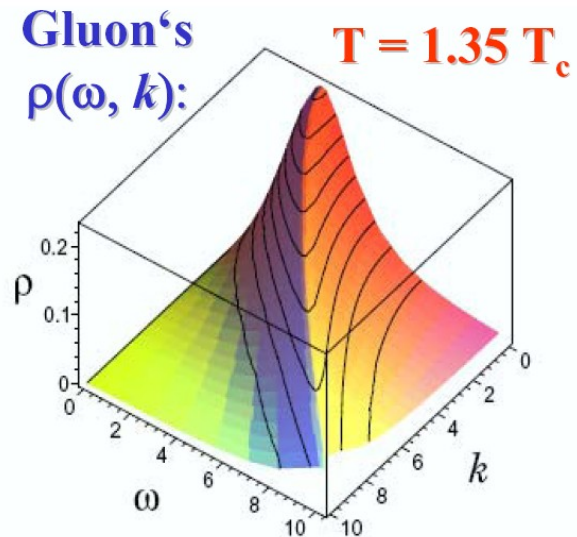
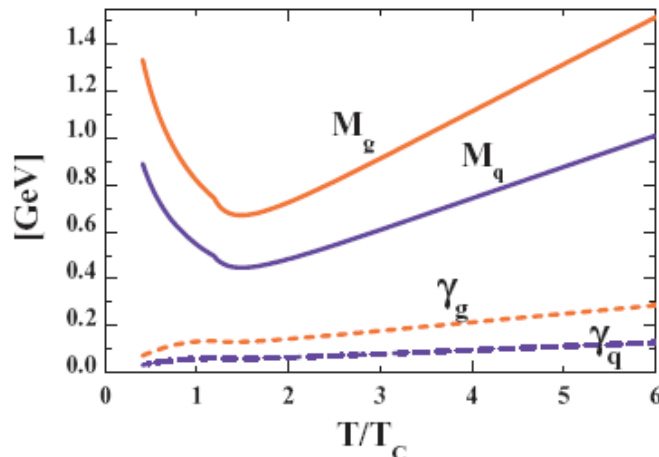
Interacting quasiparticles massive quarks and gluons (  $g, q, \bar{q}$  )  
with spectral functions

$$\rho(\omega) = \frac{\gamma}{E} \left( \frac{1}{(\omega - E)^2 + \gamma^2} - \frac{1}{(\omega + E)^2 + \gamma^2} \right)$$

fit to lattice (IQCD) results (e.g. entropy density)

**Quasiparticle properties:**

large width and mass for gluons and quarks



**DQPM matches well lattice QCD**

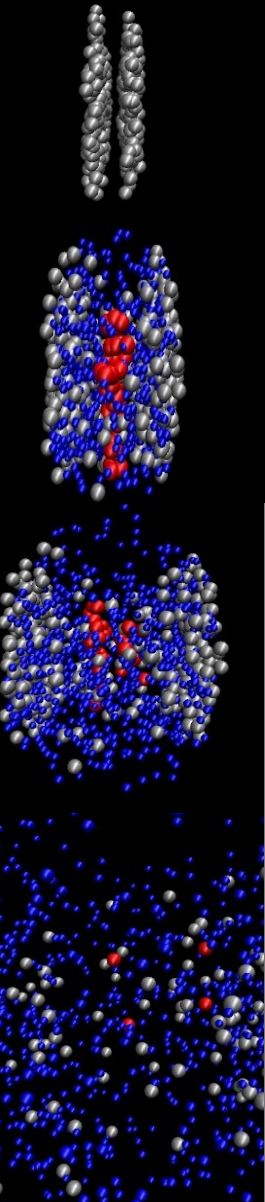
**DQPM provides mean-fields (1PI) for gluons and quarks**  
as well as **effective 2-body interactions (2PI)**

**DQPM gives transition rates for the formation of hadrons => PHSD**



# Parton-Hadron String Dynamics (PHSD)

- **Initial A+A collisions – HSD: string formation and decay to pre-hadrons**
- **Fragmentation of pre-hadrons into quarks:** using the quark spectral functions from the **Dynamical QuasiParticle Model (DQPM)** approximation to QCD  
DQPM: Peshier, Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365; NPA 795 (2007) 70.
- **Partonic phase:** quarks and gluons (= 'dynamical quasiparticles') with **off-shell spectral functions** (width, mass) defined by the DQPM
- **Elastic and inelastic parton-parton interactions:** using the effective cross sections from the DQPM
  - ✓  $q + \bar{q}$  (flavor neutral)  $\Leftrightarrow$  gluon (colored)
  - ✓ gluon + gluon  $\Leftrightarrow$  gluon (possible due to large spectral width)
  - ✓  $q + \bar{q}$  (color neutral)  $\Leftrightarrow$  hadron resonances
- **Hadronization:** based on DQPM - massive, off-shell quarks and gluons with broad spectral functions hadronize to **off-shell mesons and baryons:**
  - ✓ gluons  $\Rightarrow q + \bar{q}$
  - ✓  $q + \bar{q} \Rightarrow$  meson (or string)
  - ✓  $q + q + q \Rightarrow$  baryon (or string)W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; EPJ ST 168 (2009) 3.
- **Hadronic phase:** hadron-string interactions – off-shell HSD



PHSD: Au+Au @ 21300 AGeV,  $b = 1$  fm

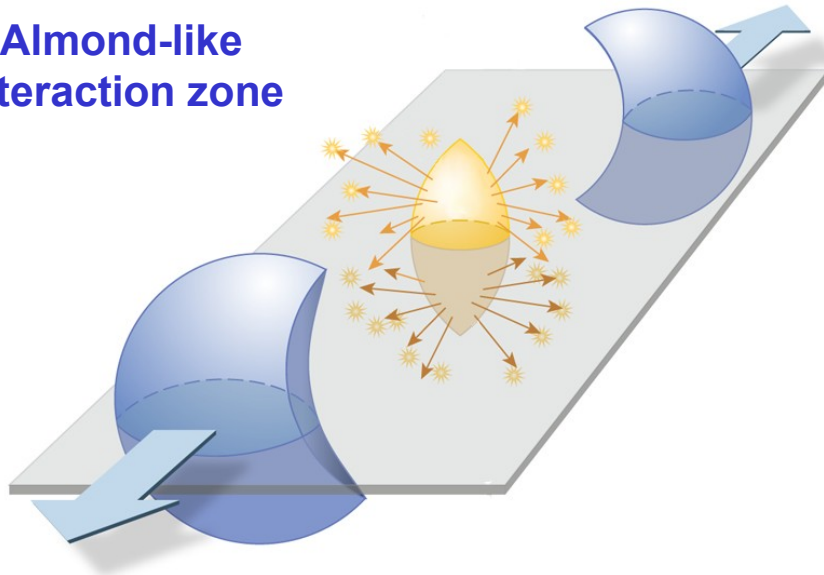
$t = 0.3$  fm/c  
Section View

- baryon
- meson
- quark
- gluon



# Flow harmonics: motivation

Almond-like interaction zone



pressure gradient

=> spatial asymmetry is converted  
to an asymmetry in momentum space  
=> collective flow

$$\frac{dN}{dy p_T dp_T d\phi} = \frac{dN}{dy p_T dp_T} \frac{1}{2\pi} (1 + 2v_1 \cos(\phi) + 2v_2 \cos(2\phi) + \dots)$$

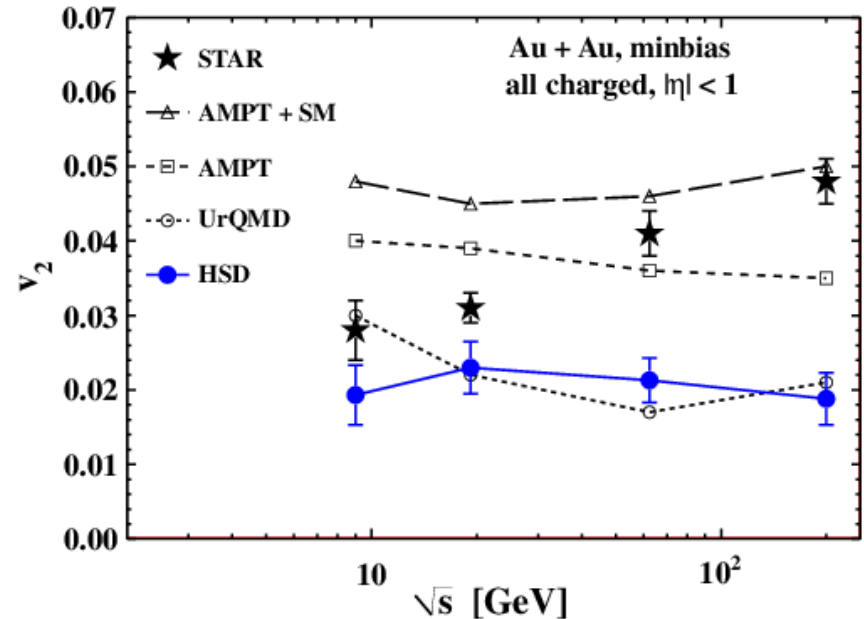
$$v_1 = \left\langle \frac{p_x}{p_T} \right\rangle$$

Direct flow

$$v_2 = \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle$$

Elliptic flow

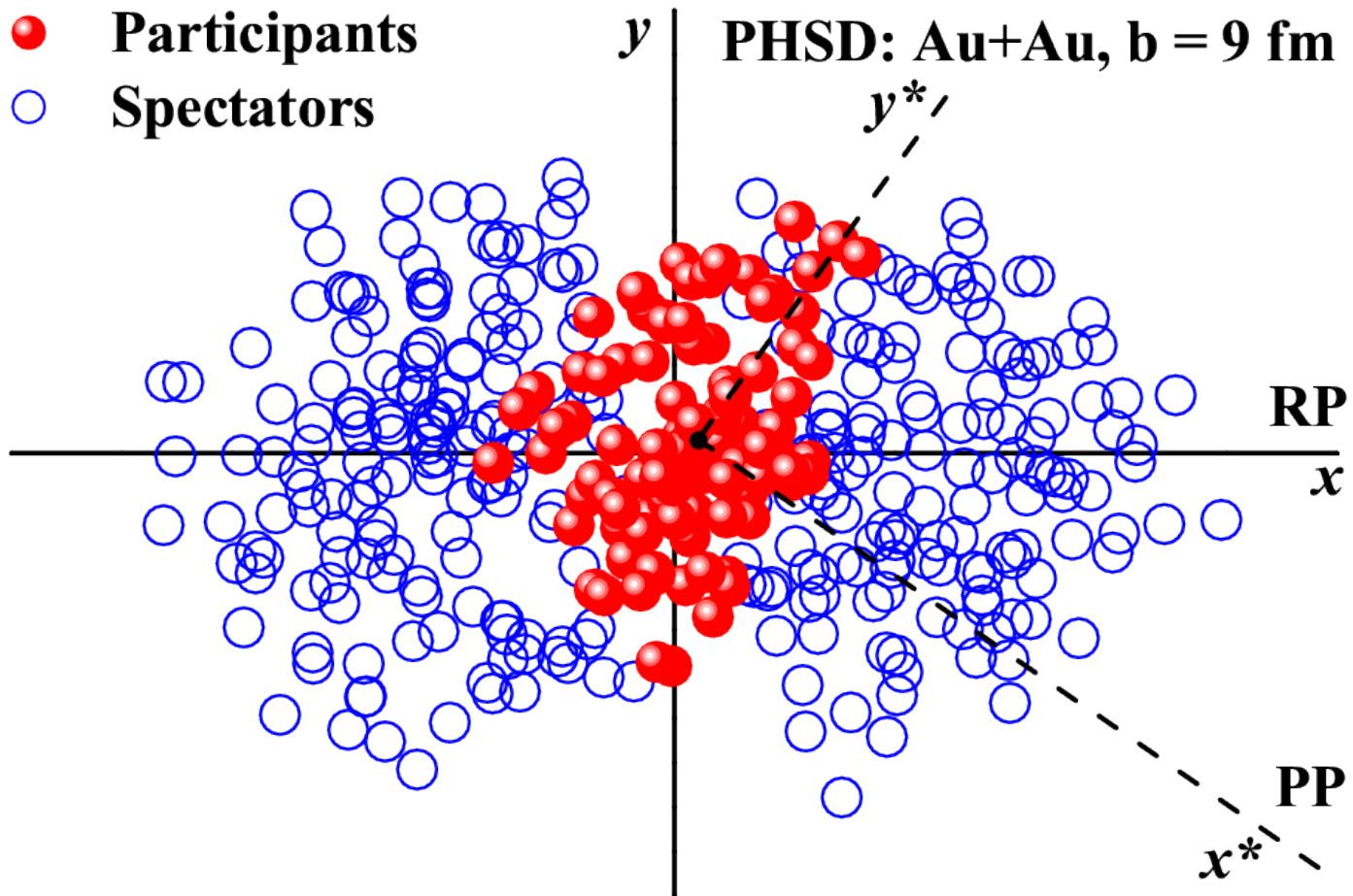
M.Nasim et al.,  
PRC82, 054908 (2010)



Neither hadronic nor partonic models  
can explain the energy  
dependence of  $v_2$ !

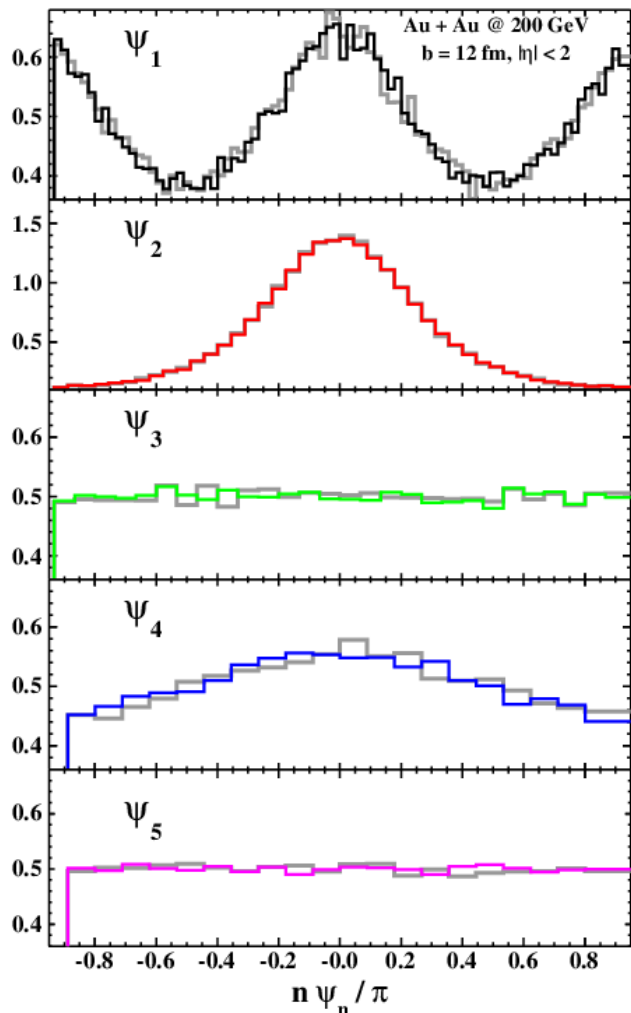


# Initial spatial distribution in a single event

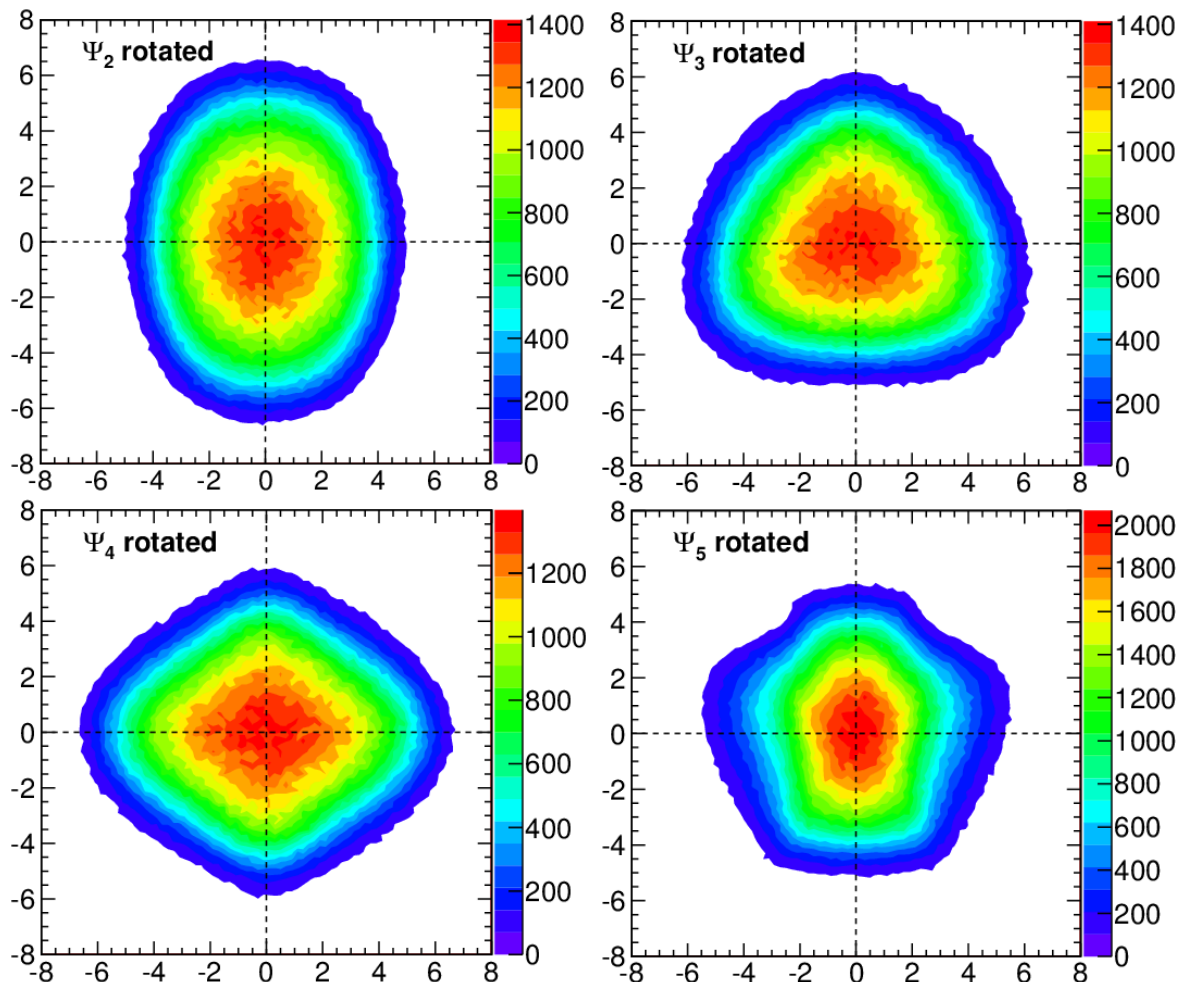


In a single event the Participant Plane (PP) is tilted relative to the Reaction Plane (RP).  
Higher order harmonics may be formed, too!

# Final angular distribution in p-space



Event plane distributions:  
even – peaked,  
odd – flat.

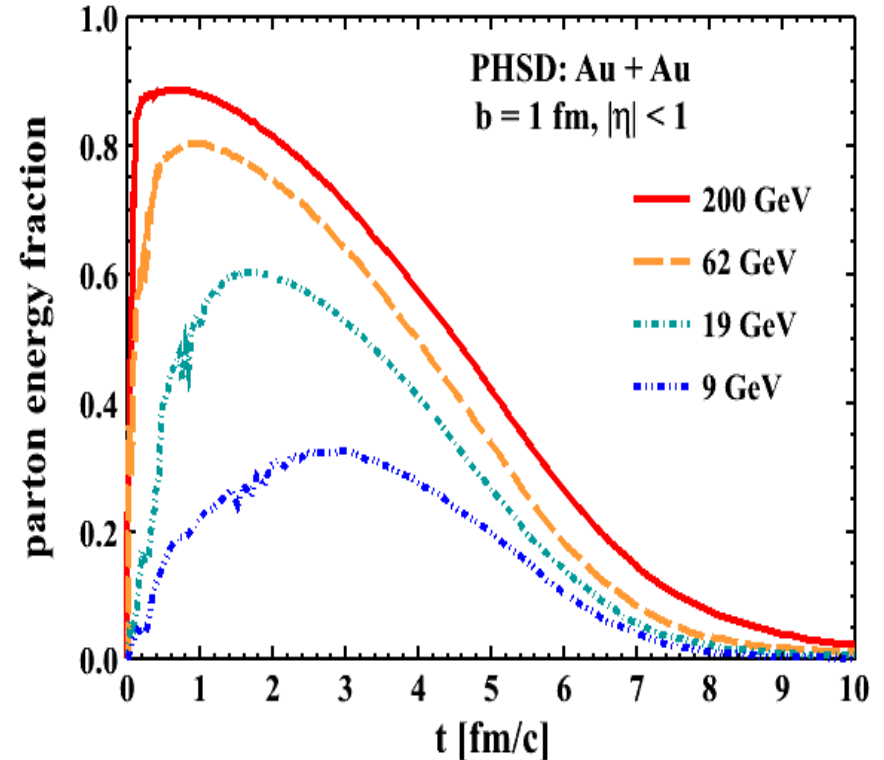
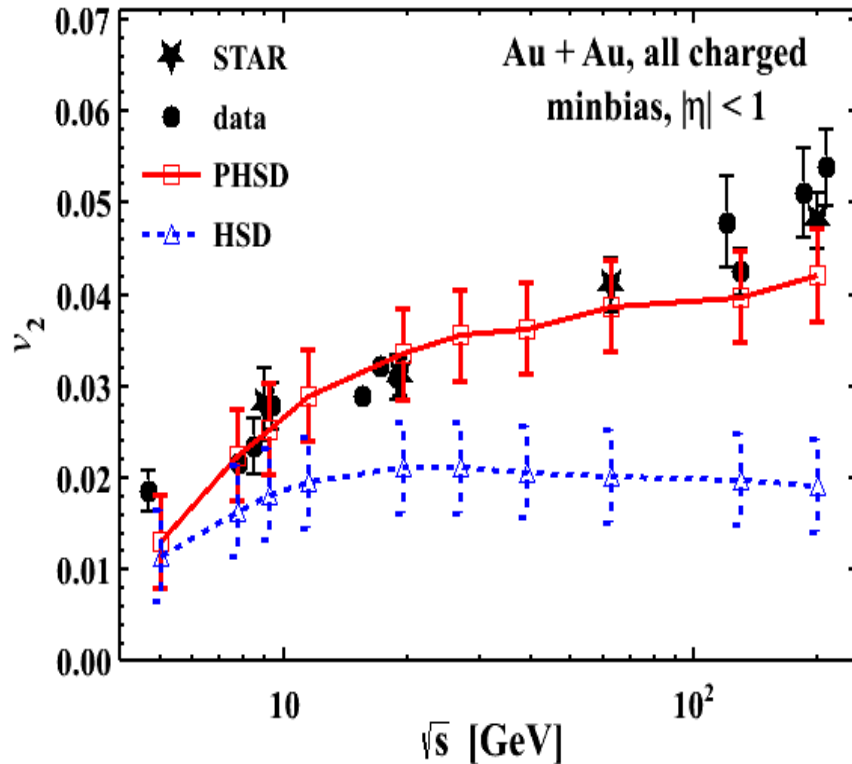


Au+Au collisions  
rotated to different event planes.

S. Voloshin, arXiv: 1111.7241

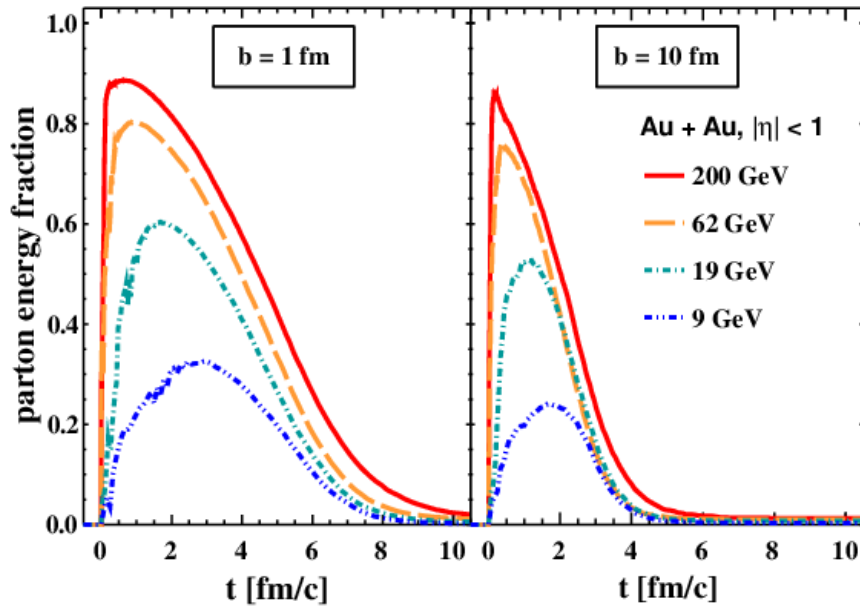


# Energy dependence of $v_2$ from PHSD



Increase of elliptic flow  $v_2$  with collision energy is reasonably described by PHSD due to an increasing fraction of partonic degrees of freedom.

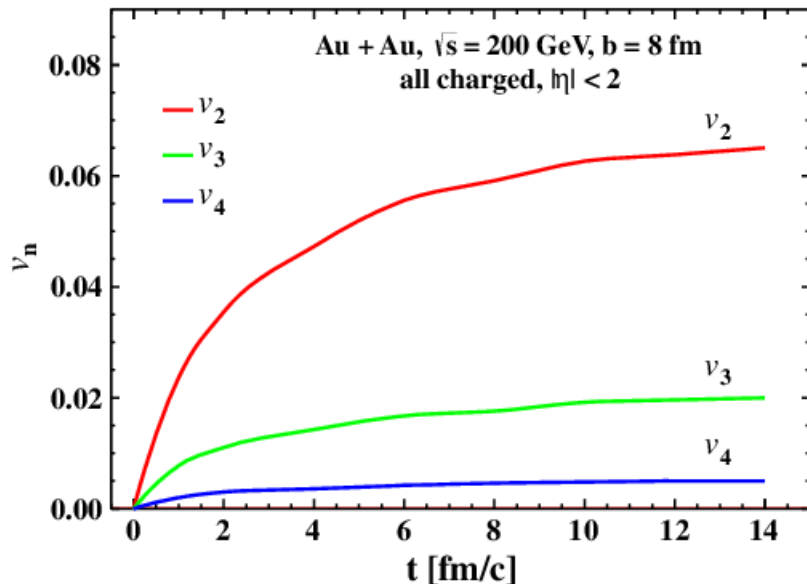
# Formation of flow



◆ Relative number of partons does not depend much on centrality.

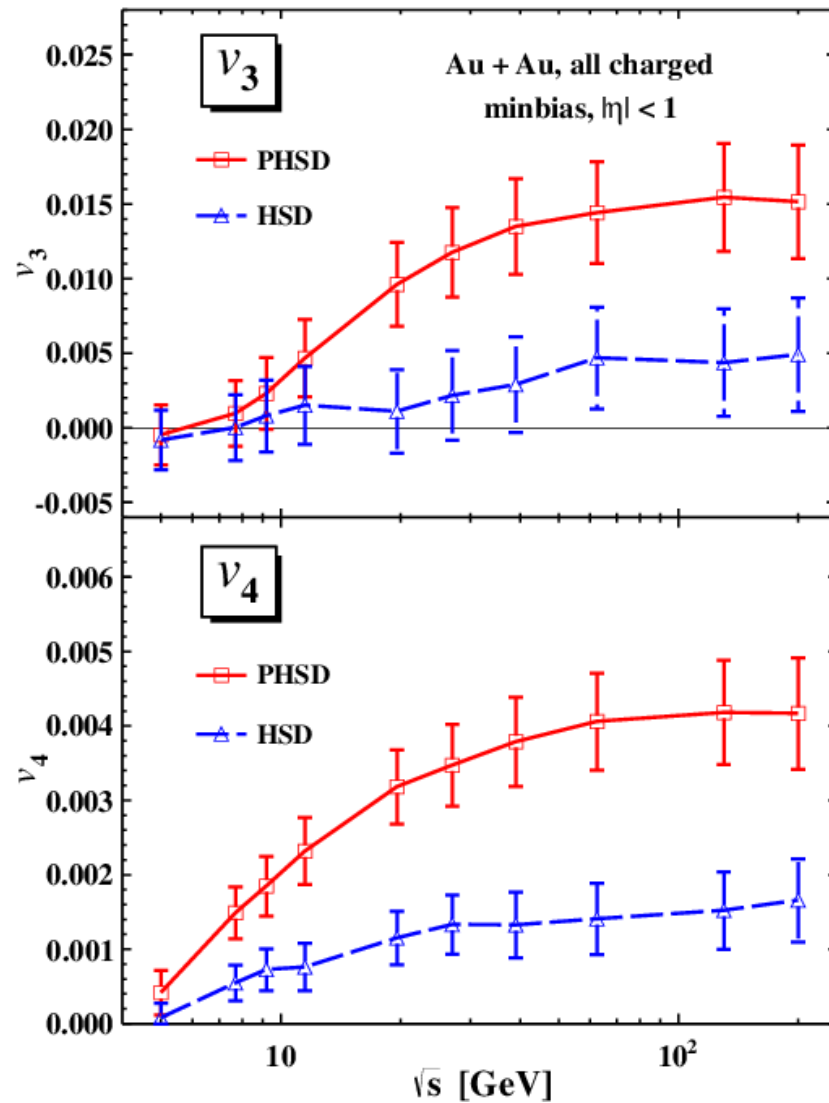
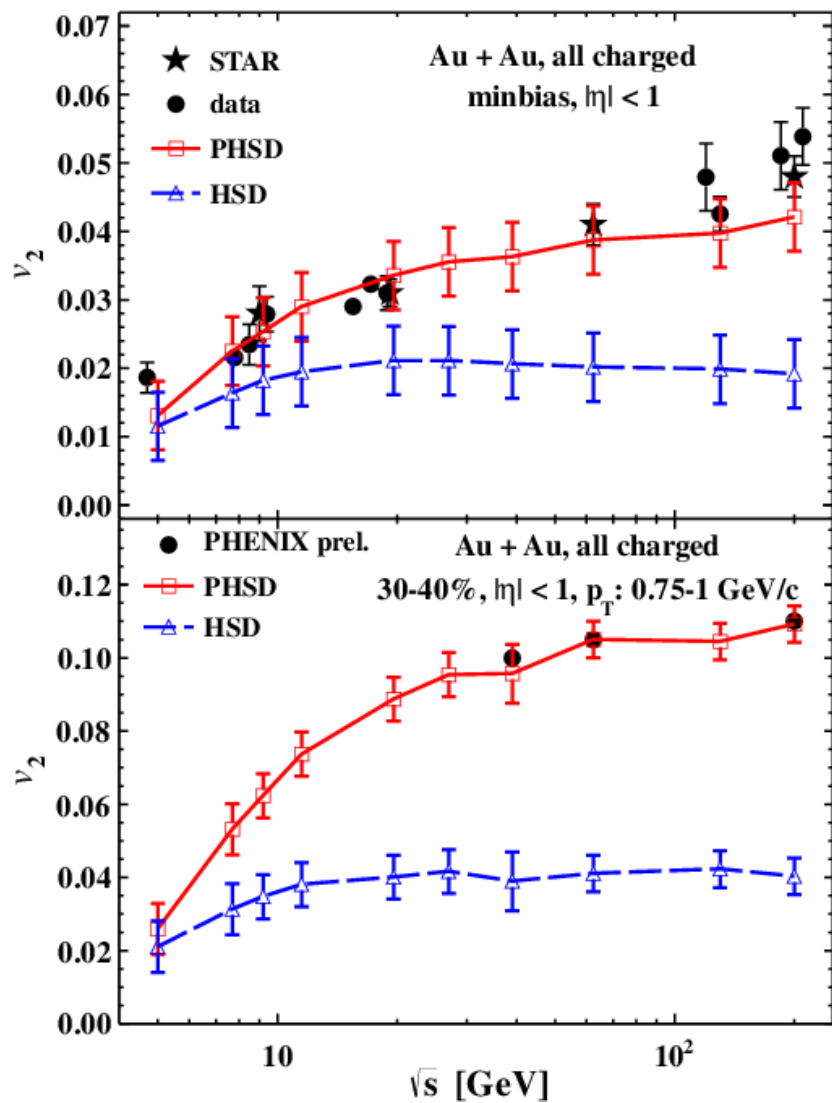
◆ In peripheral collisions the duration of the partonic phase is short.

◆ Collective flow is formed mainly during the partonic phase.

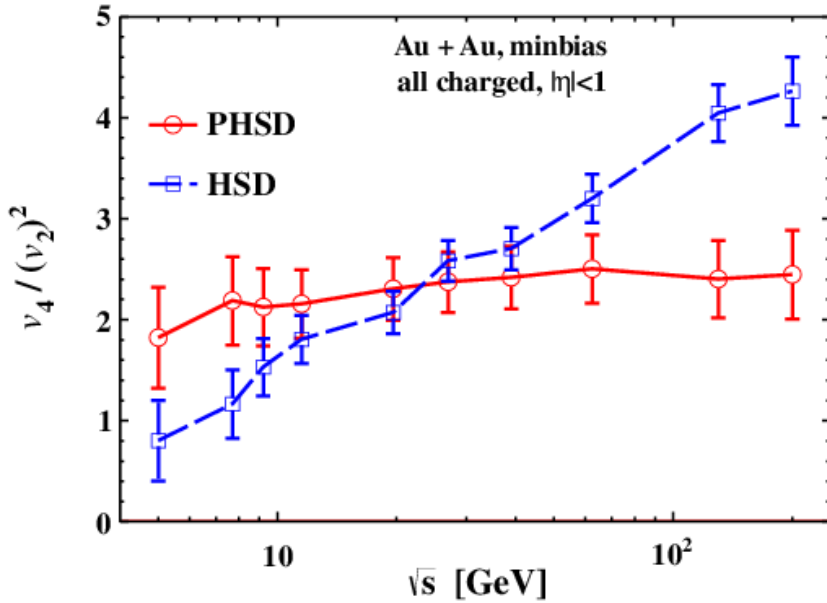


Phys. Rev. C85, 044922 (2012)

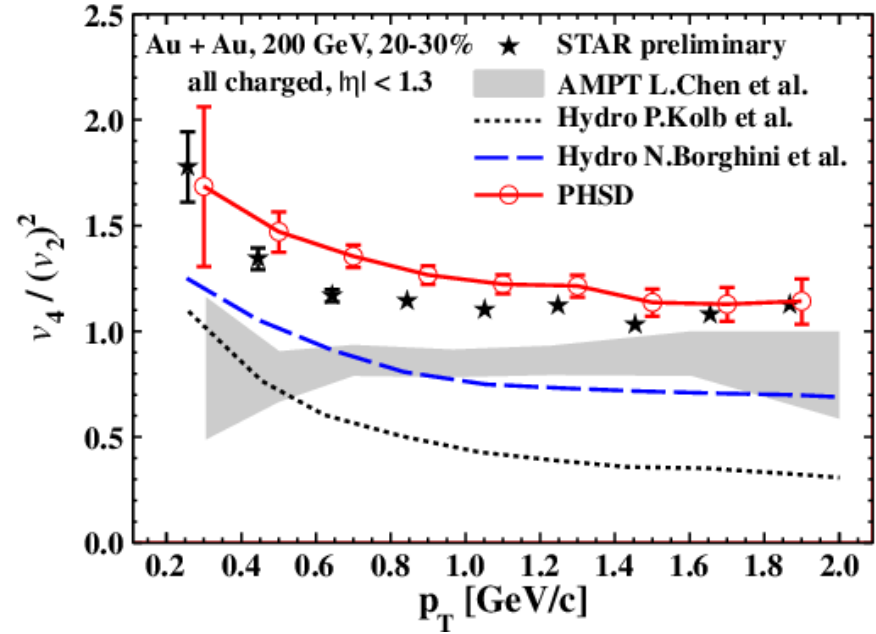
# More excitation functions



# Ratio $v_4 / v_2^2$

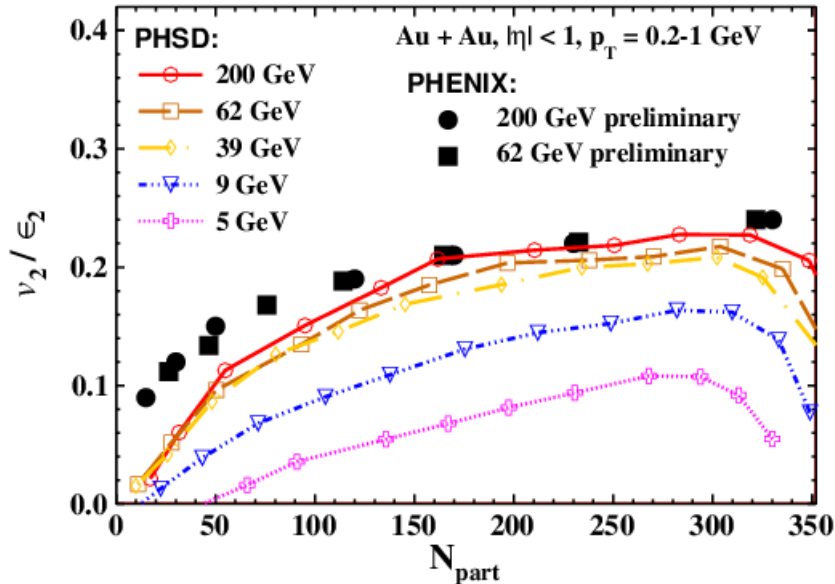


$v_4 / (v_2)^2$  is almost constant  
vs energy for PHSD



Not compatible with ideal  
hydrodynamics and very sensitive  
to the microscopic dynamics

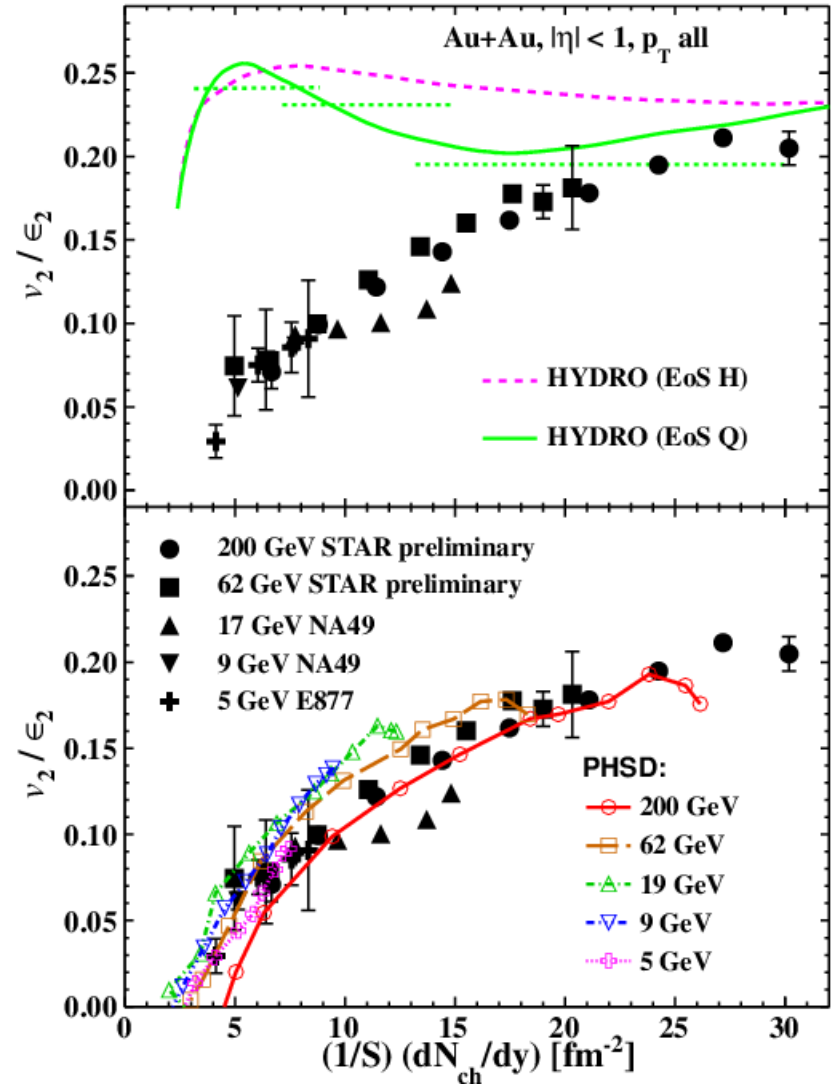
# Scaling properties



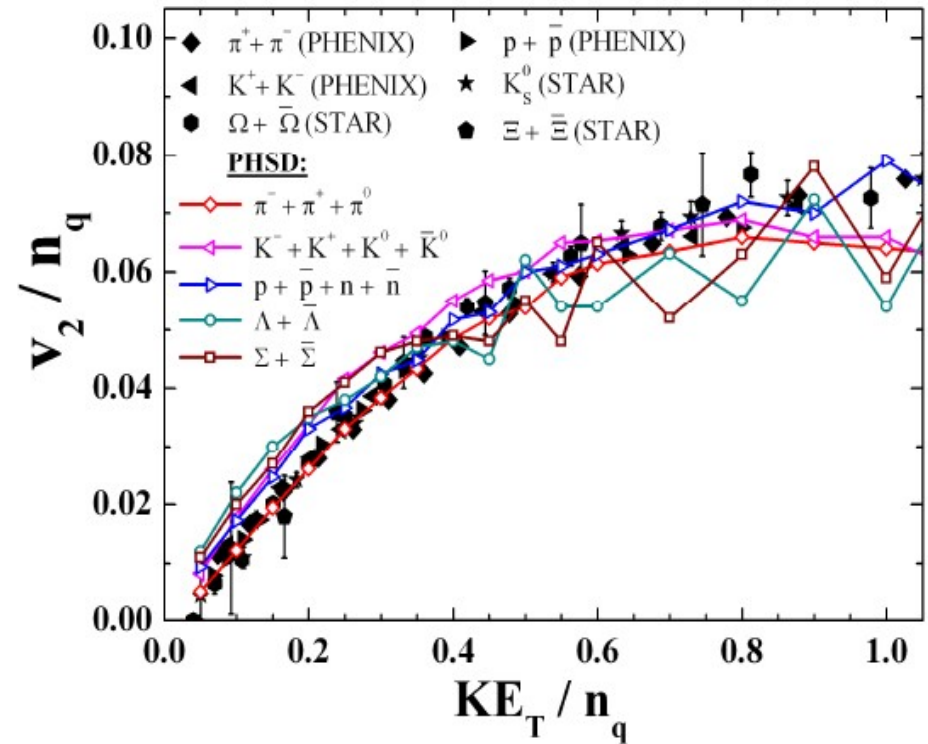
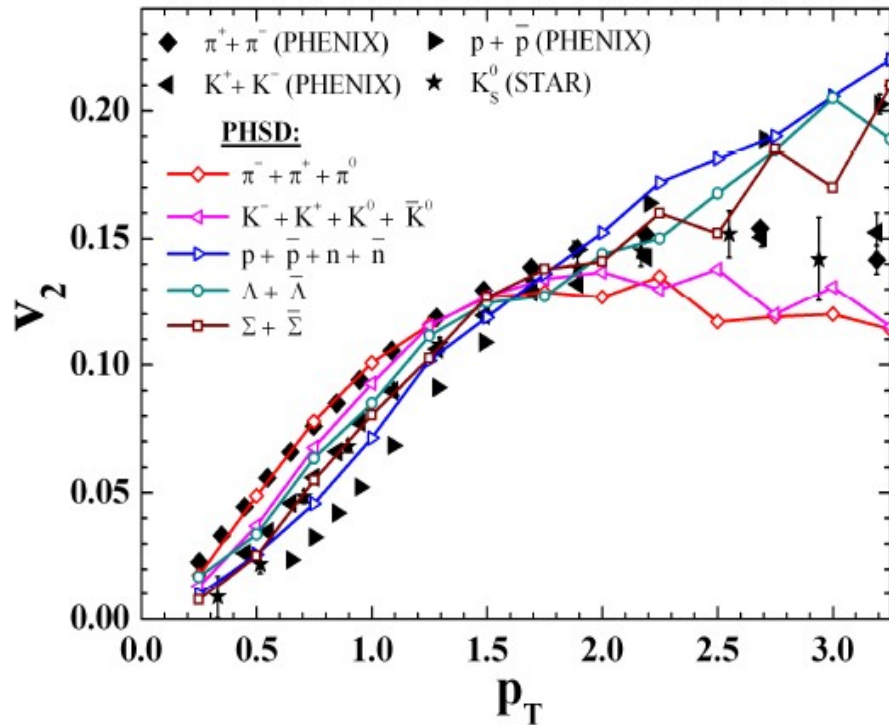
Initial assymetry:

$$\text{eccentricity } \epsilon_2 = \langle y^2 - x^2 \rangle / \langle x^2 + y^2 \rangle$$

“universal” scaling approximately works in PHSD  
but fails in hydrodynamics



# Quark number scaling

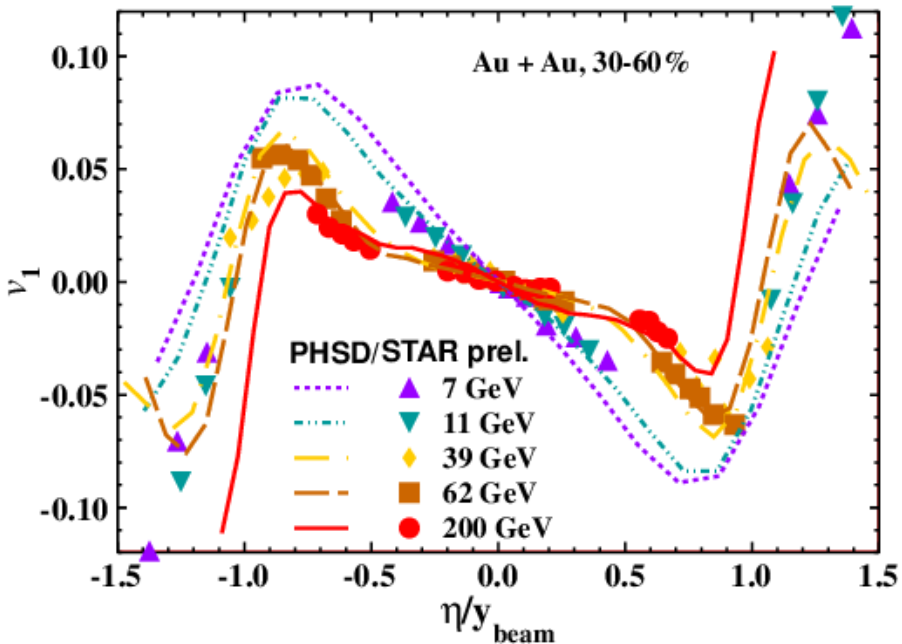


- The mass splitting at low  $p_T$  is approximately reproduced as well as the baryon-meson splitting for  $p_T > 2$  GeV/c
- The scaling of  $v_2$  with the number of constituent quarks is roughly in line with the data

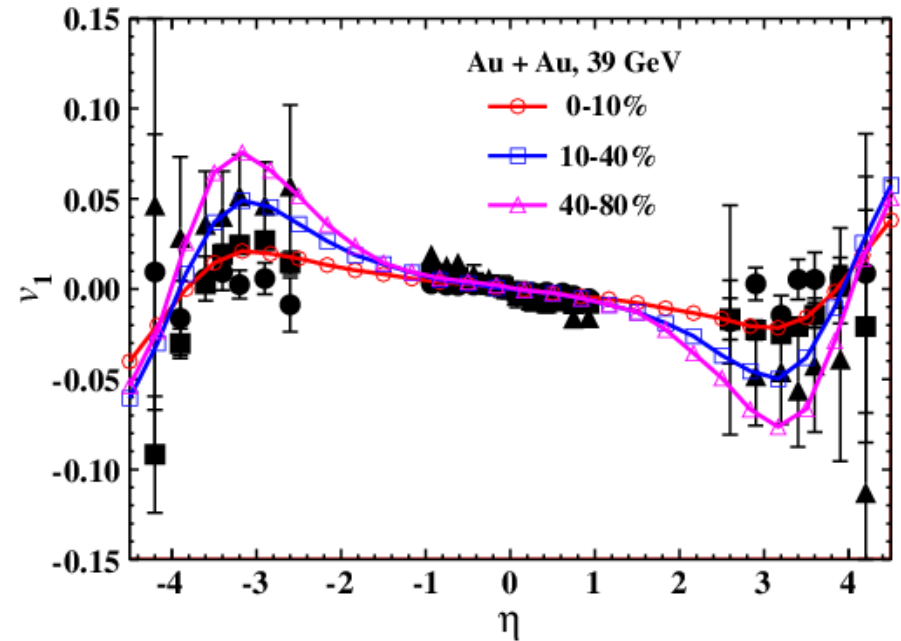


# Direct flow $v_1$

energy dependence



centrality dependence



**PHSD:  $v_1$  vs. pseudo-rapidity follows an approximate scaling for higher energies – in line with experimental data – whereas at low energies the scaling is violated!**

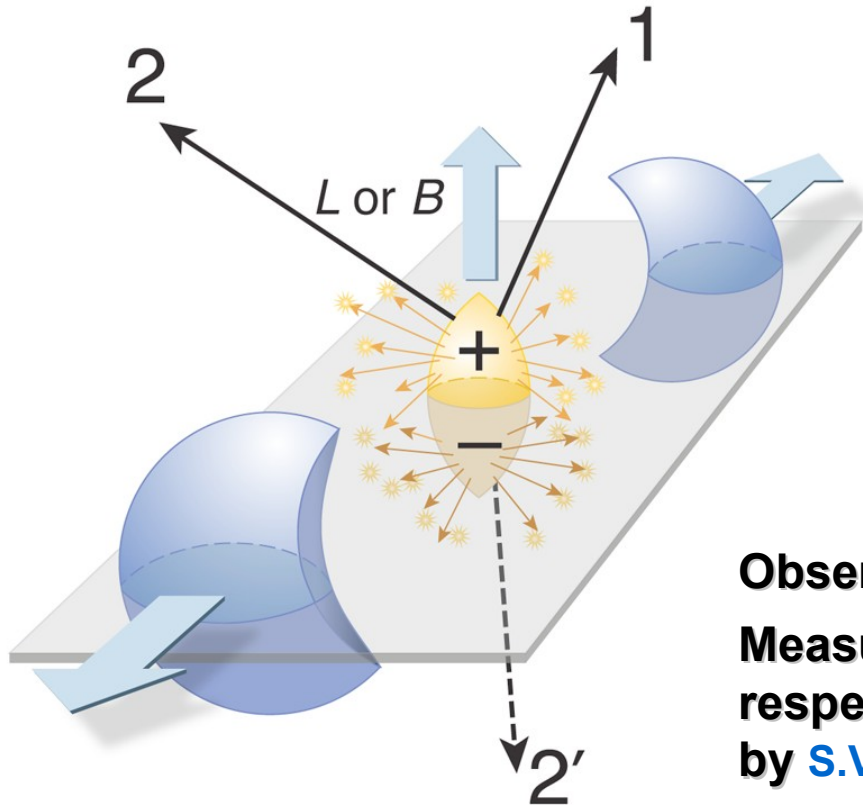
# CME: Charge separation in HIC

Nontrivial topological configurations exist in the QCD vacuum.

Transition between these states leads to a local P and CP symmetry violation.

The fluctuation of topological charges **in the presence** of magnetic field induces an electric current which will separate different charges.

illustration: Carin Cain



D.Kharzeev, PLB 633 (2006) 260.

In heavy-ion collision a **strong magnetic field** is produced mainly from charged **spectators**

Is the observed charge separation a signature of spontaneous chiral symmetry breaking?

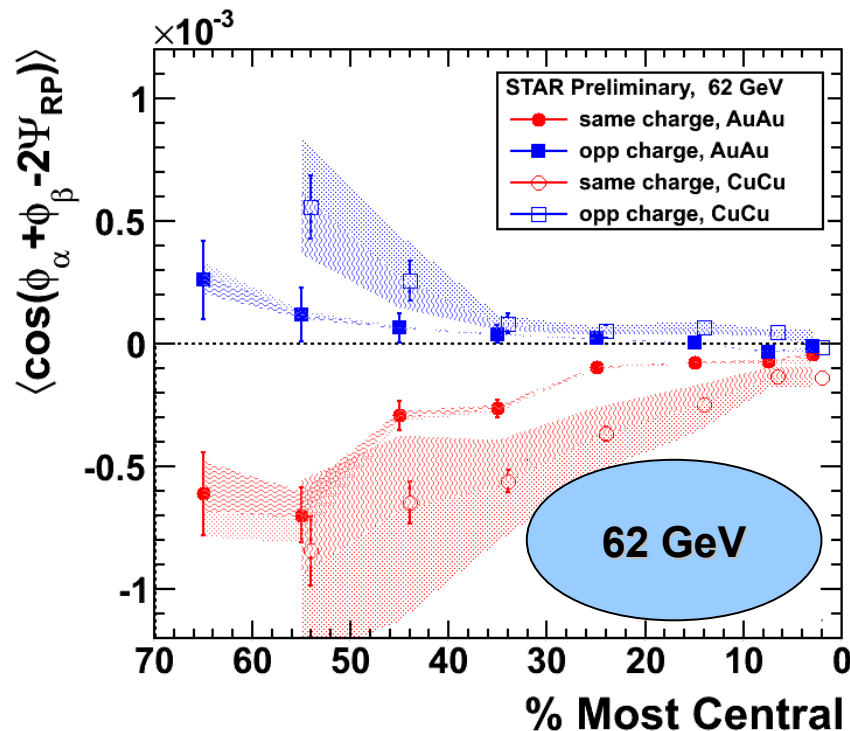
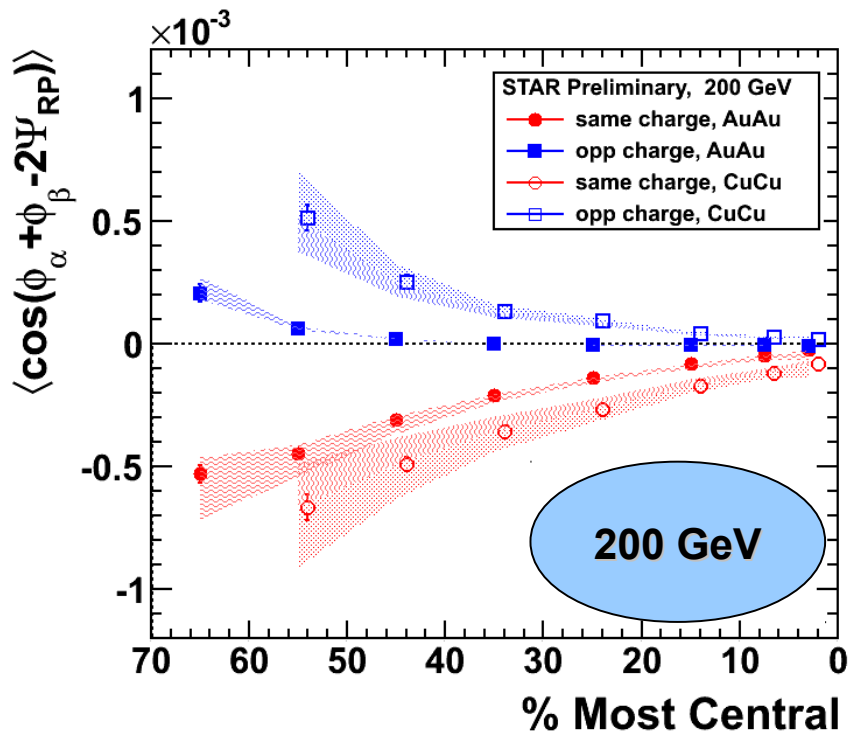
Observable:  $\langle \cos(\varphi_a + \varphi_b - 2\psi_{RP}) \rangle$

Measuring the charge separation with respect to the reaction plane was proposed by S.Voloshin, Phys. Rev. C 70 (2004) 057901.

# Charge separation in RHIC experiments

STAR Collaboration, PRL 103 (2009) 251601

$$\langle \cos(\varphi_a + \varphi_b - 2\Psi_{RP}) \rangle$$



Combination of intense B and deconfinement is needed for a spontaneous parity violation signal

# Hadron-String-Dynamics HSD



**Retarded electromagnetic field**

# Transport model with electromagnetic field

The Boltzmann equation is the basis of BUU like models:

$$\left\{ \frac{\partial}{\partial t} + \dot{\vec{r}} \cdot \vec{\nabla}_{\vec{r}} + \dot{\vec{p}} \cdot \vec{\nabla}_{\vec{p}} \right\} f(\vec{r}, \vec{p}, t) = I_{coll}(f, f_1, \dots, f_N)$$

Generalized on-shell transport equations in the presence of **electromagnetic fields** can be obtained formally by the substitution:

$$\dot{\vec{r}} \rightarrow \frac{\vec{p}}{p_0} + \vec{\nabla}_{\vec{p}} U,$$

$$\dot{\vec{p}} \rightarrow -\vec{\nabla}_{\vec{r}} U + e\vec{E} + e\vec{v} \times \vec{B}$$

$$\left\{ \frac{\partial}{\partial t} + \left( \frac{\vec{p}}{p_0} + \vec{\nabla}_{\vec{p}} U \right) \vec{\nabla}_{\vec{r}} - \left( \vec{\nabla}_{\vec{r}} U - e\vec{E} - e\vec{v} \times \vec{B} \right) \vec{\nabla}_{\vec{p}} \right\} f(\vec{r}, \vec{p}, t) = I_{coll}(f, f_1, \dots, f_N)$$

$U \sim \text{Re}(\Sigma^{ret})/2p_0$

A general solution of the wave equations

$$\left\{ \begin{array}{l} \vec{B} = \vec{\nabla} \times \vec{A} \\ \vec{E} = -\vec{\nabla} \Phi - \frac{\partial \vec{A}}{\partial t} \end{array} \right.$$

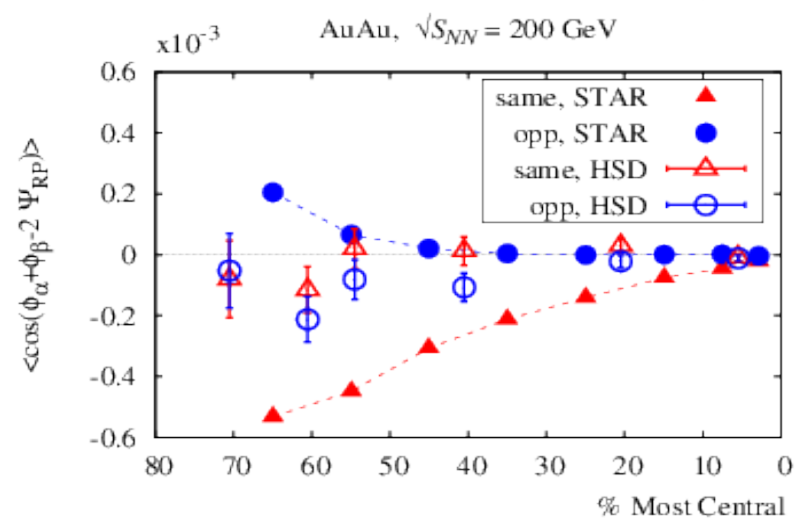
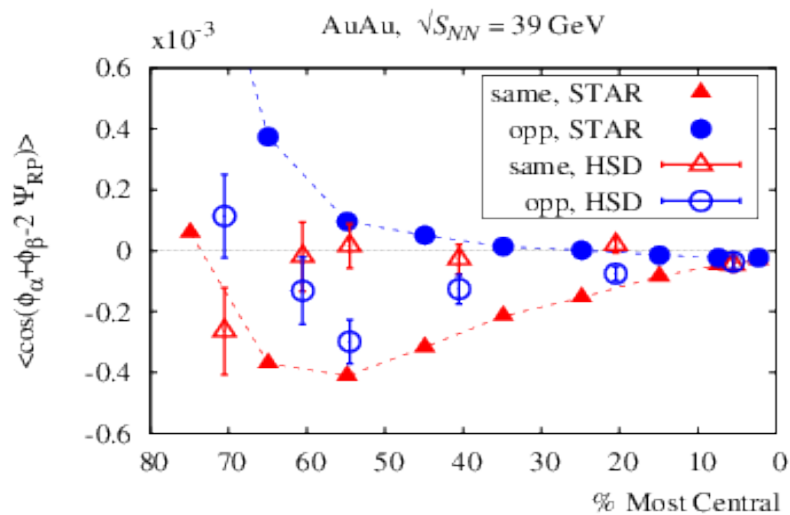
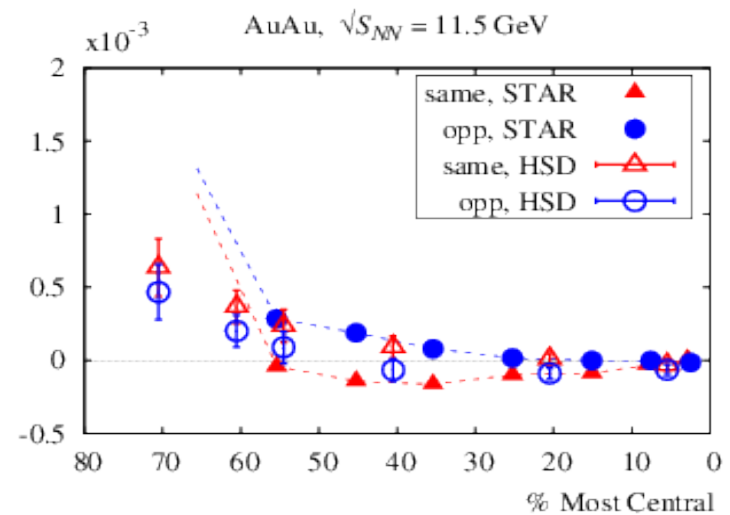
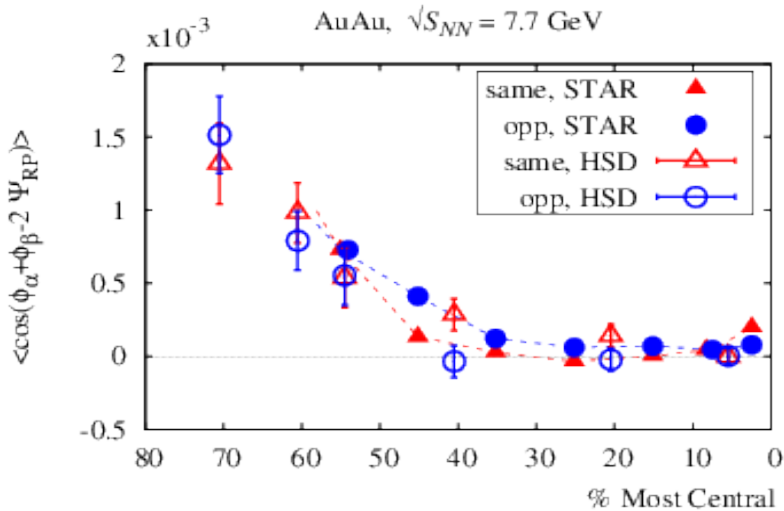
is as follows

$$\vec{A}(\vec{r}, t) = \frac{1}{4\pi} \int \frac{\vec{j}(\vec{r}', t') \delta(t - t' - |\vec{r} - \vec{r}'|/c)}{|\vec{r} - \vec{r}'|} d^3r' dt'$$

$$\Phi(\vec{r}, t) = \frac{1}{4\pi} \int \frac{\rho(\vec{r}', t') \delta(t - t' - |\vec{r} - \vec{r}'|/c)}{|\vec{r} - \vec{r}'|} d^3r' dt'$$

For point-like particles  $\rho(\vec{r}, t) = e \delta(\vec{r} - \vec{r}(t)); \quad \vec{j}(\vec{r}, t) = e \vec{v}(t) \delta(\vec{r} - \vec{r}(t)) \quad \vec{\nabla} \times \vec{A} \rightarrow \text{LW eq.}$

# Angular correlations

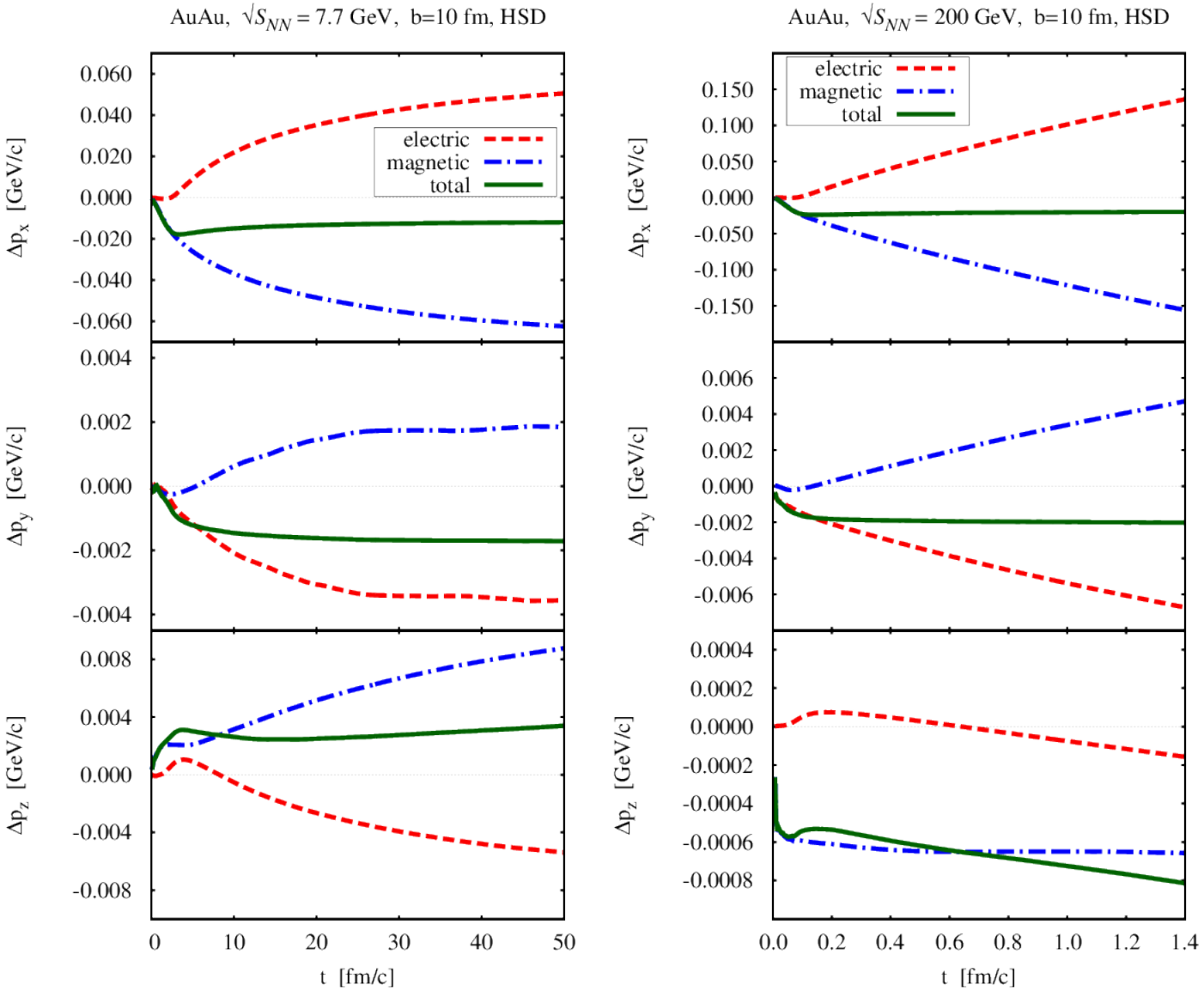


are well described by hadronic sources up to 11 GeV

V.D. Toneev et al., Phys.Rev. C85, 034910 (2012)



# Compensation of magnetic and electric forces



# Summary



- **PHSD** model with direct inclusion of quarks and gluons **provides a consistent description** of off-shell parton dynamics in line with a lattice QCD equation of state.
- A study of the elliptic flow  $v_2$  (as well as  $v_3$  and  $v_4$ ) from  $\sqrt{s} = 7.7$  GeV to 200 GeV has been made in the PHSD on an event-by-event basis. **Partonic degrees of freedom gives a rise in the elliptic flow with energy observed experimentally**
- **Quark number scaling** is described by PHSD
- The **HSD** transport model **with retarded electromagnetic fields** has been developed. Actual calculations show no noticeable influence of the created electromagnetic fields on observables. This happens due to a compensating effect between electric and magnetic fields

# Thanks

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